

# $J/\psi$ PHOTOPRODUCTION IN SEMI-PERIPHERAL HEAVY-ION COLLISIONS

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The poster for the BEACH 2022 conference features a dark background with a night view of a large, illuminated Gothic-style building with many arches. A circular inset shows a colorful particle detector event. The text is in white and orange.

**BEACH** XIV INTERNATIONAL CONFERENCE  
ON BEAUTY, CHARM AND  
HYPERON HADRONS  
**2022**  
5-11 June 2022 AGH-UST Kraków, Poland

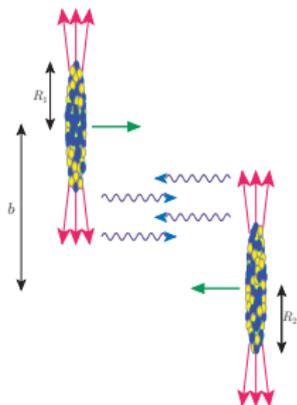
# 1 EQUIVALENT PHOTON

## APPROXIMATION

# 2 ULTRAPERIPHERAL COLLISION

# 3 SEMICENTRAL COLLISION

# 4 CONCLUSION



The strong electromagnetic field is a source of photons that can induce electromagnetic reactions in ion-ion collisions.

Electromagnetism is a long-range force, so electromagnetic interactions occur even at relatively large ion-ion separations.

$$\text{Photon energy: } \omega = \frac{\gamma}{b} \approx \gamma \times 15 \text{ MeV}$$

$$\text{Virtuality: } Q^2 = \frac{1}{R^2} \approx 0.0008 \text{ GeV}^2$$

Centrality (for  $^{208}\text{Pb}$ ):

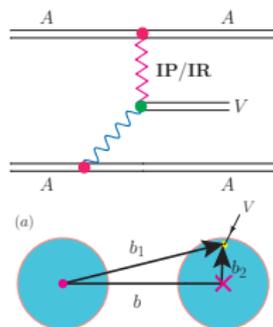
- central collisions:  $b \approx (0 \text{ fm} + \Delta b)$ ;
- semi-central collisions:  $b \approx (5 - 10) \text{ fm}$ ;
- semi-peripheral collisions:  $b \approx (10 - 12) \text{ fm}$ ;
- peripheral collisions:  $b \approx (12 \text{ fm} - (R_1 + R_2))$ ;
- **ultraperipheral** collisions:  $b > (R_1 + R_2)$ ;

where  $R = R_0 A^{1/3}$ .

① M. Klusek-Gawenda, A. Szczurek, M. V. T. Machado, V. G. Serbo, *Double-photon exclusive processes with heavy-quark-heavy-antiquark pairs in high-energy Pb-Pb collisions at energies available at the CERN Large Hadron Collider*, Phys. Rev. **C83** (2011) 024903;

② M. Klusek-Gawenda, A. Szczurek, *Photoproduction of  $J/\psi$  mesons in peripheral and semicentral heavy ion collisions*, Phys. Rev. **C93** (2016) 044912.

## EQUIVALENT PHOTON APPROXIMATION - UPC



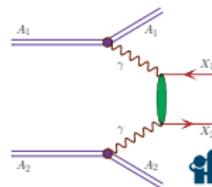
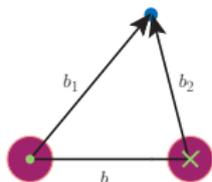
## Photoproduction

$$\frac{d\sigma_{A_1 A_2 \rightarrow A_1 A_2 V}}{d^2 b dy} = \frac{dP_{\gamma \mathbf{P}/\mathbf{R}}(y, b)}{dy} + \frac{dP_{\mathbf{P}/\mathbf{R} \gamma}(y, b)}{dy}$$

$$\frac{dP_{\gamma \mathbf{P}/\mathbf{R} \gamma}(y, b)}{dy} = \omega_{1/2} N(\omega_{1/2}, b) \sigma_{\gamma A_{2/1} \rightarrow V A_{2/1}}(W_{\gamma A_{2/1}}) S_{abs}(b)$$

 $\gamma\gamma$  fusion

$$\begin{aligned} \sigma_{A_1 A_2 \rightarrow A_1 A_2 X_1 X_2} &= \int \sigma_{\gamma\gamma \rightarrow X_1 X_2}(W_{\gamma\gamma}) N(\omega_1, \mathbf{b}_1) N(\omega_2, \mathbf{b}_2) S_{abs}^2(\mathbf{b}) \frac{W_{\gamma\gamma}}{2} dW_{\gamma\gamma} dY_{X_1 X_2} d\bar{b}_x d\bar{b}_y d^2 b \\ &= \int \frac{d\sigma_{\gamma\gamma \rightarrow X_1 X_2}(W_{\gamma\gamma})}{d \cos \theta} N(\omega_1, \mathbf{b}_1) N(\omega_2, \mathbf{b}_2) S_{abs}^2(\mathbf{b}) \frac{W_{\gamma\gamma}}{2} dW_{\gamma\gamma} dY_{X_1 X_2} d\bar{b}_x d\bar{b}_y d^2 b \\ &\times \frac{d \cos \theta}{dy_{X_1} dy_{X_2} dp_t} \times dy_{X_1} dy_{X_2} dp_t. \end{aligned}$$



## EQUIVALENT PHOTON FLUX VS. FORM FACTOR

$$N(\omega, b) = \frac{Z^2 \alpha_{em}}{\pi^2 \beta^2} \frac{1}{\omega} \frac{1}{b^2} \times \left| \int dx \chi^2 \frac{F\left(\frac{\chi^2 + u^2}{b^2}\right)}{\chi^2 + u^2} J_1(\chi) \right|^2$$

$$\beta = \frac{p}{E}, \gamma = \frac{1}{\sqrt{1-\beta^2}}, u = \frac{\omega b}{\gamma \beta}, \chi = k_{\perp} b$$

- point-like  $F(\mathbf{q}^2) = 1$

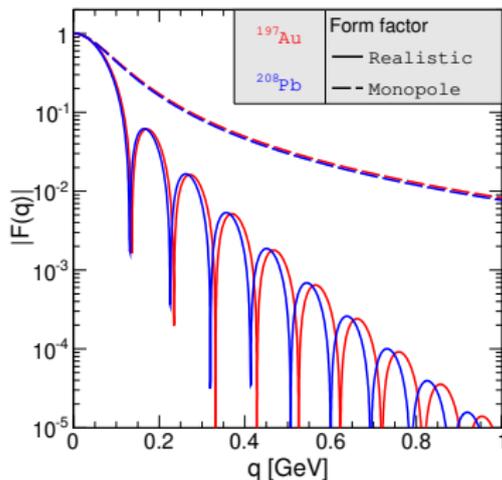
$$N(\omega, b) = \frac{Z^2 \alpha_{em}}{\pi^2 \beta^2} \frac{1}{\omega} \frac{1}{b^2} \times u^2 \left[ K_1^2(u) + \frac{1}{\gamma^2} K_0^2(u) \right]$$

- monopole  $F(\mathbf{q}^2) = \frac{\Lambda^2}{\Lambda^2 + |\mathbf{q}|^2}$

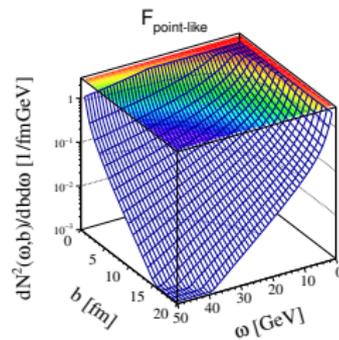
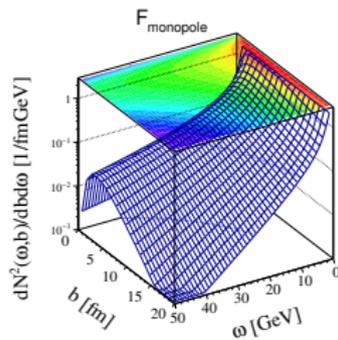
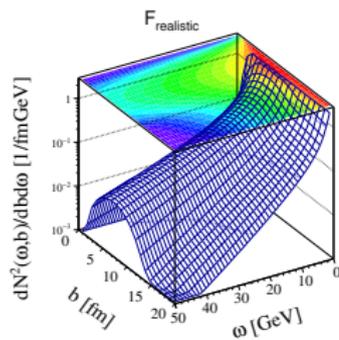
$$\sqrt{\langle r^2 \rangle} = \sqrt{\frac{6}{\Lambda^2}} = 1 \text{ fm } A^{1/3}$$

- realistic

$$F(\mathbf{q}^2) = \frac{4\pi}{|\mathbf{q}|} \int \rho(r) \sin(|\mathbf{q}| r) r dr$$



## PHOTON FLUX



Standard photon fluxes.

# $J/\psi$ - UPC

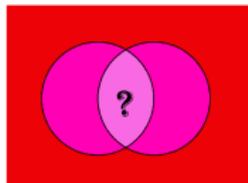
$$\begin{aligned}\sigma_{\gamma A \rightarrow J/\psi A} &= \frac{d\sigma_{\gamma A \rightarrow J/\psi A}(t=0)}{dt} \int_{-\infty}^{t_{\max}} dt |F_A(t)|^2 \\ &= \frac{\alpha_{em}}{4f_{J/\psi}^2} \sigma_{tot, J/\psi A}^2 \int_{-\infty}^{t_{\max}} dt |F_A(t)|^2\end{aligned}$$

$$t = -q^2 = -(m_{J/\psi}^2 / (2\omega_{lab}))^2$$

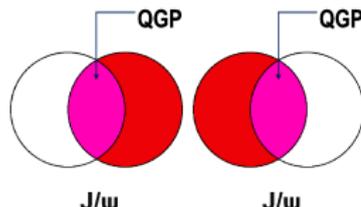
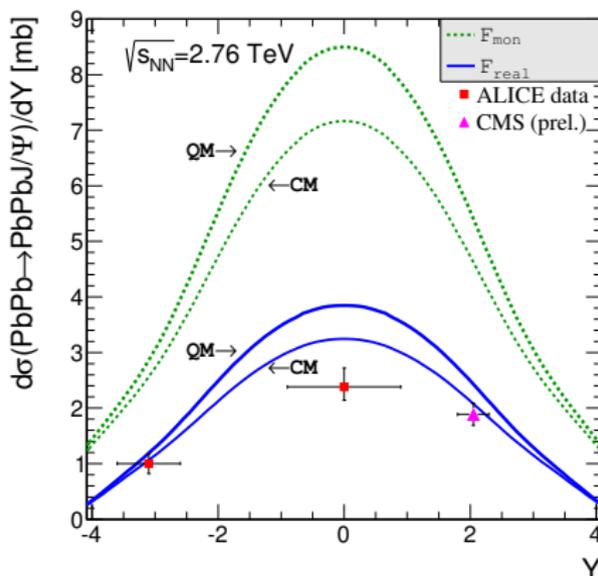
$$\sigma_{tot}^{QM}(J/\psi A) = 2 \int d^2r \left( 1 - \exp\left(-\frac{1}{2} \sigma_{tot}(J/\psi p) T_A(r)\right) \right)$$

$$\sigma_{tot}^{CM}(J/\psi A) = \int d^2r (1 - \exp(-\sigma_{tot}(J/\psi p) T_A(r)))$$

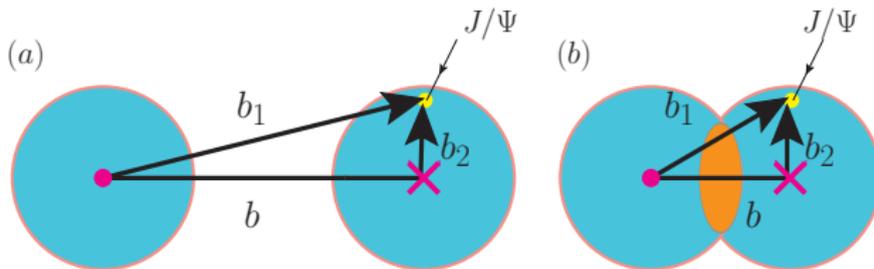
UPC  $\rightarrow$  semi-central collision



$e^+e^-, \mu^+\mu^-$



## CHARMONIUM PHOTOPRODUCTION

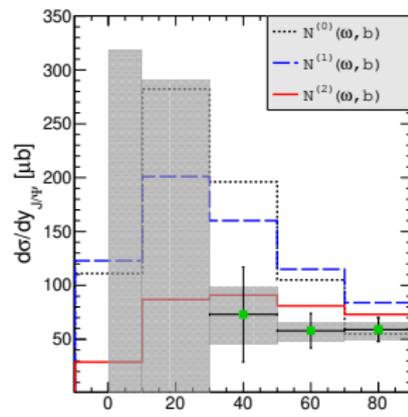


The inclusion of the absorption effect by modifying effective photon fluxes in the impact parameter space.

$$N^{(1)}(\omega_1, b) = \int N(\omega_1, b_1) \frac{\theta(R_A - (|\mathbf{b}_1 - \mathbf{b}|))}{\pi R_A^2} d^2 b_1$$

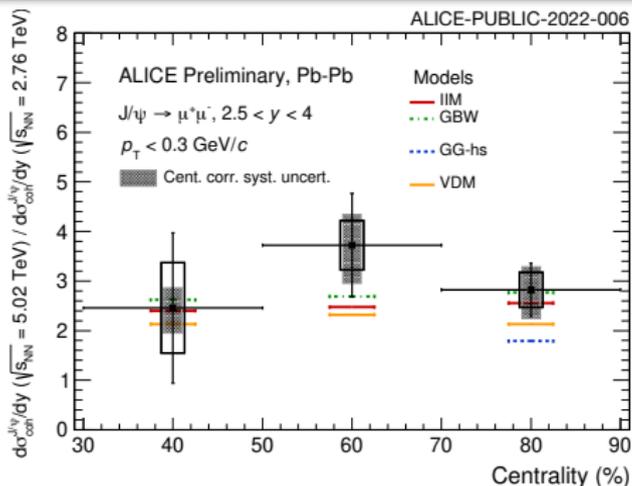
$$N^{(2)}(\omega_1, b) = \int N(\omega_1, b_1) \frac{\theta(R_A - (|\mathbf{b}_1 - \mathbf{b}|))(b_1 - R_A)}{\pi R_A^2} d^2 b_1$$

A successful description of ALICE data,  $\sqrt{s_{NN}} = 2.76$  TeV



Coherent  $J/\psi$  cross section at forward rapidity

NEW



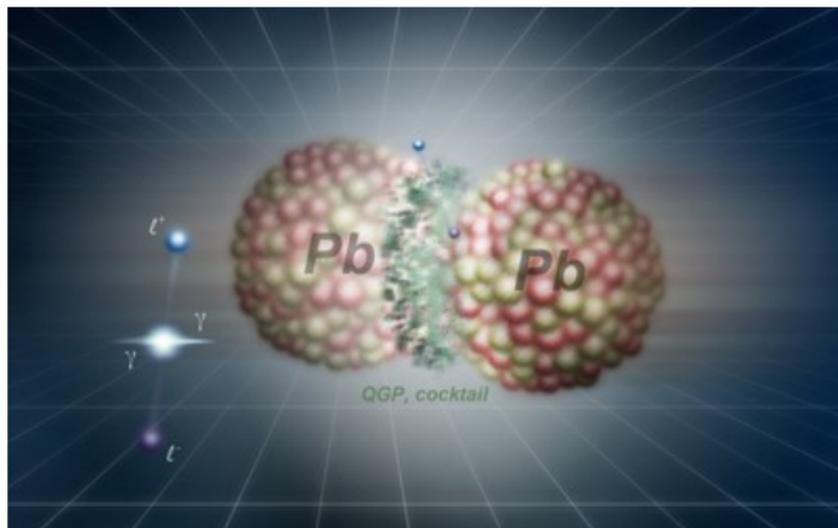
ALI-PREL-512349

- Ratio of the measurements at  $\sqrt{s_{NN}} = 5.02$  TeV and  $\sqrt{s_{NN}} = 2.76$  TeV shows no centrality dependence within uncertainties
- Fair agreement of the measured ratio to models ( except GG-hs ) within uncertainties

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19

## DILEPTON PRODUCTION



- From ultraperipheral to semicentral collisions → dilepton sources
  - $\gamma\gamma$  fusion mechanism

## DIELECTRON INVARIANT-MASS SPECTRA - RHIC

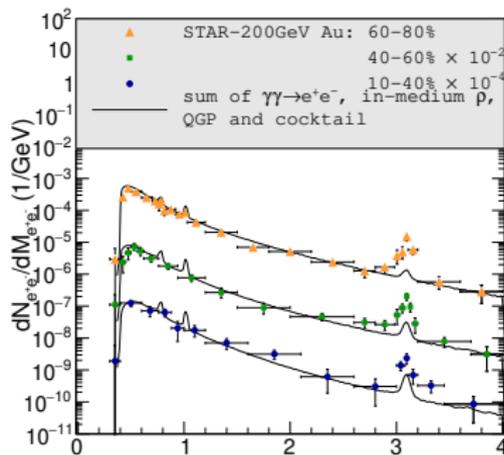
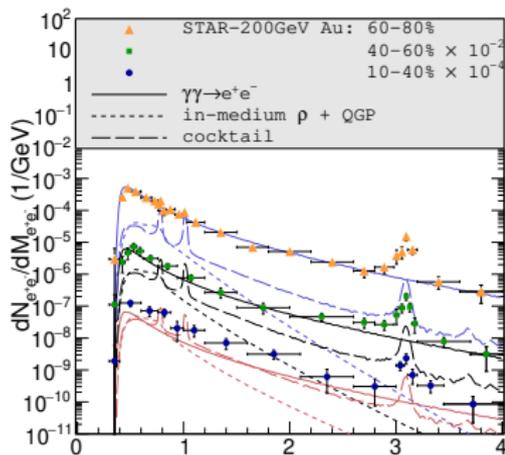
$$p_t > 0.2 \text{ GeV},$$

$$|\eta_e| < 1$$

$$|y_{e^+e^-}| < 1$$

- ✓  $\gamma\gamma$ -fusion
- ✓ thermal radiation
- ✓ hadronic cocktail

3 centrality classes



The coherent emission dominates for the two peripheral samples

and is comparable to the cocktail and thermal radiation yields in semi-central collisions.

## EPA in the impact parameter space - the pair transverse momentum $P_T^{\ell^+ \ell^-}$ is neglected

$$\sigma_{A_1 A_2 \rightarrow A_1 A_2 \ell^+ \ell^-} = \int N(\omega_1, \mathbf{b}_1) N(\omega_2, \mathbf{b}_2) \delta^{(2)}(\mathbf{b} - \mathbf{b}_1 - \mathbf{b}_2) \int d^2 \mathbf{b}_1 d^2 \mathbf{b}_2 d^2 \mathbf{b} dy_{\ell^+} dy_{\ell^-} d\rho_{T, \ell}^2 \frac{d\sigma(\gamma\gamma \rightarrow \ell^+ \ell^-; \hat{s})}{d(-\hat{t})}$$

⇒  $k_t$ -factorization

$$\frac{dN_{\parallel}}{d^2 \mathbf{P}_T^{\ell^+ \ell^-}} = \int \frac{d\omega_1}{\omega_1} \frac{d\omega_2}{\omega_2} d^2 \mathbf{q}_{1t} d^2 \mathbf{q}_{2t} \frac{dN(\omega_1, \mathbf{q}_{1t}^2)}{d^2 \mathbf{q}_{1t}} \frac{dN(\omega_2, \mathbf{q}_{2t}^2)}{d^2 \mathbf{q}_{2t}} \delta^{(2)}(\mathbf{q}_{1t} + \mathbf{q}_{2t} - \mathbf{P}_T^{\ell^+ \ell^-}) \hat{\sigma}(\gamma\gamma \rightarrow \ell^+ \ell^-) \Big|_{\text{cuts}},$$

⇒ Exact calculation

$$\begin{aligned} \frac{d\sigma[C]}{d^2 \mathbf{P}_T^{\ell^+ \ell^-}} &= \int \frac{d^2 \mathbf{Q}}{2\pi} w(\mathbf{Q}; b_{\max}, b_{\min}) \int \frac{d^2 \mathbf{q}_1}{\pi} \frac{d^2 \mathbf{q}_2}{\pi} \delta^{(2)}(\mathbf{P}_T^{\ell^+ \ell^-} - \mathbf{q}_1 - \mathbf{q}_2) \int \frac{d\omega_1}{\omega_1} \frac{d\omega_2}{\omega_2} \\ &\times E_j\left(\omega_1, \mathbf{q}_1 + \frac{\mathbf{Q}}{2}\right) E_j^*\left(\omega_1, \mathbf{q}_1 - \frac{\mathbf{Q}}{2}\right) E_k\left(\omega_2, \mathbf{q}_2 - \frac{\mathbf{Q}}{2}\right) E_l^*\left(\omega_2, \mathbf{q}_2 + \frac{\mathbf{Q}}{2}\right) \frac{1}{2\hat{s}} \sum_{\lambda \bar{\lambda}} M_{ik}^{\lambda \bar{\lambda}} M_{jl}^{\lambda \bar{\lambda} \dagger} d\Phi(\ell^+ \ell^-). \end{aligned}$$

The factorization formula is written in terms of the **Wigner function**:

$$N_{ij}(\omega, \mathbf{b}, \mathbf{q}) = \int \frac{d^2 \mathbf{Q}}{(2\pi)^2} \exp[-i\mathbf{bQ}] E_i\left(\omega, \mathbf{q} + \frac{\mathbf{Q}}{2}\right) E_j^*\left(\omega, \mathbf{q} - \frac{\mathbf{Q}}{2}\right) = \int d^2 \mathbf{s} \exp[i\mathbf{qs}] E_i\left(\omega, \mathbf{b} + \frac{\mathbf{s}}{2}\right) E_j^*\left(\omega, \mathbf{b} - \frac{\mathbf{s}}{2}\right),$$

$$N(\omega, \mathbf{q}) = \delta_{ij} \int d^2 \mathbf{b} N_{ij}(\omega, \mathbf{b}, \mathbf{q}) = \delta_{ij} E_i(\omega, \mathbf{q}) E_j^*(\omega, \mathbf{q}) = |\mathbf{E}(\omega, \mathbf{q})|^2,$$

$$N(\omega, \mathbf{b}) = \delta_{ij} \int \frac{d^2 \mathbf{q}}{(2\pi)^2} N_{ij}(\omega, \mathbf{b}, \mathbf{q}) = \delta_{ij} E_i(\omega, \mathbf{b}) E_j^*(\omega, \mathbf{b}) = |\mathbf{E}(\omega, \mathbf{b})|^2.$$

## PAIR TRANSVERSE MOMENTUM - RHIC &amp; LHC

$$p_t > 0.2 \text{ GeV,}$$

$$|\eta_e| < 1$$

$$c = (60-80)\%$$

$$|y_{ee}| < 1$$

----- PLB790 (2019) 339

vs.

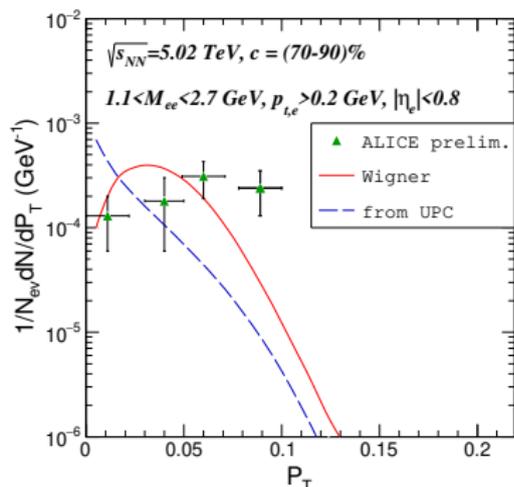
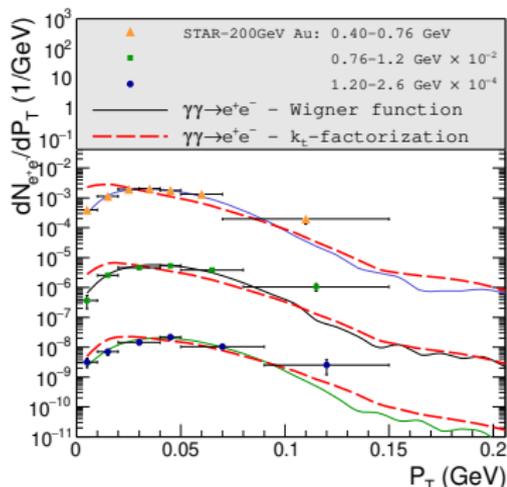
— PLB814 (2021) 136114

$$p_t > 0.2 \text{ GeV,}$$

$$|\eta_e| < 0.8$$

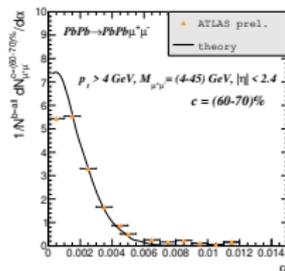
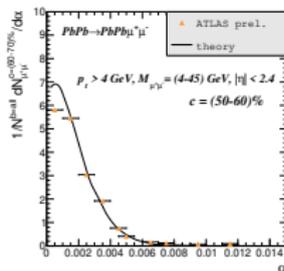
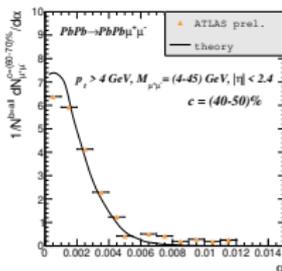
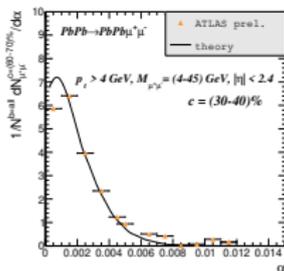
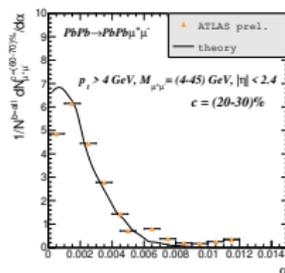
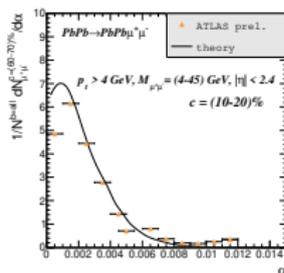
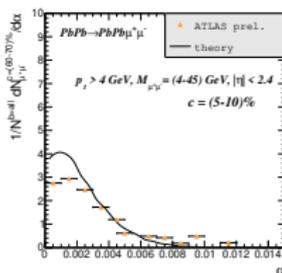
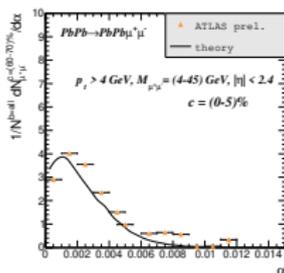
$$c = (70-90)\%$$

$$M_{e^+e^-} = (1.1-2.7) \text{ GeV}$$



Small correction to the STAR description & much better situation for LHC

## ACOPLANARITY - ATLAS DATA



A successful description of ATLAS data by  $\gamma\gamma$ -fusion alone

A correct normalization and shape of the distributions

$$p_t > 4 \text{ GeV},$$

$$M_{\mu^+\mu^-} = (4-45) \text{ GeV},$$

$$|\eta_{\mu}| < 2.4$$

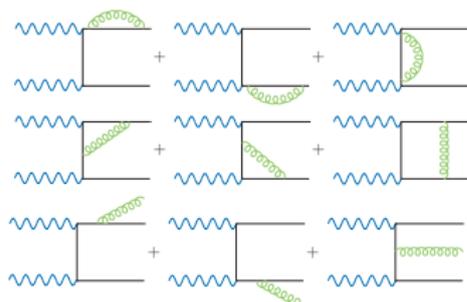
## Elementary cross section



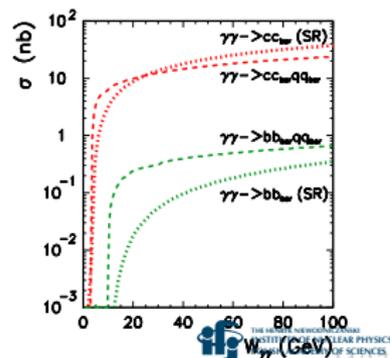
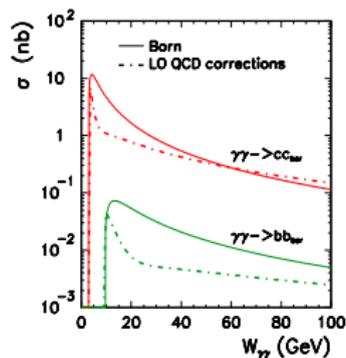
The Born amplitudes.

 $Q\bar{Q}q\bar{q}$  production.

The single-resolved mechanism.

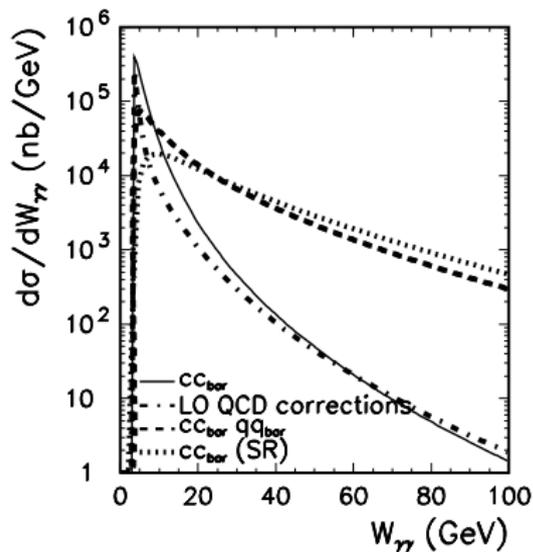


The leading-order QCD corrections.



## Nuclear cross section

$\gamma - \gamma$  subsystem energy



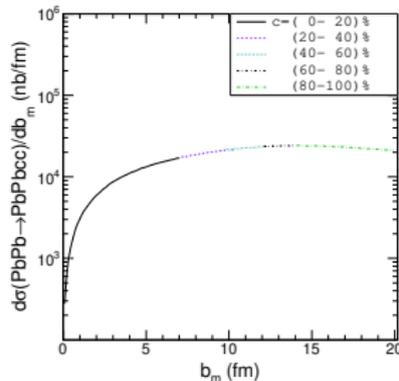
Partial contributions of different mechanisms.

	$\sigma_{tot}$	Born	QCD-corrections
$c\bar{c}$	2.47 mb	42.5 %	14.6 %
		4-quark	Single-resolved
		27.1 %	15.8 %

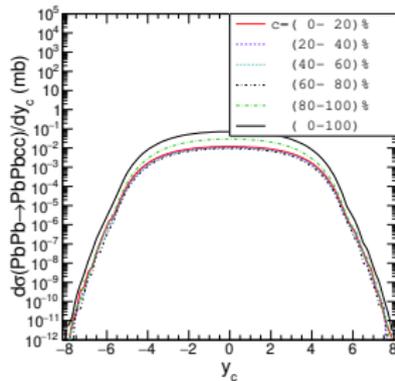
UPC results ( $\sqrt{s_{NN}} = 5.5$  TeV) for  $c\bar{c}$  production

$C\bar{C}$  VS. CENTRALITY**Nuclear cross section**

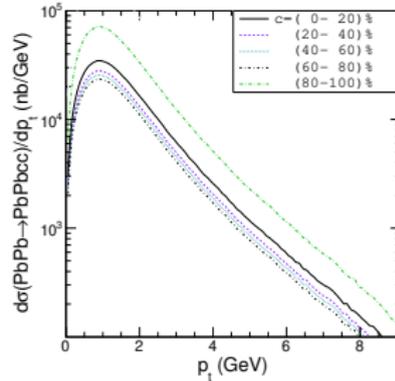
Impact parameter



Rapidity



Transverse momentum

Non-UPC results ( $\sqrt{s_{NN}} = 5.02$  TeV)

# CONCLUSION

- EPA in the impact parameter space
  - Ultrapерipheral & semicentral heavy-ion collisions
  - Fourier transform of the charge distribution
  - Multidimensional integrals → differential cross section
  - Description of experimental data for UPC and semicentral events
    - First description of ALICE data for  $J/\psi$  production; centrality  $< 100\%$
    - Description of STAR and ALICE data for Dilepton production -  $J/\psi$  contribution is missing
  - $c\bar{c}$  production
    - $PbPb \rightarrow PbPbc\bar{c}$
    - $pp \rightarrow c\bar{c}$
    - $pn \rightarrow c\bar{c}$
    - $np \rightarrow c\bar{c}$
    - $nn \rightarrow c\bar{c}$
- $D$  meson production

Thank you