



Precision measurements with Kaons at CERN

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Precision measurements with Kaons at CERN

1. First measurement of $K^{\pm} \rightarrow \pi^0 \pi^0 \mu^{\pm} \nu$ [PRELIMINARY]
2. New study of $K^+ \rightarrow \pi^0 e^+ \nu \gamma$ [PRELIMINARY]
3. Measurement of $K^+ \rightarrow \pi^+ \mu^+ \mu^-$ [PRELIMINARY]

Kaon physics at CERN

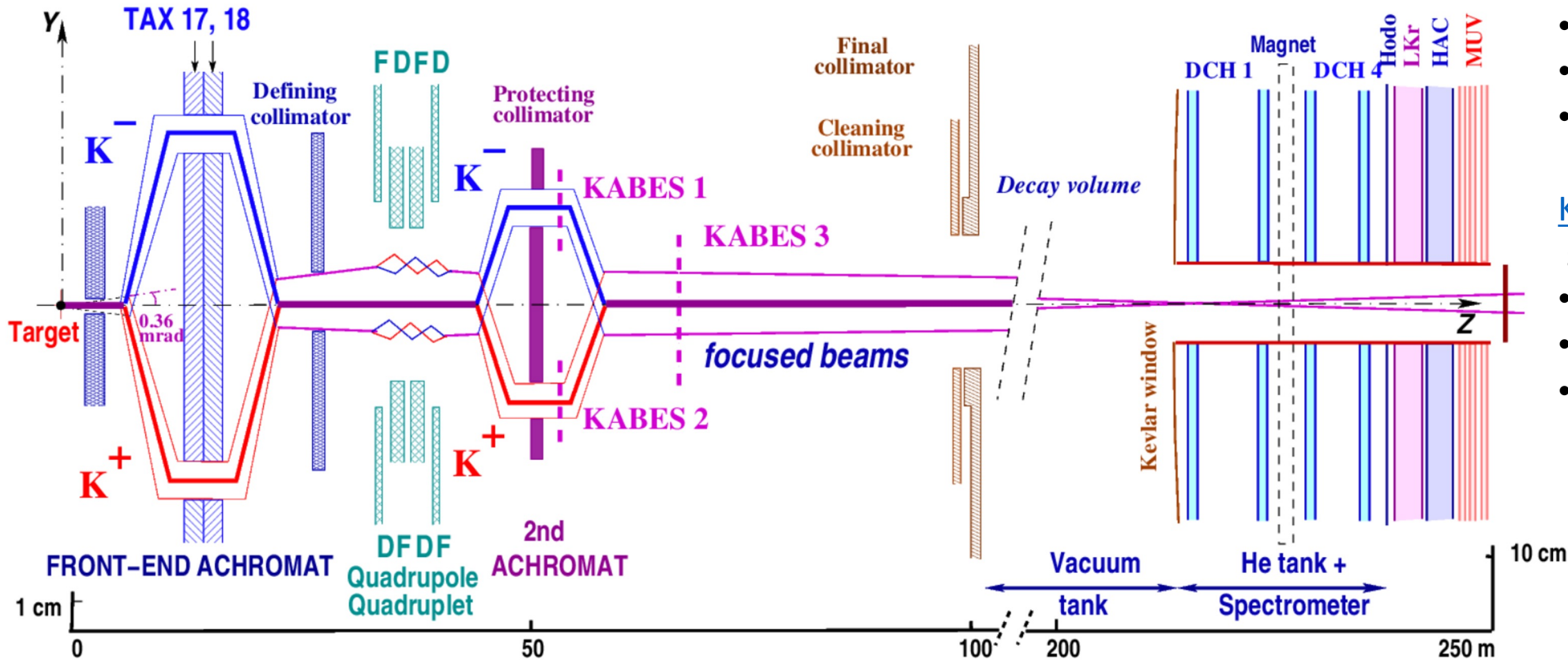
- Significant history of kaon physics experiments in the CERN North Area (NA)
- Today I will show results from NA48/2 and NA62



Recent history of NA kaon experiments

1984		
↓	NA31 (K_S/K_L)	First evidence of direct CPV
1990		
↓	NA48 (K_S/K_L)	Re ϵ'/ϵ Discovery of direct CPV
1997		
↓	NA48/1 (K_S /hyperons)	Rare K_S and hyperon decays
2001		
↓	NA48/2 (K^+/K^-)	Direct CPV Rare K^+ / K^- decays
2002		
↓	NA62 R_K phase (K^+/K^-)	$R_K = K_{ev}^\pm / K_{\mu\nu}^\pm$
2003		
↓	NA62 (K^+)	$K^+ \rightarrow \pi^+ \nu \bar{\nu}$ Rare K^+ and π^0 decays
2004		
↓		
2007		
↓		
2008		
↓		
2016		
↓		
2018		

The NA48/2 beamline



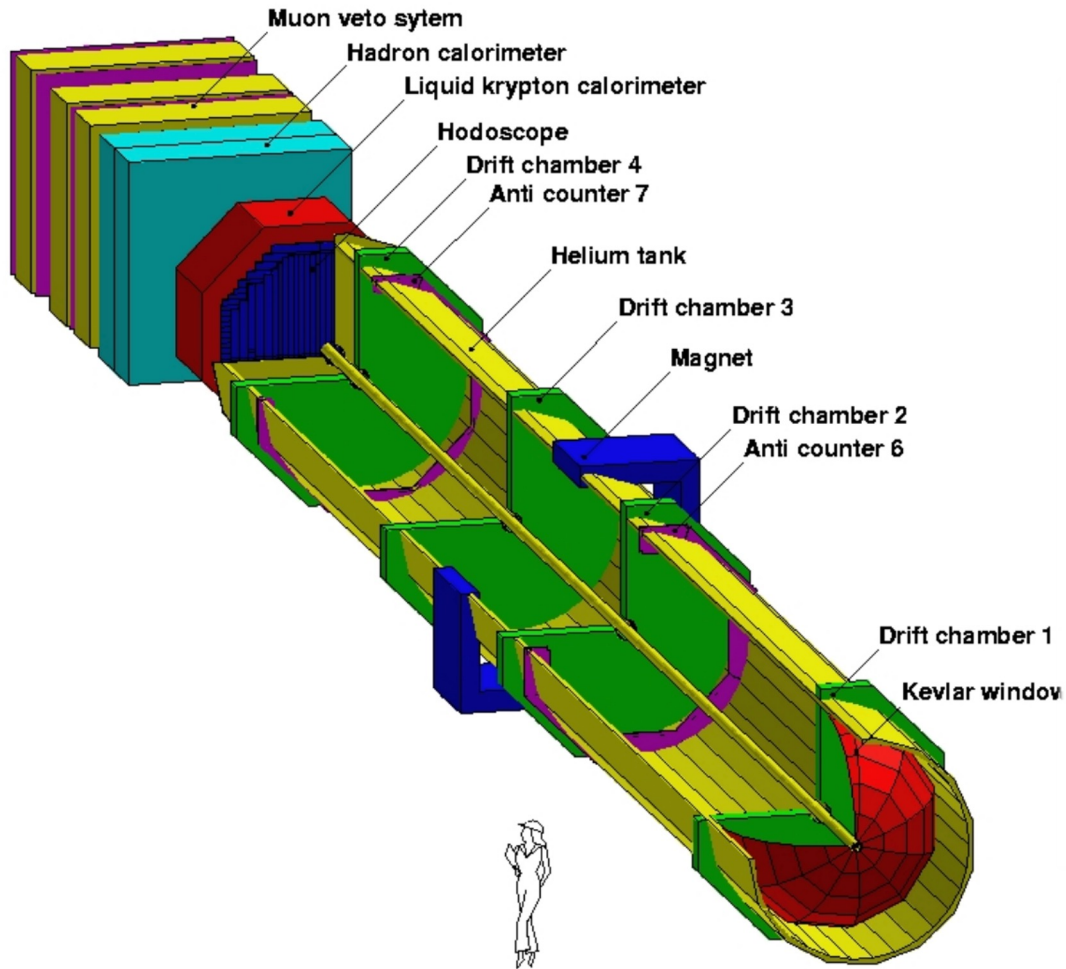
- Two charged beams:
- 6% of K^\pm
 - $\langle P_K \rangle \approx 60 \text{ GeV}/c$
 - $\Delta P_K / \langle P_K \rangle \approx \pm 3.8\%$

KABES (kaon beam spectrometer):

- $\sigma(X, Y) \sim 800 \mu\text{m}$
- $\sigma(P_K) \sim 1\%$
- $\sigma(T) \sim 600 \text{ ps}$

The NA48/2 detector

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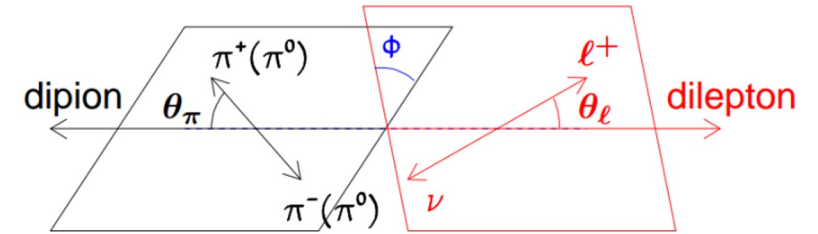


- Magnetic spectrometer (drift chambers DCH1–DCH4):
 - $\sigma(X, Y) \sim 90 \mu\text{m}$ per chamber
 - $\sigma(P_{DCH})/P_{DCH} = (1.02 \oplus 0.044 \cdot P_{DCH})\%$
(P_{DCH} in GeV/c)
- Scintillator hodoscope (HOD):
 - $\sigma(T) \sim 150 \text{ ps}$
- Liquid Krypton EM calorimeter (LKr):
 - $\sigma_x = \sigma_y = (0.42/\sqrt{E_\gamma} \oplus 0.06) \text{ cm}$
 - $\sigma(E_\gamma)/E_\gamma = (3.2/\sqrt{E_\gamma} \oplus 9.0/E_\gamma \oplus 0.42)\%$
(E_γ in GeV)
- Hadronic calorimeter, muon system MUV.

First measurement of $K^\pm \rightarrow \pi^0 \pi^0 \mu^\pm \nu$

$K \rightarrow \pi\pi\mu\nu (K_{l4})$ depends on F, G, R, H form-factors.

Cabibbo-Maksymowicz variables: S_π (dipion mass squared), S_l (dilepton mass squared) and angles θ_π (in the dipion frame), θ_l (in the dilepton frame), ϕ .



- For $K_{\mu 4}^{00}$, s-wave for $\pi^0 \pi^0$, there are no dependence on $\cos \theta_\pi, \phi$, and only F and R contribute.
- Unlike $K_{e 4}^{00}$ case, R plays some role due to μ mass.

K_{l4} mode	BR [10^{-5}]	N_{cand}	
$K_{e 4}^\pm$	4.26 ± 0.04	1108941	NA48/2 (2012)
$K_{e 4}^{00}$	2.55 ± 0.04	65210	NA48/2 (2014)
$K_{\mu 4}^\pm$	1.4 ± 0.9	7	Bisi et al. (1967)
$K_{\mu 4}^{00}$?	0	

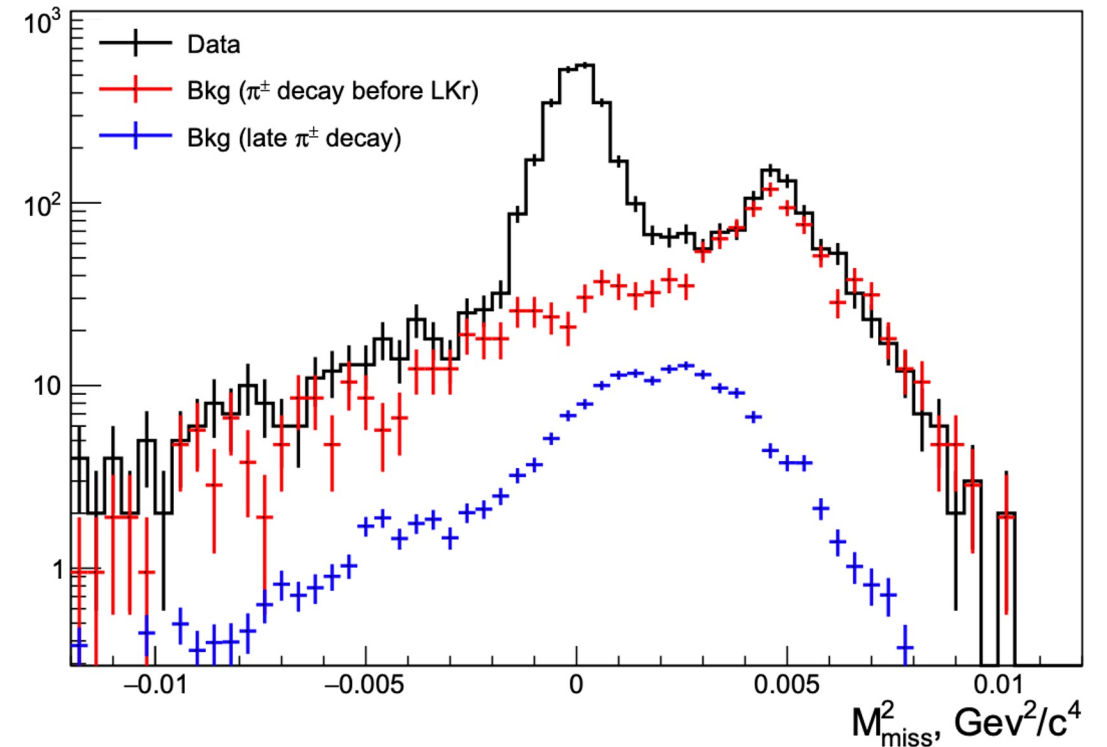
$K_{\mu 4}^{00}$: first observation, ChPT test, check of R presence, potential study of $\pi\pi$ rescattering effects in the $F(S_\pi)$.

$K_{\mu 4}$: huge bkg $K^\pm \rightarrow \pi\pi(\pi^\pm \rightarrow \mu^\pm \nu)$.

- To simulate $K^\pm \rightarrow \pi^0 \pi^0 \mu^\pm \nu$ decays, can use parameterisation of $F(S_\pi, S_\ell)$ from $K_{e 4}^{00}$ measurements [[NA48/2 JHEP 08 \(2014\) 159](#)]
- The only available source of $R(S_\pi, S_\ell)$ is ChPT calculation [[J. Bijnens, G. Colangelo, J. Gasser, Nucl. Phys. B 427 \(1994\) 427](#)]

Event selection

- Signal is $K^\pm \rightarrow \pi^0 \pi^0 \mu^\pm \nu$
- Normalised to $K^\pm \rightarrow \pi^\pm \pi^0 \pi^0$
- Event selection: 4 isolated photons consistent with $2\pi^0$ matched in time and space with a KABES beam track and a DCH track with associated MUV response
- The main background is $K^\pm \rightarrow \pi^\pm \pi^0 \pi^0$ with $\pi^\pm \rightarrow \mu^\pm \nu$ decay-in-flight before LKr
- Cuts imposed on 3-pion mass and p_T , missing mass, and $\cos(\theta_\ell)$
- Number of background events extracted from a fit to missing mass sidebands

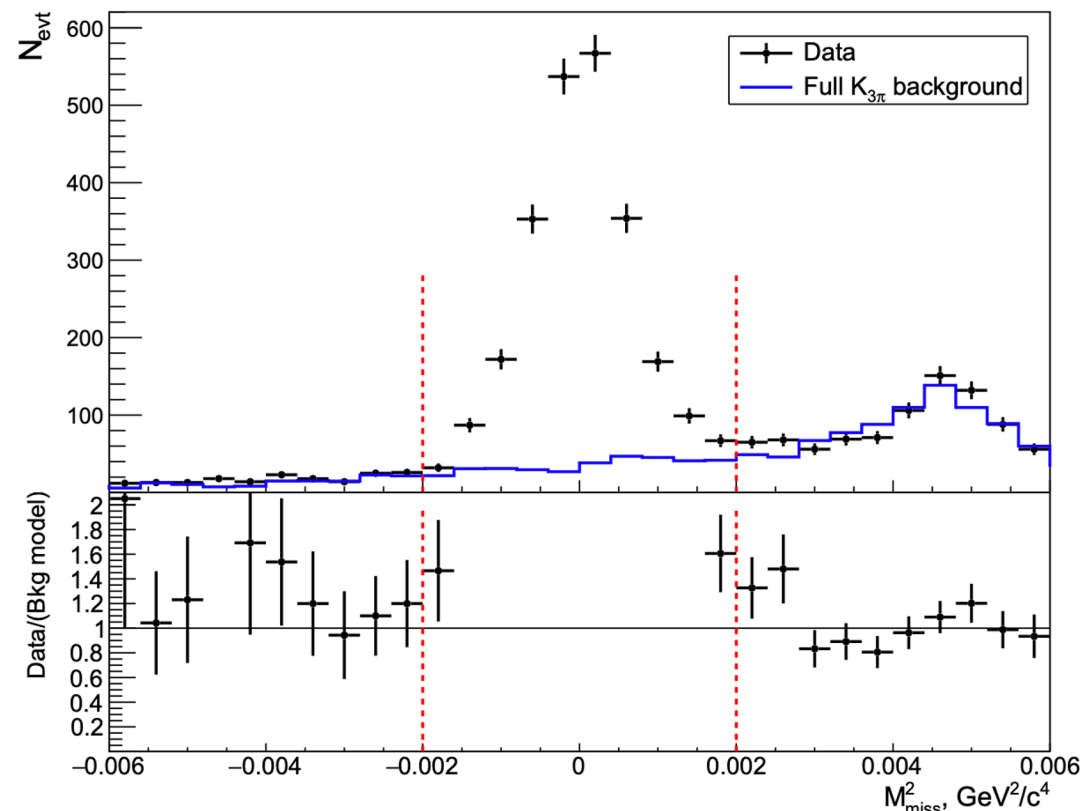


Event selection

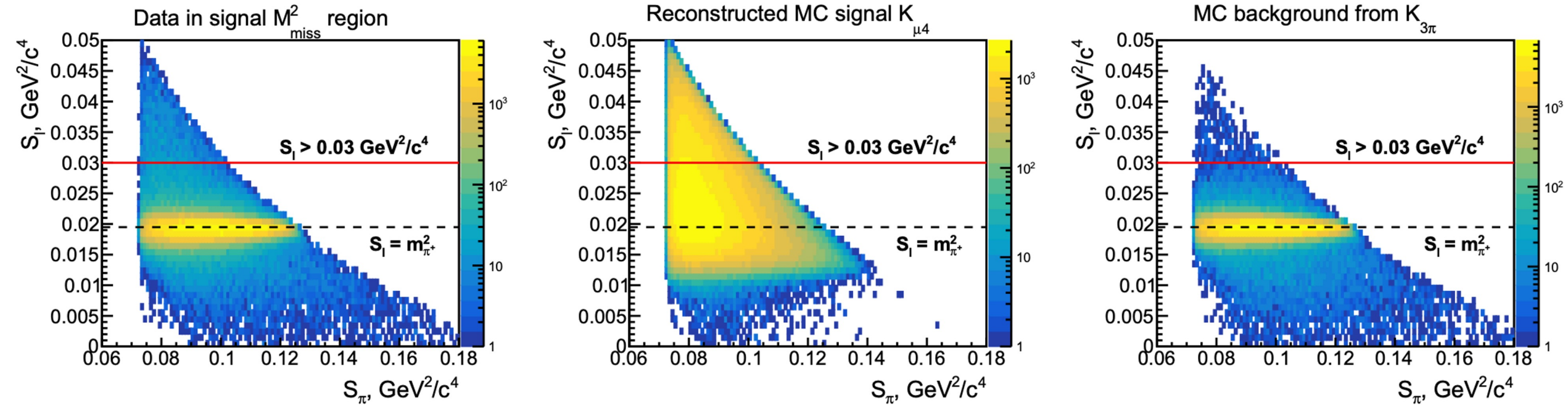
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2437 candidates in signal region

$354 \pm 33_{stat}$ background events



Full and restricted phase-space



- The branching ratio is measured for the restricted phase space $S_{\pi^+}^{\text{true}} > 0.03 \text{ GeV}^2/c^4$.
- Extrapolation to the full phase space depends on the theory.

Ingredients to the branching ratio

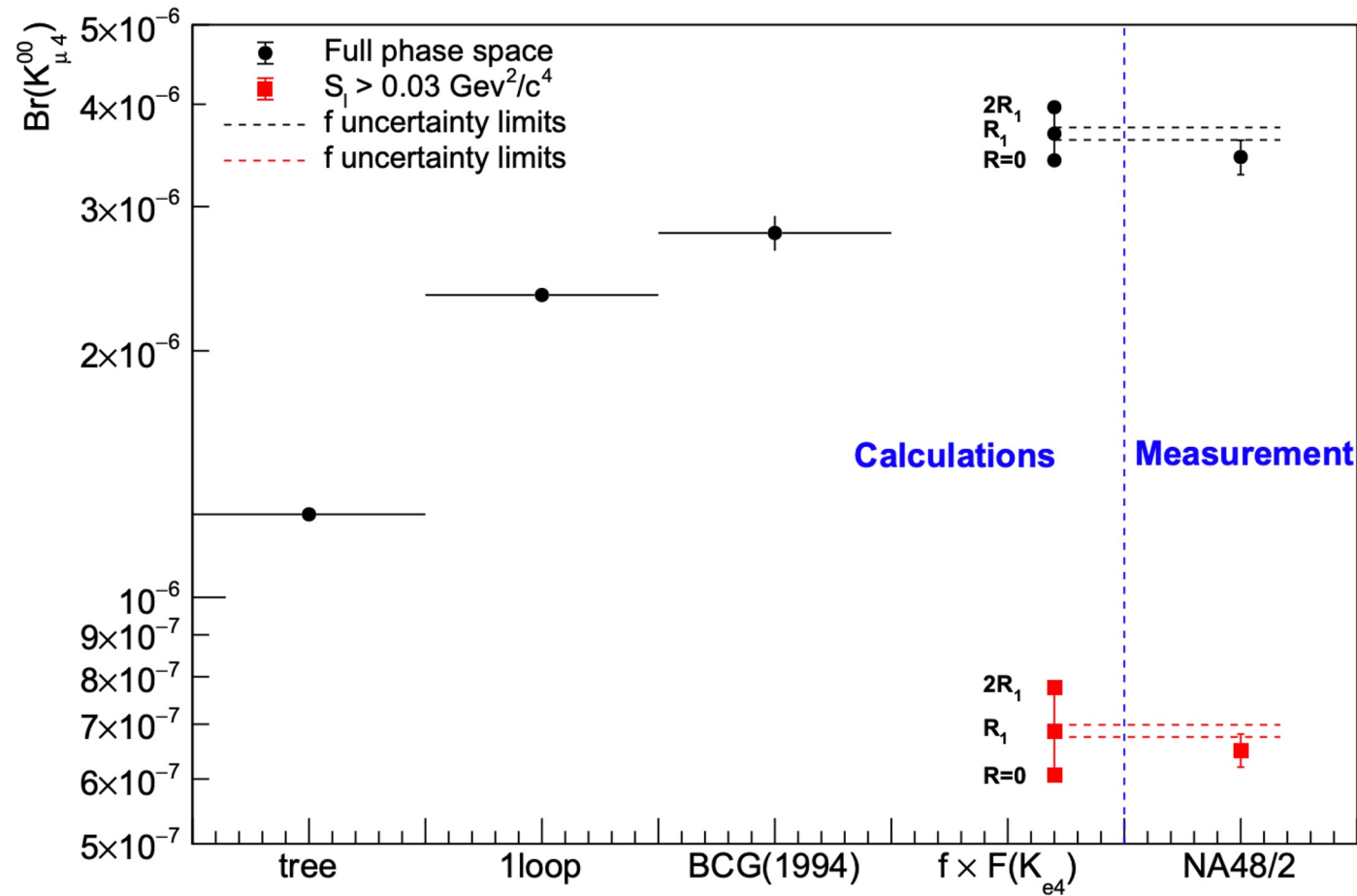
$$BR(K_{\mu 4}^{00}) = \frac{N_S}{N_N} \cdot \frac{A_N}{A_S} \cdot K_{trig} \cdot BR(K_{3\pi}^{00}).$$

- Extracted signal $N_S = N_{Sign. \text{ cand.}} - N_{Bkg} = 2437 - (354 \pm 33_{stat}) = 2083 \pm 59_{stat}$ events;
 - Signal/Background is $5.89 \pm 0.66_{stat}$;
- Number of normalization events $N_N = 72.99 \times 10^6$;
- Normalization acceptance $A_N = (4.477 \pm 0.002)\%$;
- Signal acceptance for the restricted phase space $A_S^r = (3.453 \pm 0.007)\%$;
- Signal acceptance for the full phase space $A_S = (0.651 \pm 0.001)\%$;
- Trigger correction (extracted with control triggers)
 $K_{trig} = K_{CHT} \cdot K_{NUT} = (0.998 \pm 0.002) \cdot (1.0007 \pm 0.0007) = 0.999 \pm 0.002$;
- PDG $BR(K_{3\pi}^{00}) = (1.760 \pm 0.023)\%$;

Systematic uncertainties

	Full phase space		$S_I > 0.03 \text{ GeV}^2/c^4$	
$BR(K_{\mu 4})$ central value [10^{-6}]	3.45		0.651	
	$\delta BR [10^{-6}]$	$\delta BR / BR$	$\delta BR [10^{-6}]$	$\delta BR / BR$
Data stat. error	0.10	2.85%	0.019	2.85%
MC stat. error	0.01	0.21%	0.001	0.21%
Trigger	0.01	0.18%	0.001	0.18%
Background	0.10	2.96%	0.019	2.96%
Accidentals	0.01	0.32%	0.002	0.32%
MUV inefficiency	0.06	1.65%	0.011	1.65%
Form Factor modelling	0.05	1.37%	0.001	0.14%
$BR(K_{3\pi})$ error (external)	0.05	1.31%	0.009	1.31%
Total error	0.17	4.83%	0.030	4.64%

Comparison to theory predictions

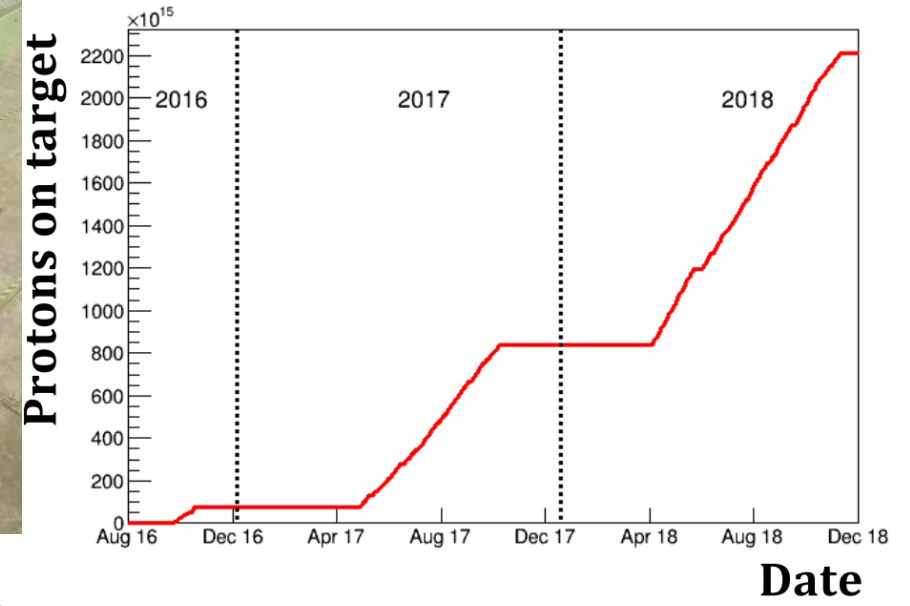
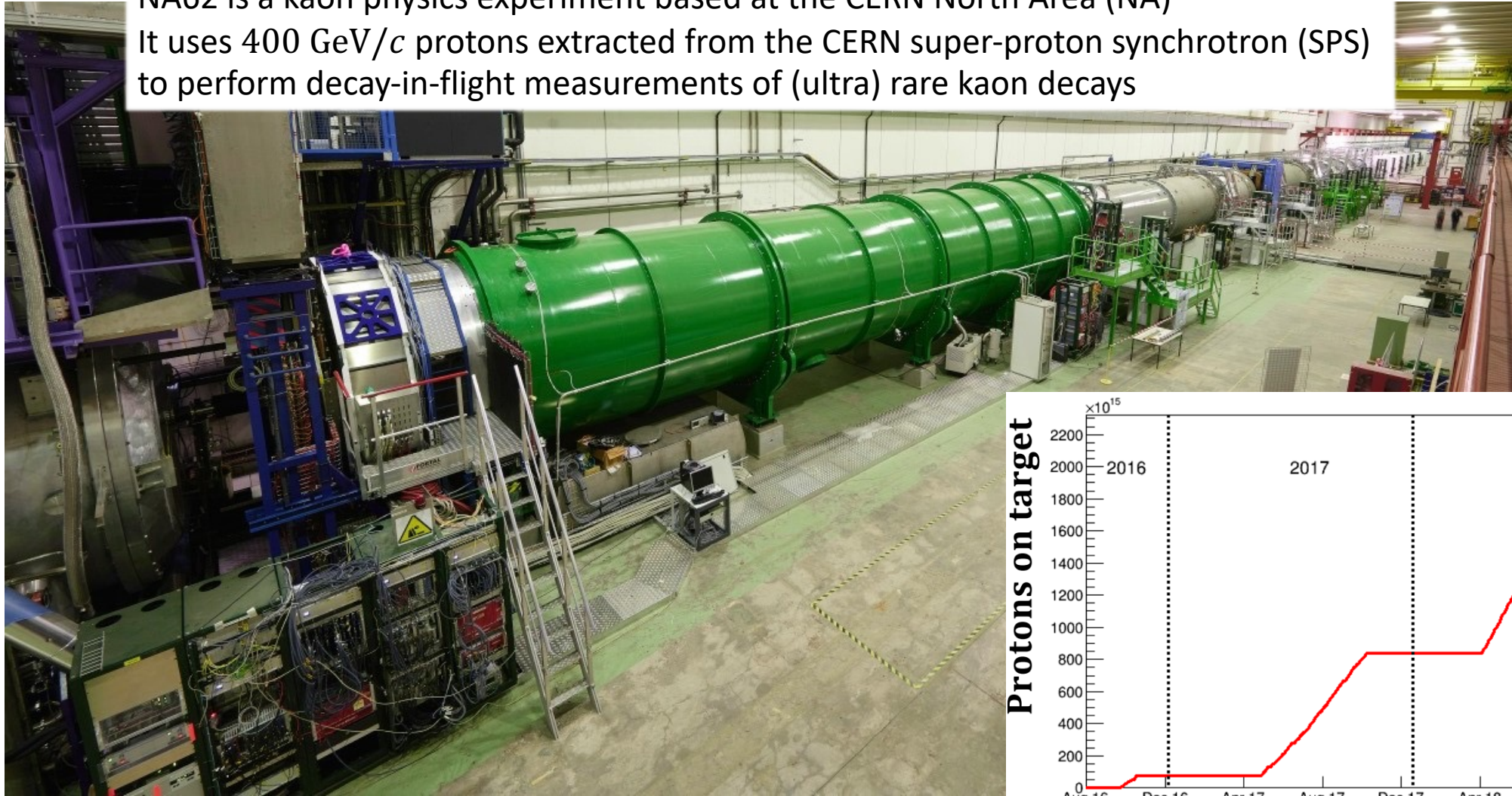


Theory:

- J. Bijnens, G. Colangelo, J. Gasser, Nucl. Phys. B, 427 (1994) 427:
 - Tree approximation;
 - 1-loop;
 - BCG(1994): 'beyond 1-loop' with measured F from [Rosset et al. Phys. Rev. D 15 (1977) 574].
- Re-calculated now:
 - $F(K_{e4})$ from NA48/2 (2015);
 - $R_1 = R(1loop)$;
 - 1-loop (F,R) phase;
 - 2020 PDG constants.

The NA62 experiment

NA62 is a kaon physics experiment based at the CERN North Area (NA)
It uses 400 GeV/c protons extracted from the CERN super-proton synchrotron (SPS)
to perform decay-in-flight measurements of (ultra) rare kaon decays

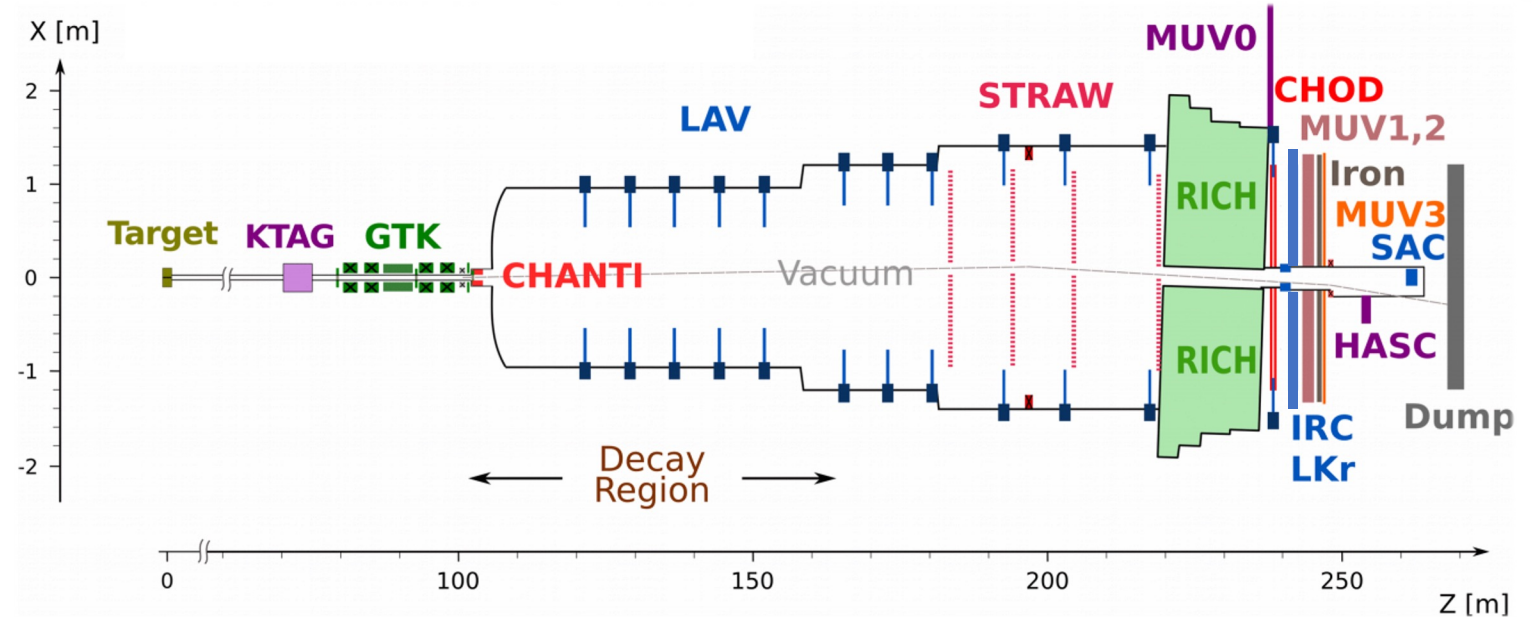


The NA62 detector

[JINST 12 P05025]

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400 GeV/c protons from CERN SPS
Slow extraction in 'spills' of 5 seconds



- Proton-target interactions + achromatic selector forms secondary hadron beam with $p \approx 75 \text{ GeV}/c$
 - There are 750MHz of particles in the secondary beam; 6% are K^+ (45MHz)
- Measurement of all beam particles by kaon tagger **KTAG** and beam-particle tracker **GTK**
- About 15% of K^+ decay within the $\sim 75\text{m}$ vacuum **decay region**, which defines the experiments **fiducial volume**
- Measurement of K^+ decay products by the **STRAW** tracker and **CHOD** detectors
- Particle identification by the **RICH**, the **LKr** and **MUV** calorimeters, and the **MUV3** detector
- Hermetic photon veto provided by the **LAV**, **LKr**, **IRC**, **SAC** photon detectors

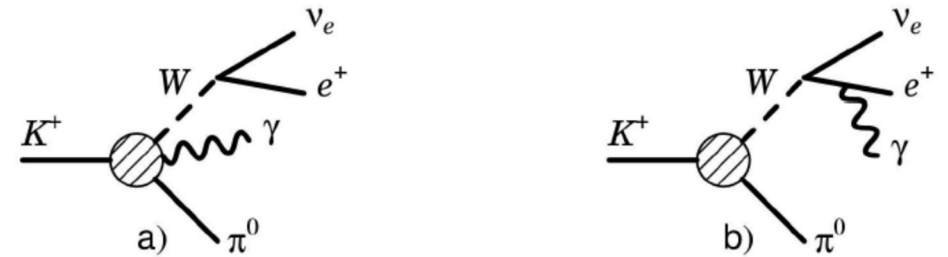
New study of $K^+ \rightarrow \pi^0 e^+ \nu \gamma$

[Nucl. Phys. B 396 \(1993\) 81](#)
[Phys. Rev. D 65 \(2002\) 054038](#)
[Eur. Phys. J. C 50 \(2007\) 557](#)
[Phys. Atom. Nucl. 74 \(2011\) 1214](#)

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- The $K^+ \rightarrow \pi^0 e^+ \nu \gamma$ decay is a radiative decay described in ChPT, with the photon produced either via direct emission (DE) and inner bremsstrahlung (IB)
- The IB amplitude diverges when $E_\gamma \rightarrow 0$ and $\theta_{e,\gamma} \rightarrow 0$
- Measure branching fraction ratio $R = BR(\pi^0 e^+ \nu \gamma) / BR(\pi^0 e \nu)$ in 3 kinematic regions R_j

DE (a) + IB (b) + INT



[arxiv:2010.07983](#)

Range	E_γ cut	$\theta_{e,\gamma}$ cut	$O(p^6)$ ChPT [10^{-2}]	ISTRA + [10^{-2}]	OKA [10^{-2}]
R_1	$E_\gamma > 10 \text{ MeV}$	$\theta_{e,\gamma} > 10^\circ$	1.804 ± 0.021	$1.81 \pm 0.03 \pm 0.07$	$1.990 \pm 0.017 \pm 0.021$
R_2	$E_\gamma > 30 \text{ MeV}$	$\theta_{e,\gamma} > 20^\circ$	0.640 ± 0.008	$0.63 \pm 0.02 \pm 0.03$	$0.587 \pm 0.010 \pm 0.015$
R_3	$E_\gamma > 10 \text{ MeV}$	$0.6 < \cos \theta_{e,\gamma} < 0.9$	0.559 ± 0.006	$0.47 \pm 0.02 \pm 0.03$	$0.532 \pm 0.010 \pm 0.012$

[Phys. Atom. Nucl. 70, 29 \(2007\)](#)

New study of $K^+ \rightarrow \pi^0 e^+ \nu \gamma$

- The decay is also sensitive to a T-odd observable ξ , with asymmetry in ξ defined as A_ξ

$$\xi = \frac{\vec{p}_\gamma \cdot (\vec{p}_e \times \vec{p}_\pi)}{M_K^3} ; A_\xi = \frac{N_+ - N_-}{N_+ + N_-}$$

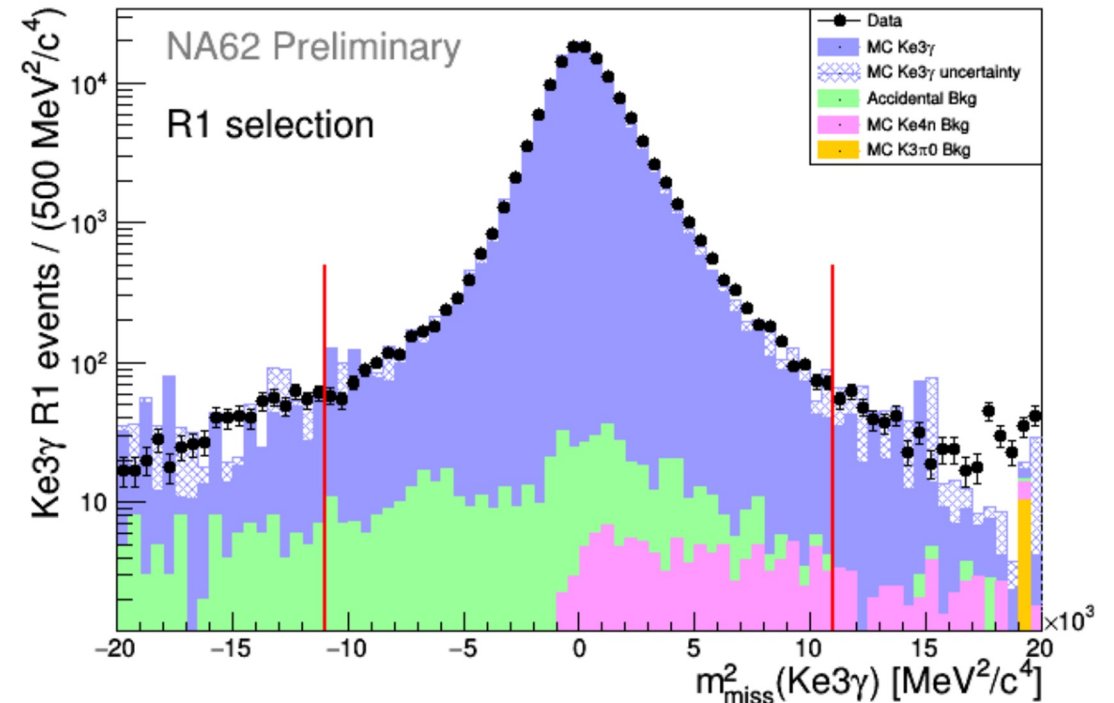
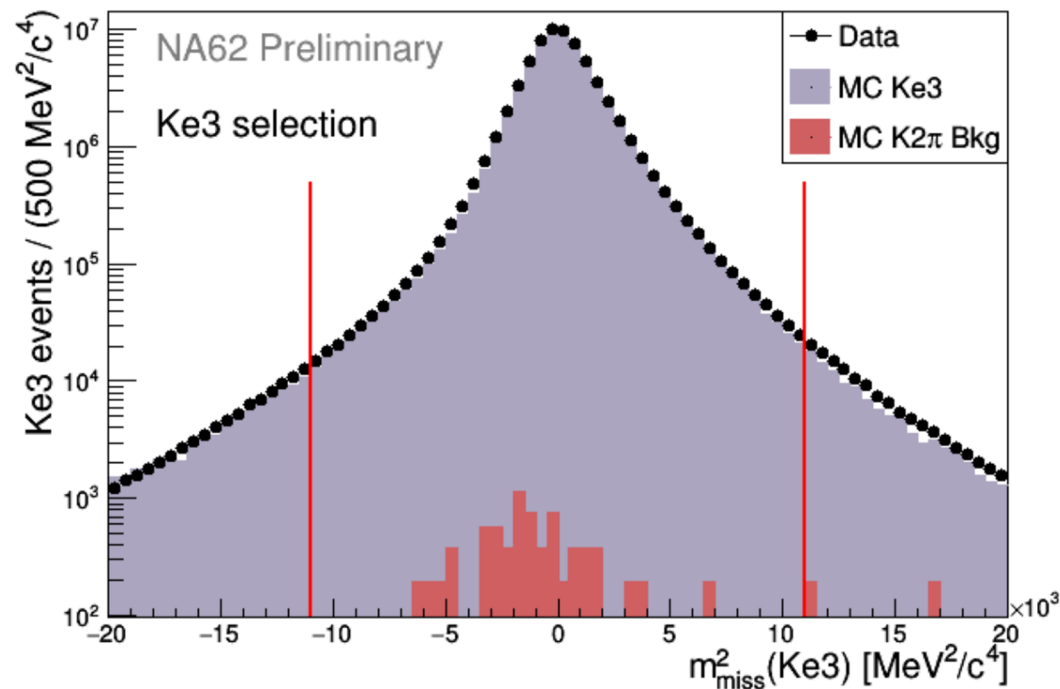
- Expect $|A_\xi| < 10^{-4}$ in SM and beyond; non-zero due to NLO electromagnetic corrections
- Existing measurement from ISTRA+

$$A_\xi^{ISTRA+}(R3) = 0.015 \pm 0.021$$

- No measurement in regions 1 or 2

Event selection

- Branching fraction measurements normalised to $K^+ \rightarrow \pi^0 e^+ \nu$
- Event selection based on K^+ associated to e^+ , $\pi^0 \rightarrow \gamma\gamma$ reconstructed in LKr
- Radiative γ must be in-time with the event and isolated; other activity not allowed to suppress $K^+ \rightarrow \pi^0 \pi^0 e^+ \nu$; cuts to remove γ from bremsstrahlung and suppress $K^+ \rightarrow \pi^+ \pi^0 \pi^0$ and $K^+ \rightarrow \pi^+ \pi^0$
- Obtain 66M normalisation events and 130k signal events (R1) with 0.5% background contamination

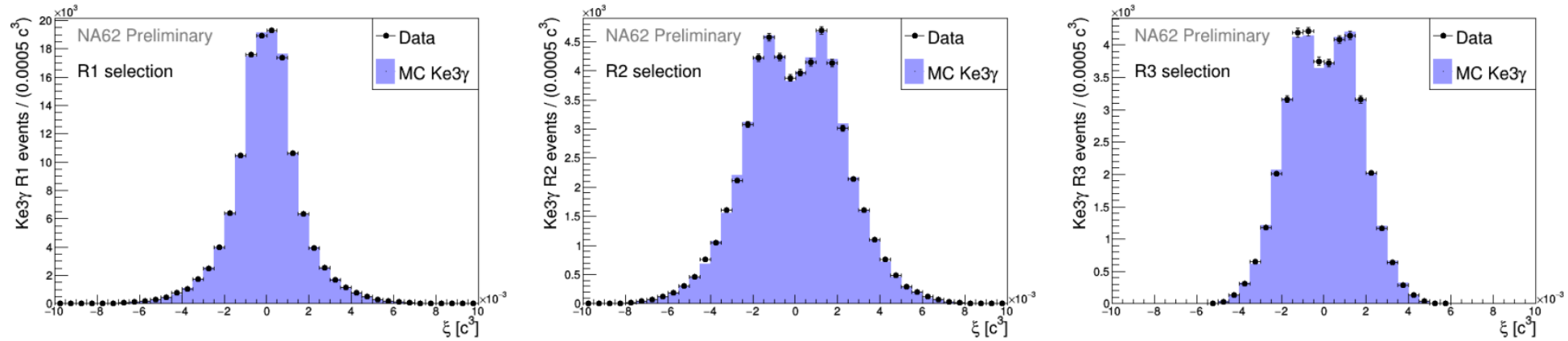


Results and systematics

	$O(p^6)$ ChPT	ISTRA+	OKA	NA62 preliminary
$R_1 (\times 10^2)$	1.804 ± 0.021	$1.81 \pm 0.03 \pm 0.07$	$1.990 \pm 0.017 \pm 0.021$	$1.684 \pm 0.005 \pm 0.010$
$R_2 (\times 10^2)$	0.640 ± 0.008	$0.63 \pm 0.02 \pm 0.03$	$0.587 \pm 0.010 \pm 0.015$	$0.599 \pm 0.003 \pm 0.005$
$R_3 (\times 10^2)$	0.559 ± 0.006	$0.47 \pm 0.02 \pm 0.03$	$0.532 \pm 0.010 \pm 0.012$	$0.523 \pm 0.003 \pm 0.003$

Uncertainty source	$\delta R_1 / R_1$	$\delta R_2 / R_2$	$\delta R_3 / R_3$
Statistical	0.3%	0.5%	0.6%
Acceptances from MC	0.2%	0.4%	0.4%
Background estimation	0.1%	0.2%	0.1%
LKr response modeling	0.5%	0.6%	0.5%
Theoretical model	0.1%	0.5%	0.1%
Total systematic	0.6%	0.9%	0.6%
Total stat+syst	0.7%	1.0%	0.8%

Measurements of A_ξ



	R_1 selection	R_2 selection	R_3 selection
$A_\xi^{Data} (\times 10^2)$	0.2 ± 0.3	0.1 ± 0.4	-0.6 ± 0.5
$A_\xi^{MCgene} (\times 10^2)$	-0.01 ± 0.01	0.00 ± 0.02	-0.01 ± 0.02
$A_\xi^{MCreco} (\times 10^2)$	0.3 ± 0.2	0.4 ± 0.3	0.3 ± 0.5
$A_\xi (\times 10^2)$	$-0.1 \pm 0.3_{stat} \pm 0.2_{MC}$	$-0.3 \pm 0.4_{stat} \pm 0.3_{MC}$	$-0.9 \pm 0.5_{stat} \pm 0.4_{MC}$

- First ever measurements of R_1 and R_2 T-asymmetry
- R_3 T-asymmetry precision improved by a factor greater than 3

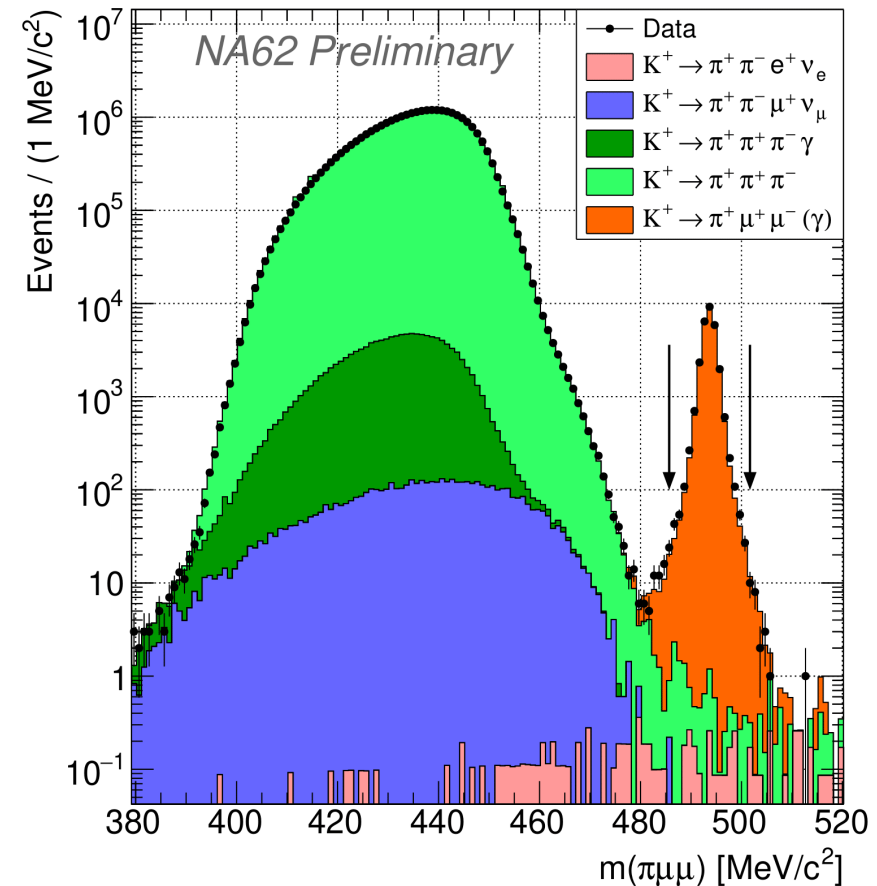
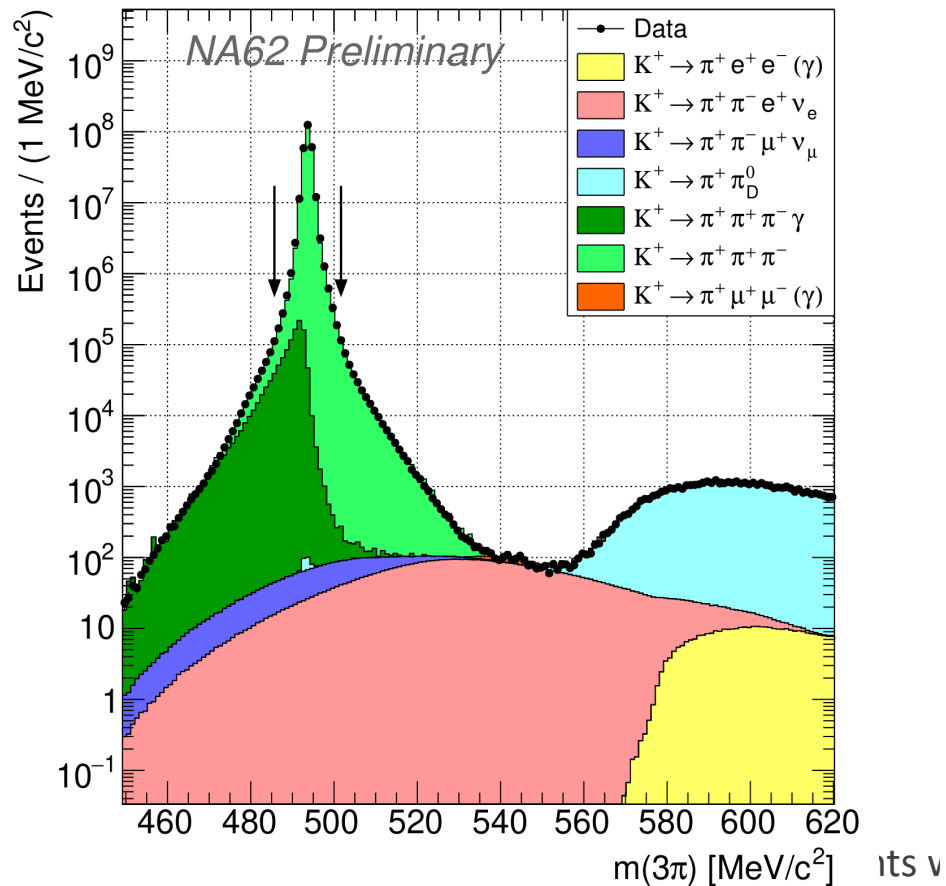
Measurement of $K^+ \rightarrow \pi^+ \mu^+ \mu^-$

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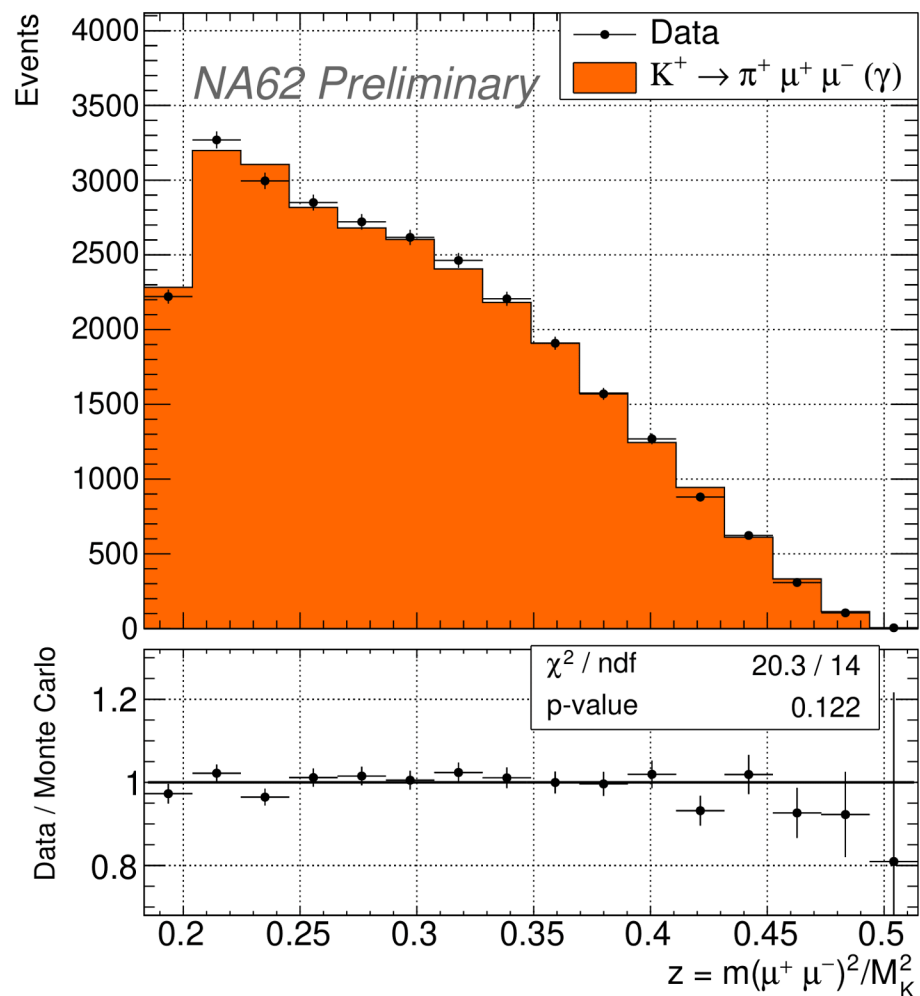
- The $K^+ \rightarrow \pi^+ \ell^+ \ell^-$ decay is a *Flavour Changing Neutral Current* $s \rightarrow d \ell \ell$ process
- The SM branching fraction is $O(10^{-7})$; dominated by long-distance effects
[Nucl. Phys. B291 (1987) 692–719], [JHEP 08 (1998) 004], [Phys. Part. Nucl. Lett. 5 (2008) 76–84], [Eur. Phys. J. C70 (2010) 219–231]
- The form factor is parameterised by two coefficients: a_+ and b_+
- Short distance physics can be extracted by comparing a_+ and b_+ between $\pi^+ \mu^+ \mu^-$ and $\pi^+ e^+ e^-$ as the SM predicts them to be identical: a probe of *Lepton Flavour Universality*
- The a_+ parameter can be related to B anomalies (assuming MFV) [Phys. Rev. D 93, 074038 (2016)]
- Largest uncertainty on a_+ is in the dimuon mode

Event selection

- Normalised to $K^+ \rightarrow \pi^+ \pi^+ \pi^-$. Events selected by reconstructing three-track vertices, and looking for associated K^+ and muon signatures. Kinematic cuts to further suppress $K^+ \rightarrow \pi^+ \pi^+ \pi^-$ backgrounds
- 2.78×10^8 normalisation events, **28011** signal events (9x larger than earlier measurement)



Fit to the form-factor parameters



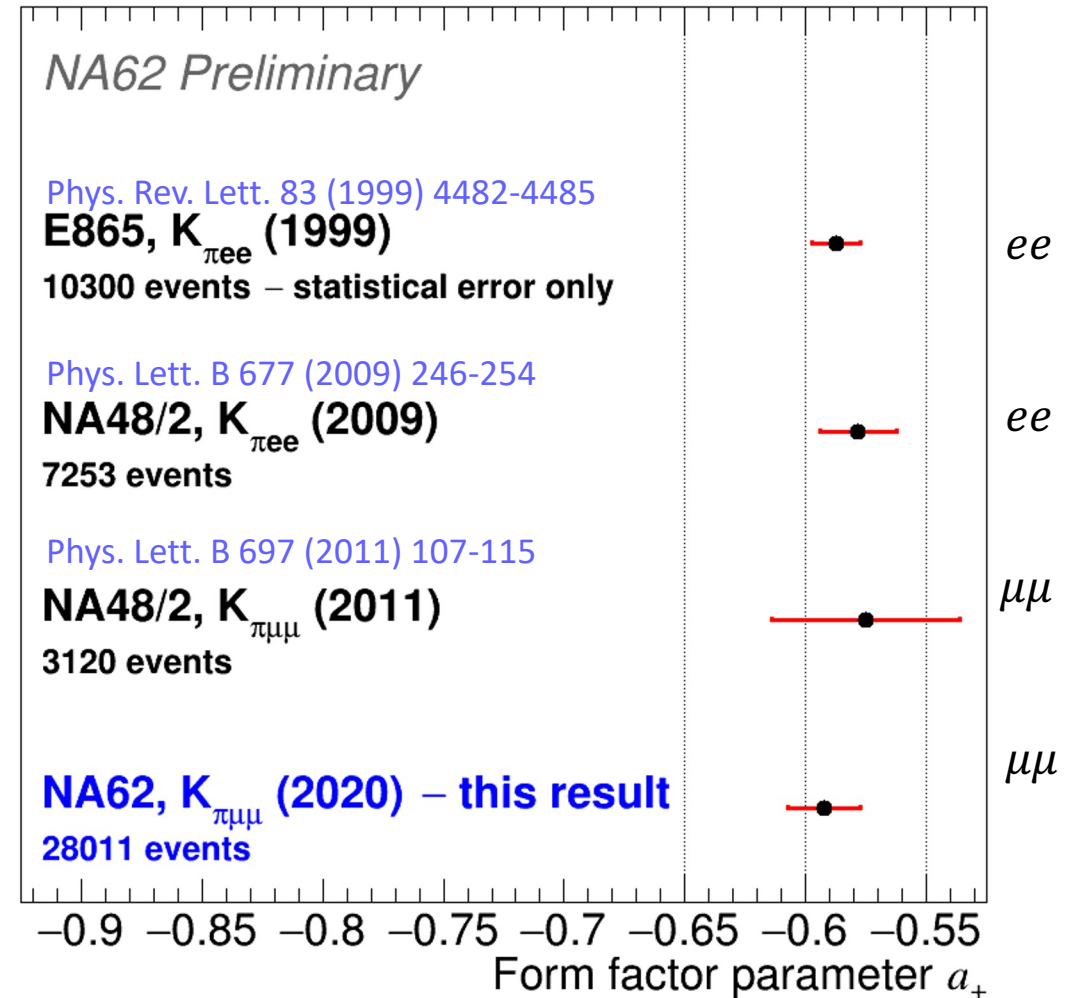
Fitting procedure:

- z spectrum of simulated $K^+ \rightarrow \pi^+ \mu^+ \mu^-$ events reweighted to best fit the data by minimising $\chi^2(a, b)$

	a	b	$\mathcal{B}_{\pi\mu\mu} \times 10^8$
Best fit	-0.592	-0.699	9.27
<i>Errors</i>			
	δa	δb	$\delta \mathcal{B}_{\pi\mu\mu} \times 10^8$
Statistical	0.013	0.046	0.07
Systematic			
Reconstruction efficiency	0.005	0.026	0.06
Beam & pileup simulation	0.005	0.024	0.05
Trigger efficiency	0.001	0.005	0.04
Background	0.000	0.001	0.01
<i>Total systematic</i>	0.007	0.035	0.08
External			
PDG error on $\mathcal{B}(K_{3\pi})$	0.001	0.003	0.04
Total	0.015	0.058	0.11

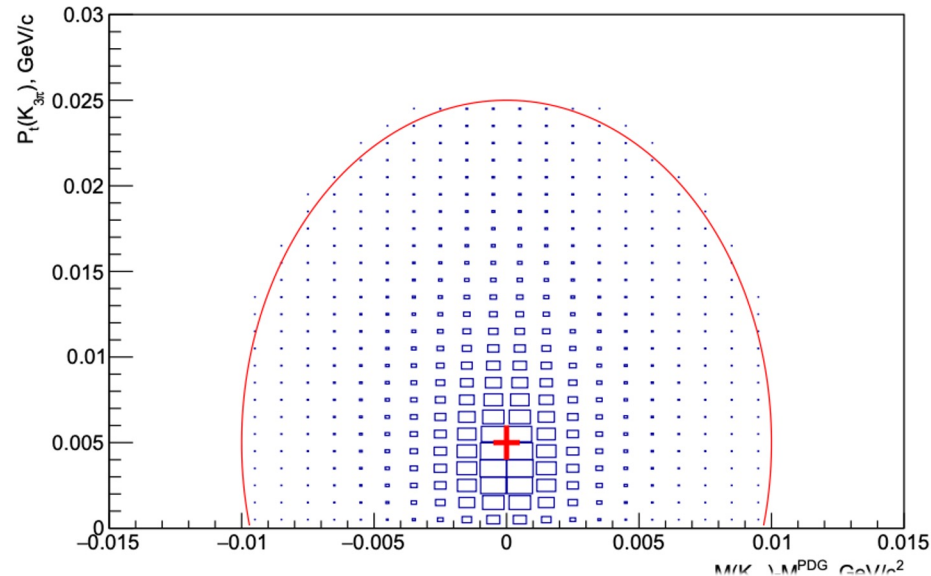
Comparison with existing measurements

- The NA62 measurement of $a_+^{\mu\mu}$ is the worlds most precise determination
- The result is consistent with the earlier NA48/2 measurement, and is consistent with existing measurements of a_+^{ee}
- No indication of discrepancy with SM predictions, including LFU violation



1. First observation and BR measurement of $K^\pm \rightarrow \pi^0 \pi^0 \mu^\pm \nu$ by NA48/2 [PRELIMINARY]
 - Restricted phase-space:
$$BR(S_\ell > 0.03) = (0.65 \pm 0.019_{stat} \pm 0.024_{syst}) \times 10^{-6} = (0.65 \pm 0.03) \times 10^{-6}$$
 - Full phase-space result:
$$BR = (3.4 \pm 0.10_{stat} \pm 0.13_{syst}) \times 10^{-6} = (3.4 \pm 0.2) \times 10^{-6}$$
 - Consistent with contribution from R form-factor, as expected from ChPT.
2. New study of $K^+ \rightarrow \pi^0 e^+ \nu \gamma$ by NA62 [PRELIMINARY]
 - Precision of R_j measurements improved by factors between 2.0 and 3.6
 - First T-asymmetry measurements in R_1 and R_2 , improved result on R_3 by factor 3
 - T-asymmetry results compatible with zero
3. Measurement of $K^+ \rightarrow \pi^+ \mu^+ \mu^-$ by NA62 [PRELIMINARY]
 - Most precise measurements of a_+ and b_+ parameters and branching ratio
 - No hints of lepton non-universality

- Signal $K_{\mu 4}$ is $K^\pm \rightarrow \pi^0 \pi^0 \mu^\pm \nu$
- Normalization $K_{3\pi}$ is $K^\pm \rightarrow \pi^\pm \pi^0 \pi^0$
- Trigger chain: L1 trigger using HOD and LKr, followed by L2 trigger using DCH for online momentum calculation.
- Event selection: 4 isolated photons consistent with $2\pi^0$ in time-spatial matching with a KABES beam track and a DCH track.



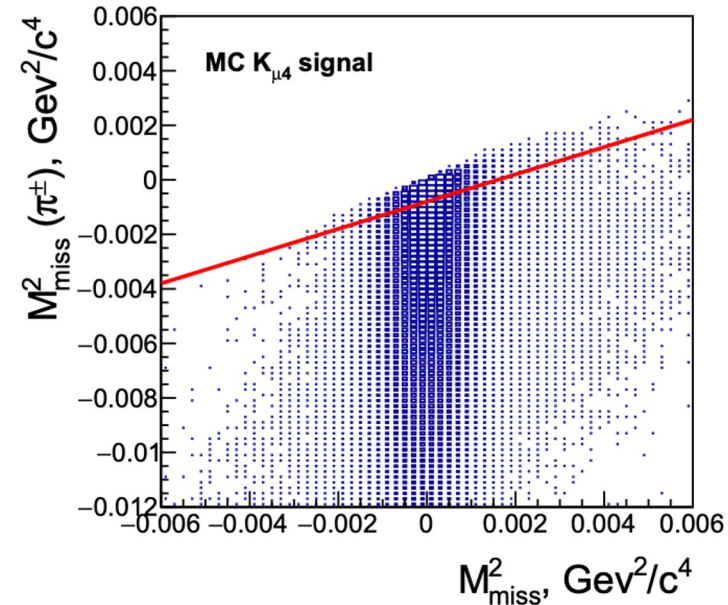
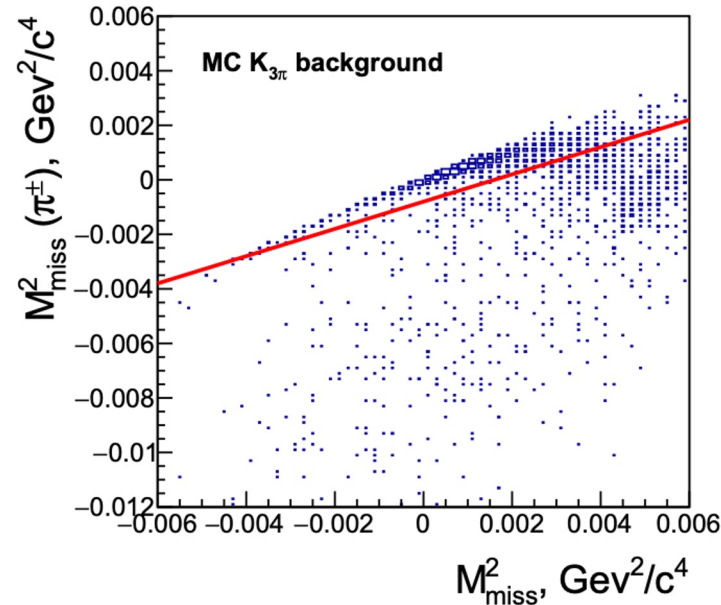
Normalization $K_{3\pi}$ kinematic selection ellipse:

- center:
 - $M(K_{3\pi}) = M_K^{PDG}$
 - $P_t = 5 \text{ MeV}/c$
- semi-axes:
 - $\Delta M(K_{3\pi}) = 10 \text{ MeV}/c^2$
 - $\Delta P_t = 20 \text{ MeV}/c$
- 72.99×10^6 $K_{3\pi}$ selected data events.

- Off the $K_{3\pi}$ kinematic ellipse
- DCH track has associated MUV response

$$M_{miss}^2 = (P_K - P(\pi_1^0) - P(\pi_2^0) - P(\mu^\pm))^2$$

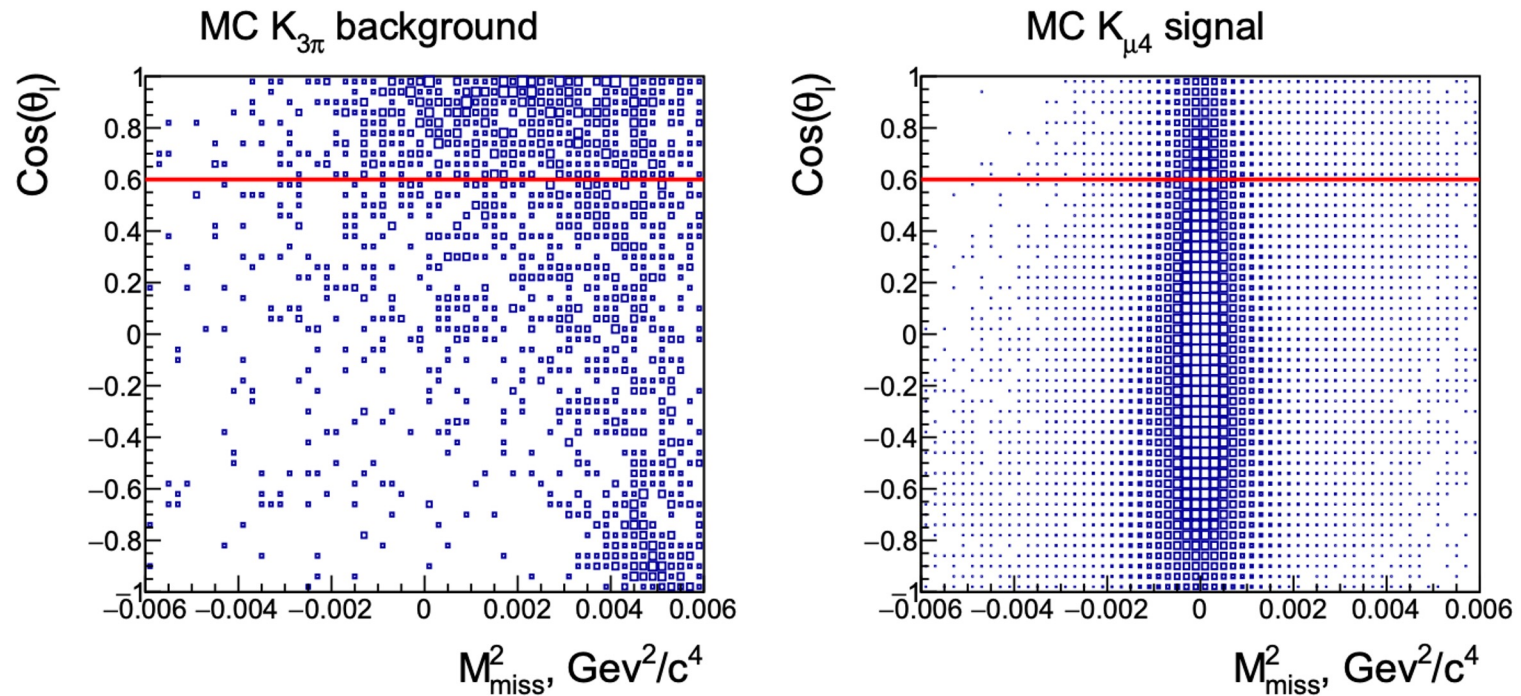
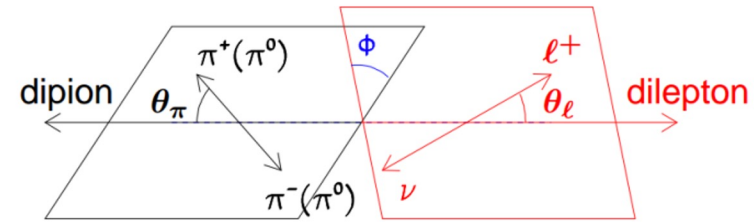
$$M_{miss}^2(\pi^\pm) = (P_K - P(\pi_1^0) - P(\pi_2^0) - P(\pi^\pm))^2$$

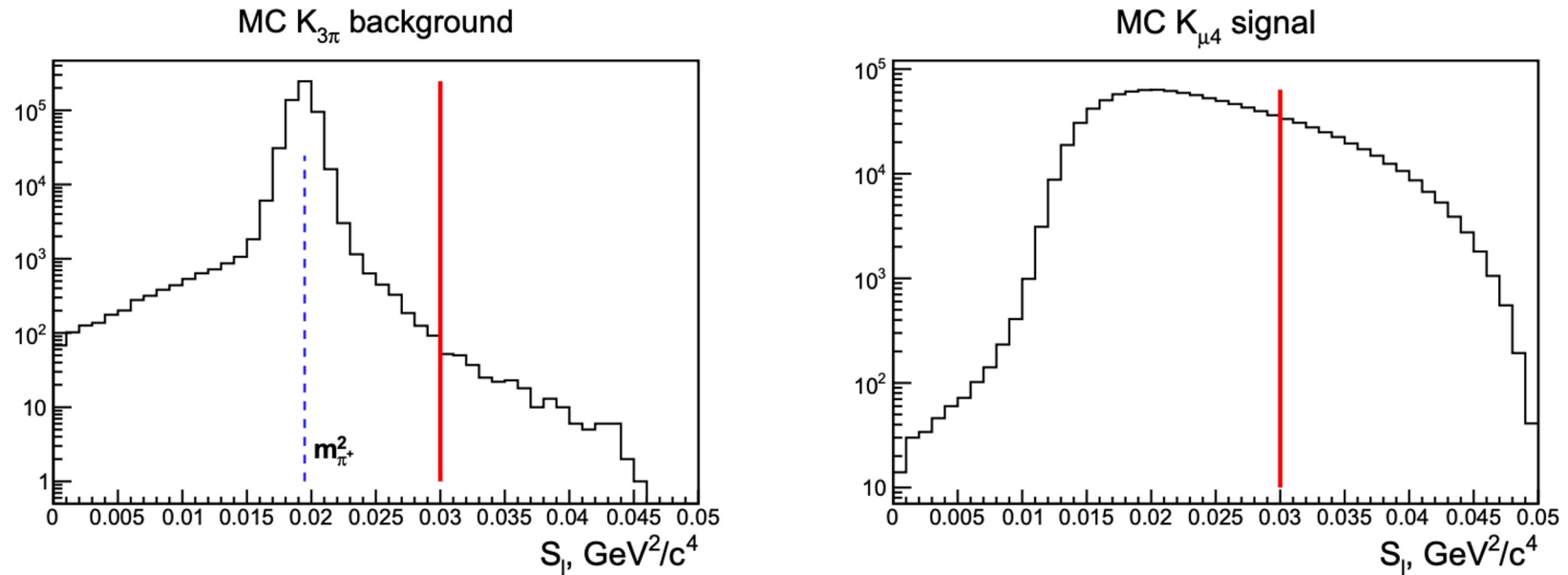


- $M_{miss}^2(\pi^\pm) < 0.5M_{miss}^2 - 0.0008 \text{ GeV}^2/c^4$



- $\cos(\Theta_l) < 0.6$





- $S_l = m(\mu\nu)^2 > 0.03 \text{ GeV}^2/c^4$ (to reject $\pi^\pm \rightarrow \mu^\pm\nu$).
- 3718 $K_{\mu 4}$ data candidates selected
- 2437 data candidates in M_{miss}^2 signal region $[-0.002, 0.002] \text{ GeV}^2/c^4$
- The MC M_{miss}^2 signal region contains 98.2% of all selected MC events

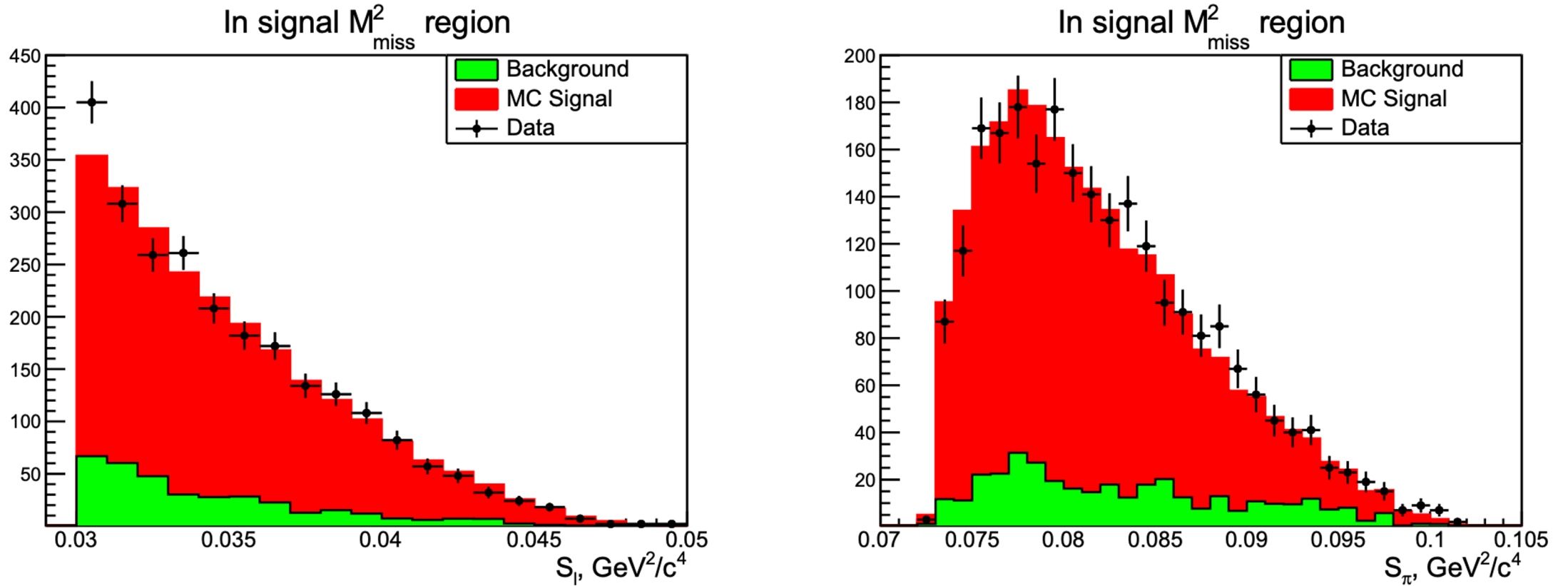


Figure: 1D projections comparison for $S_I > 0.03 \text{ GeV}^2/c^4$

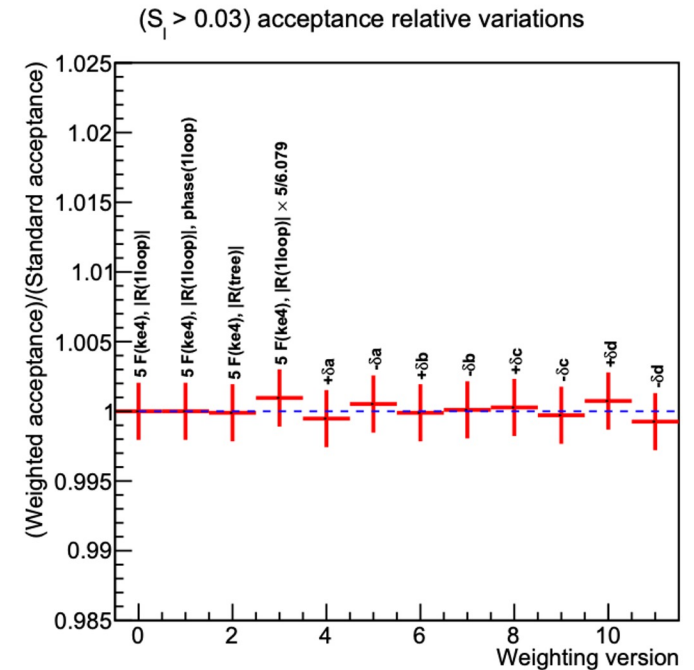
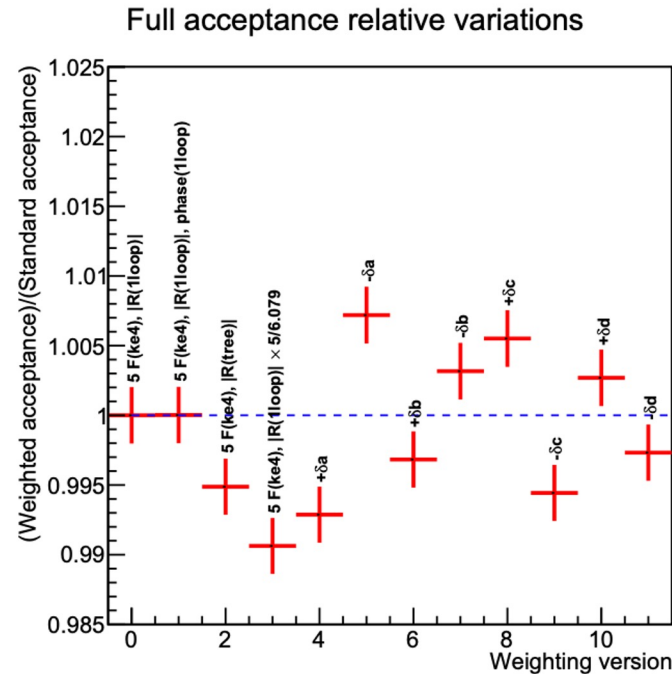
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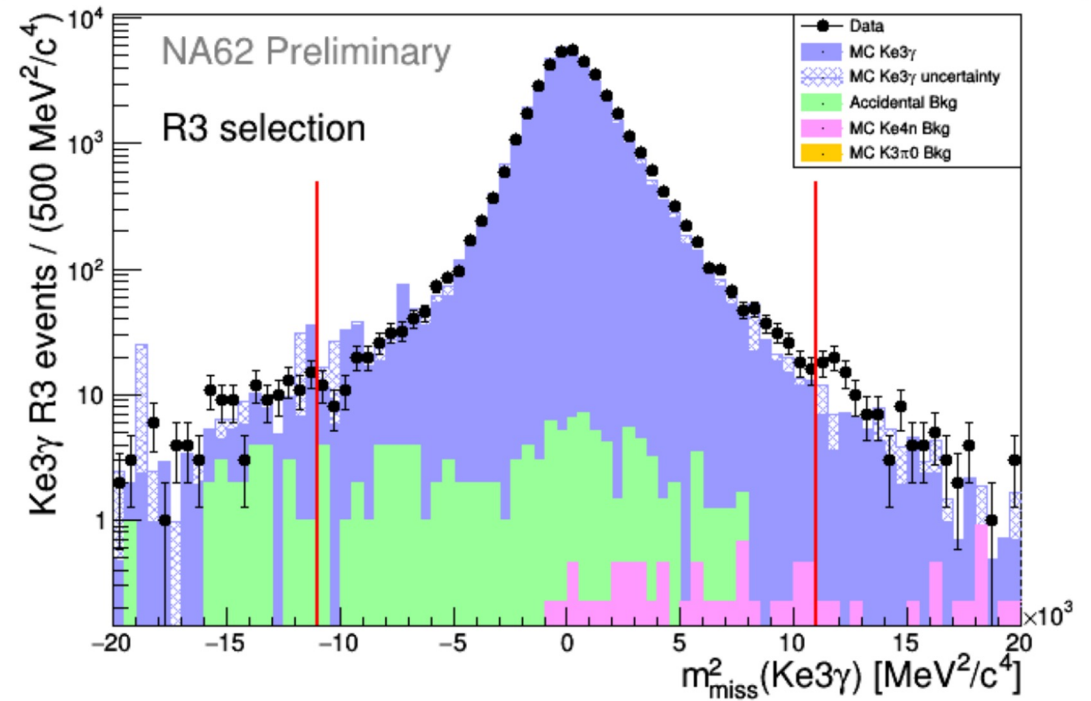
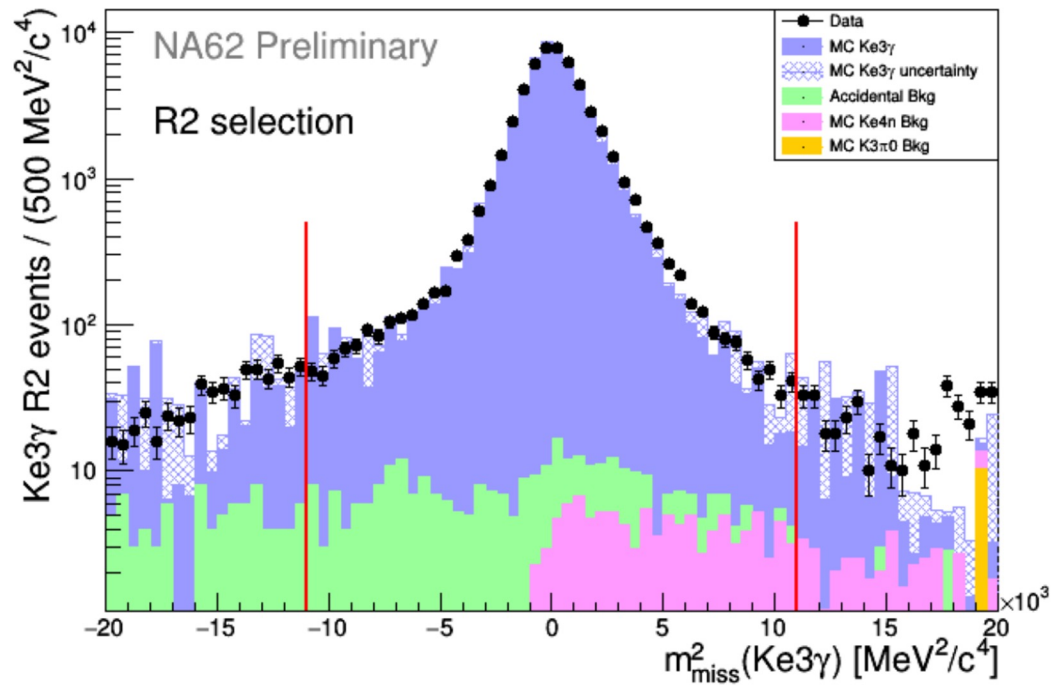
The absolute normalization is also measured $F = f \times F(K_{e4})$,
 $f = 6.079 \pm 0.055$.

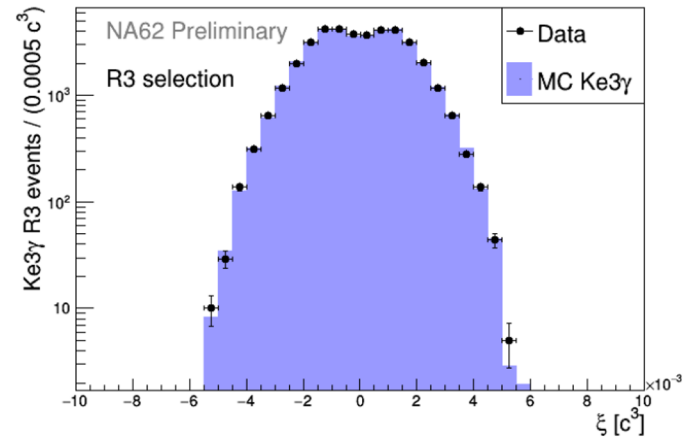
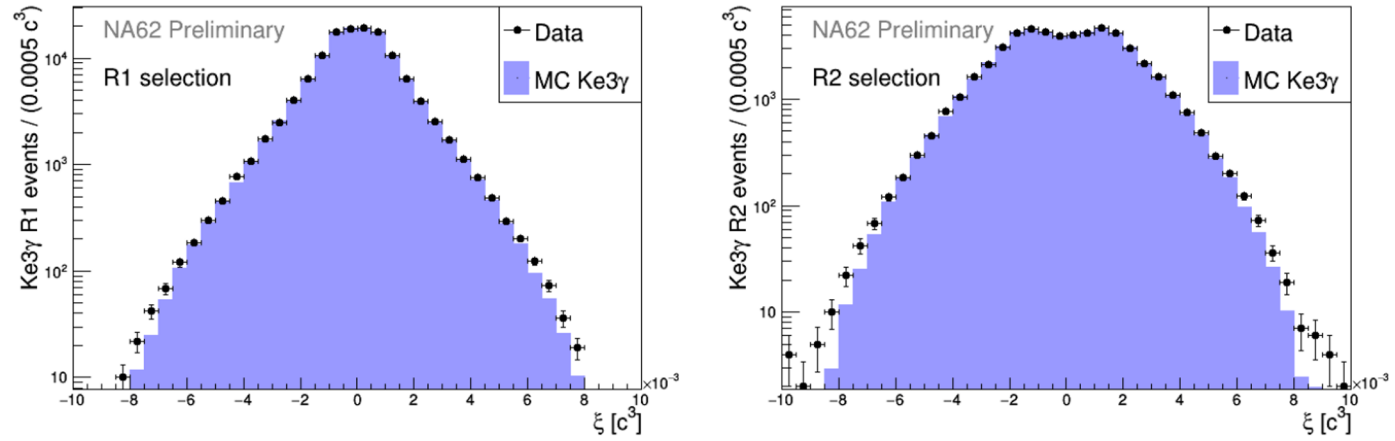
$$F(K_{e4}) = \begin{cases} (1 + aq^2 + bq^4 + c \cdot S_1/4m_{\pi^+}^2) & \text{for } q^2 \geq 0 \\ (1 + d\sqrt{|q^2/(1+q^2)|} + c \cdot S_1/4m_{\pi^+}^2) & \text{for } q^2 < 0 \end{cases}$$

where $q^2 = S_{\pi}/4m_{\pi^+}^2 - 1$.

- Decay generator was modified by MC events weighting.
- The acceptance spread is taken as systematics.







	a	b	$\mathcal{B}_{\pi\mu\mu} \times 10^8$
Best fit	-0.592	-0.699	9.27
<i>Errors</i>	δa	δb	$\delta \mathcal{B}_{\pi\mu\mu} \times 10^8$
Statistical	0.013	0.046	0.07
Systematic			
Reconstruction efficiency	0.005	0.026	0.06
Beam & pileup simulation	0.005	0.024	0.05
Trigger efficiency	0.001	0.005	0.04
Background	0.000	0.001	0.01
<i>Total systematic</i>	0.007	0.035	0.08
External			
PDG error on $\mathcal{B}(K_{3\pi})$	0.001	0.003	0.04
Total	0.015	0.058	0.11

Note: a_+ measurement limited by statistical uncertainty

