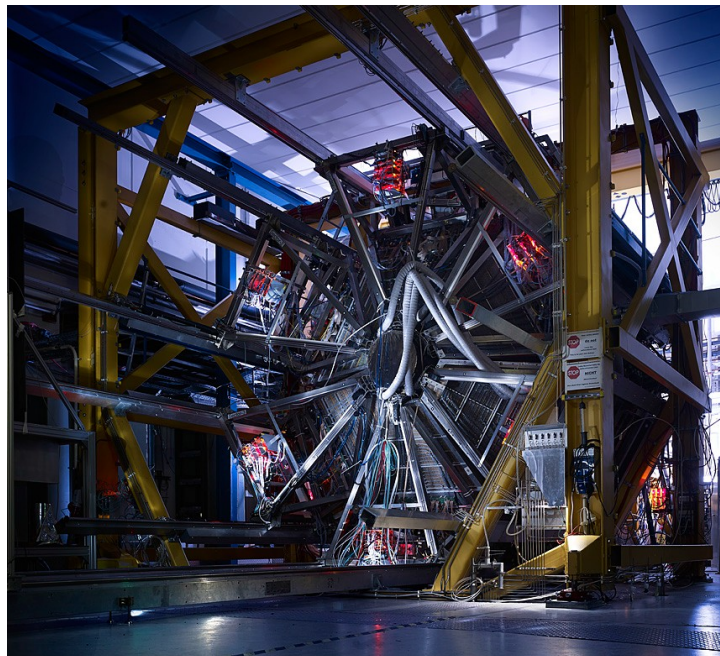


# Studies of pion-induced reactions with HADES



## OUTLINE:

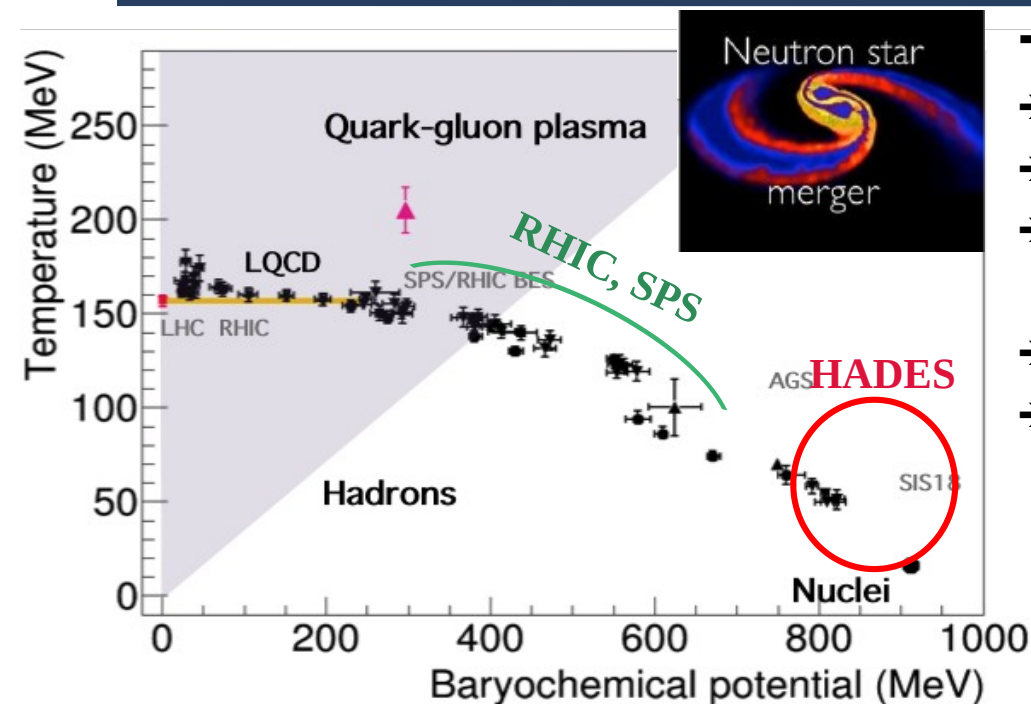
- 1) Motivations of the HADES experiment,
- 2) HADES detector,
- 3) Pion-induced reactions at  $p_\pi = 0.7$  GeV/c:
  - I. Studies of baryon structure with pion beam,
  - II. Studies of pion and proton emission channels with C target (INCL, SMASH, GiBUU, RQMD),
- 4) Conclusions and outlook.



Izabela Ciepał  
24. 03. 2023



# HADES: exploring dense QCD matter

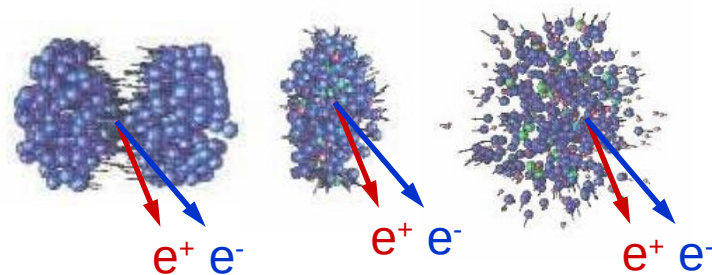


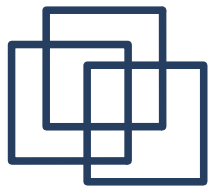
- Equation-of-State: First order transition ?
- Search for a critical point
- Chiral symmetry restoration
- Microscopic structure of baryon dominated matter
- Role of baryonic resonances, hyperons
- Complementary to SPS, RHIC,..

A+A: 1-3A GeV  
 $\sqrt{s}=2-2.4$  GeV

## Observables:

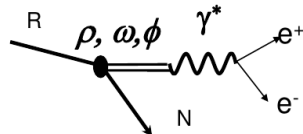
- ✓ Correlations and fluctuations
- ✓ Collective effects
- ✓ Strangeness
- ✓ **Dileptons**





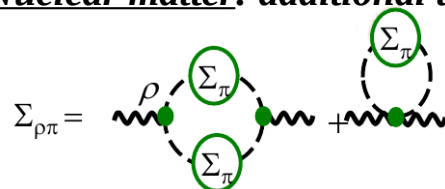
# HI and elementary collisions

- baryon-dominated matter
- role of vector mesons

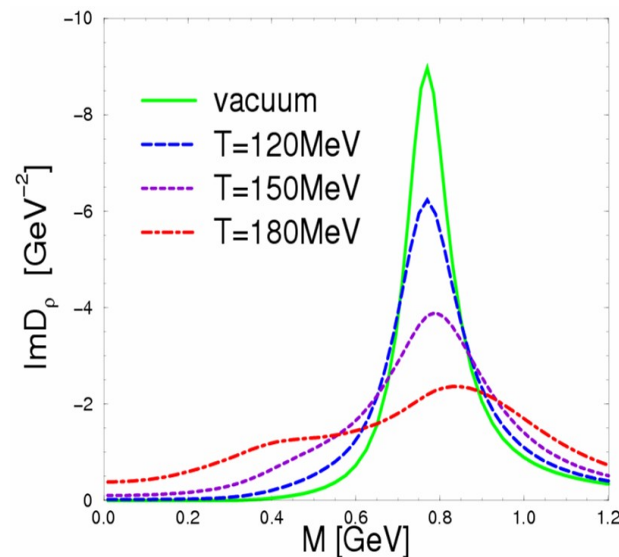
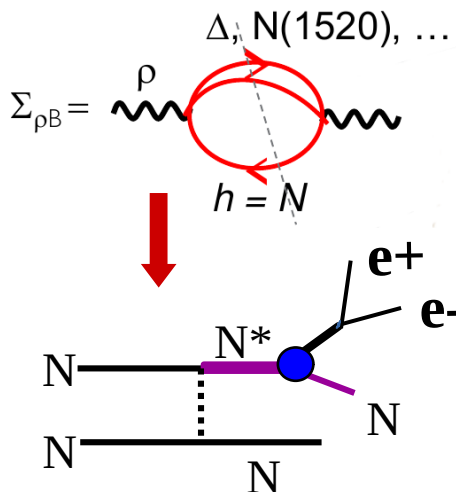


$$D_\rho(M, q, T, \mu_B) = \frac{1}{[M^2 - m_\rho^2 - \Sigma_{\rho\pi\pi} - \Sigma_{\rho B} - \Sigma_{\rho M}]}$$

Nuclear matter: additional terms



**pion loop:  $\pi N$  interactions**



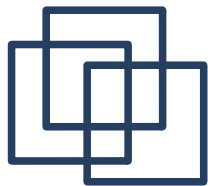
- in-medium  $\rho$  broadening
- chiral symmetry restoration

## $\rho$ -meson

Vacuum:

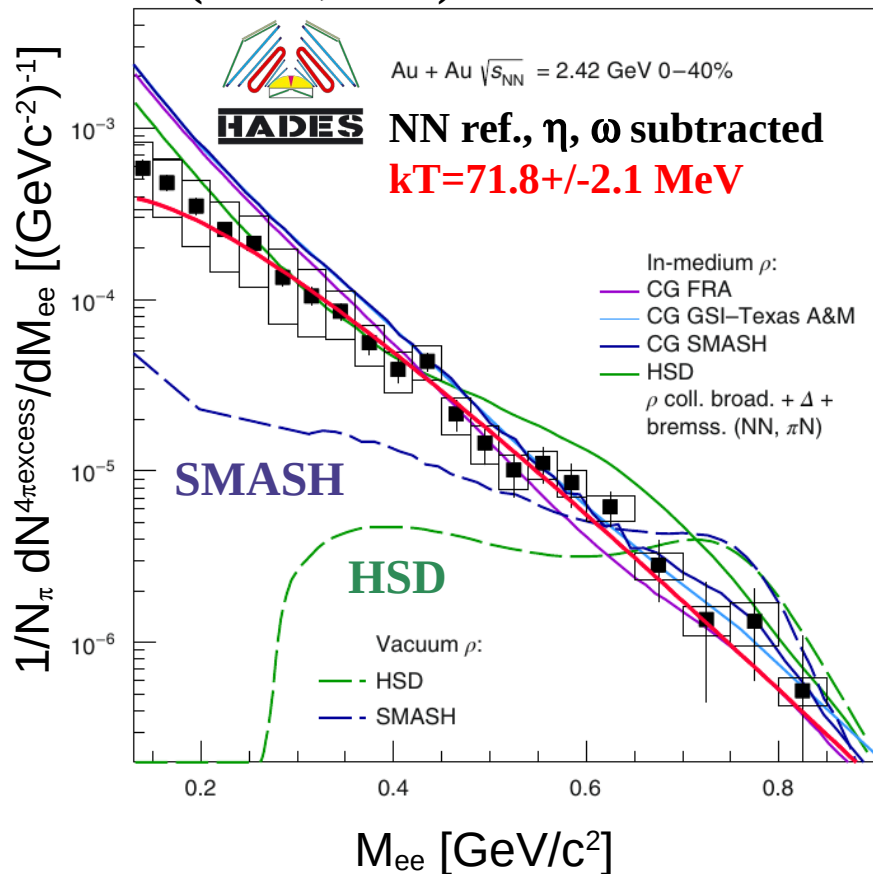


in-medium **spectral function**  
depends on  **$\rho NN^*$  coupling**  
( $N(1520)$ ,  $\Delta(1720)$ ,  $N(1910)$ , ....)  
studied in  **$NN$ ,  $\pi N$  collisions** via  
 $N^*(\Delta) \rightarrow N e^+ e^-$  Dalitz decays



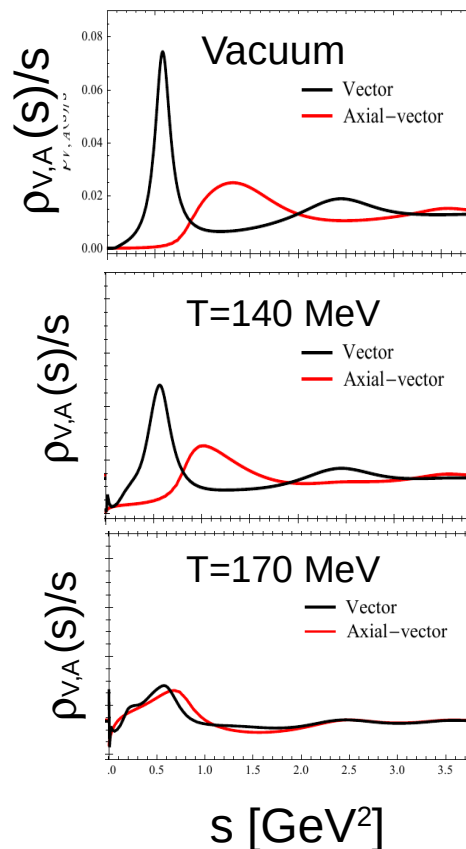
# HI and elementary collisions

- in-medium  $\rho$  broadening (NA60, DLS)



HADES: *Nature Phys.* 15 (2019) 10, 1040

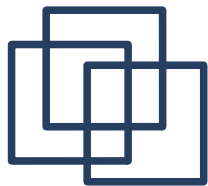
- chiral symmetry restoration
- vector and axial-vector spectral functions



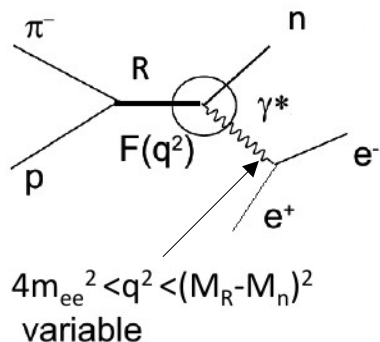
chiral parity  
 partners  
 $\rho(760)/a_1(1260)$   
 become  
 degenerate  
 at  $T \sim T_c$ ,  $\mu_b = 0$   
 ( $\rho$ - $a_1$  mixing)

P. M. Hohler and R. Rapp

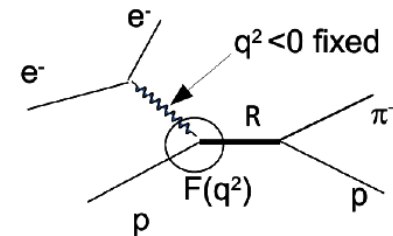
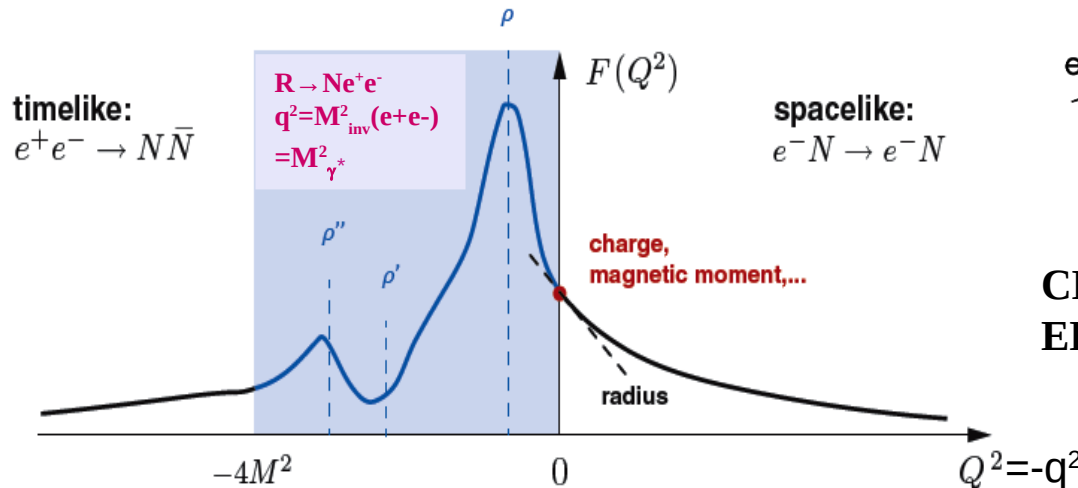
*Nuclear Physics B Proceedings Supplement* 00 (2021) 1



# Electromagnetic structure of baryons



no data available



CLAS/Jlab, MAMI, ELSA, JLab-Hall A, ...

Rezonans → Nucleon Transition Form Factor – **baryon Dalitz decay**

$$\frac{d\Gamma(\Delta \rightarrow N e^+ e^-)}{dq^2} = f(m_\Delta, q^2) \left( |G_M^2(q^2)| + 3|G_E^2(q^2)| + \frac{q^2}{2m_\Delta^2} |G_C^2(q^2)| \right)$$

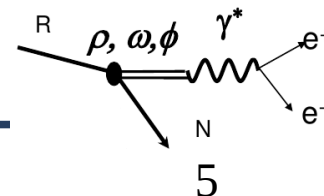
**QED**

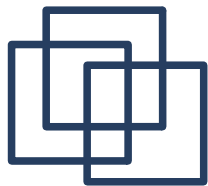
transition of point-like particles

**$G_{M/E/C}$** : Form-Factors

internal structure of hadrons  
(various models)

**Important role of vector mesons:  $J^{PC} = 1^{--}$  ( $=\gamma$ )**

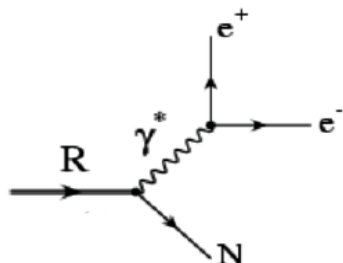




# Dalitz decays of baryon resonances

## QED “point-like”

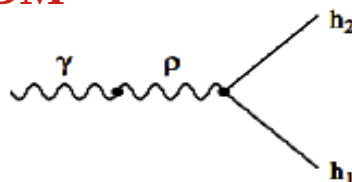
R- $\gamma^*$  vertex



*M. Zetenyi et al.,  
PRC 67, 044002 (2003)*

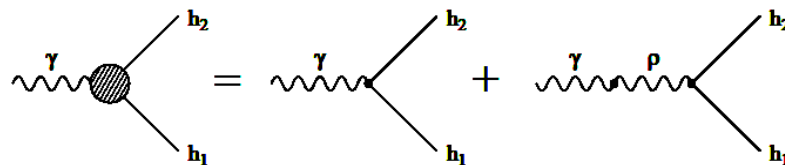
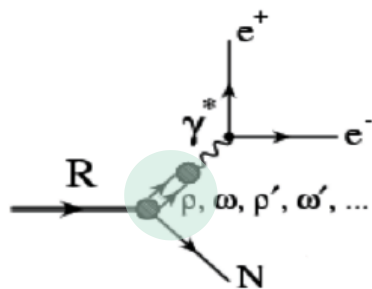
## Vector Meson Dominance Model (VDM)

→ **strict VDM**



*Sakurai, Phys. Rev 22 (1969) 981  
M. I. Krivoruchenko et al.,  
Ann. Phys. 296, 299 (2002)*

→ **2-component VDM**



*Kroll, Lee & Zuminio  
Phys. Rev. 157, 1376 (1967)*





# Implementation of VDMs

## Covariant quark model +VMD

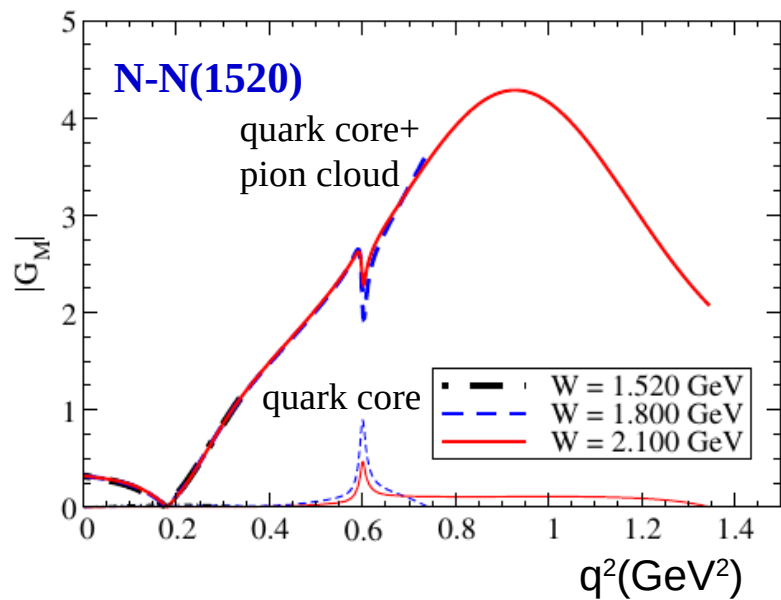
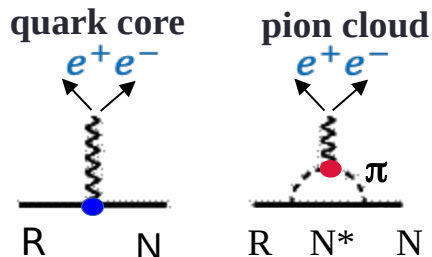
T. Pena & G. Ramalho

N- $\Delta(1232)$ : *Phys.Rev. D*85 (2012) 113014

N-N(1520): *Phys. Rev. D*95, (2017) 014003

N-N(1535): *Phys.Rev. D*101 (2020)114008

VDM:  
quark FF  
pion FF



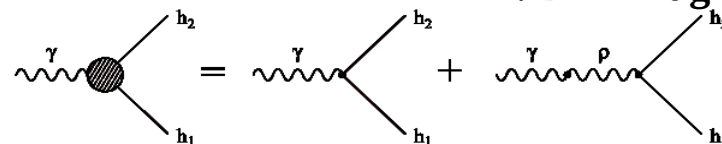
## Two-component Lagrangian model

M. Zetenyi & G. Wolf

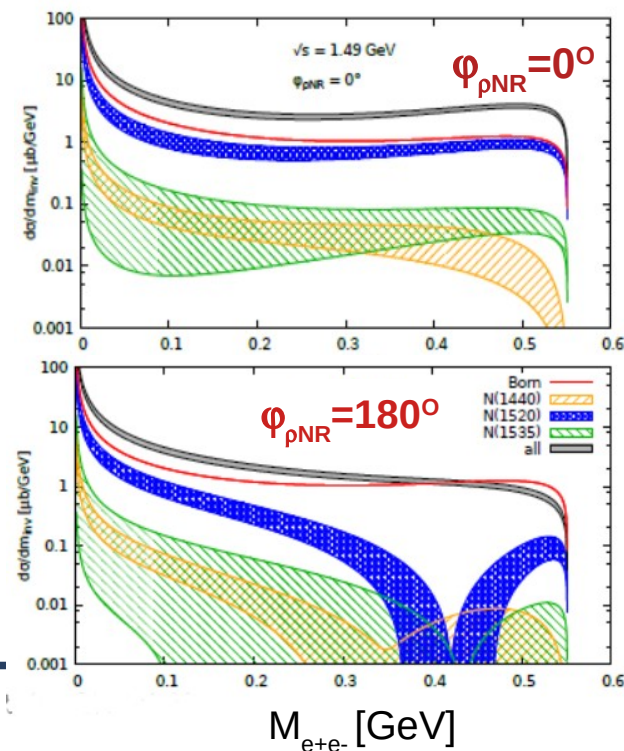
*Phys. ReV. C* 86, 065209 (2012)

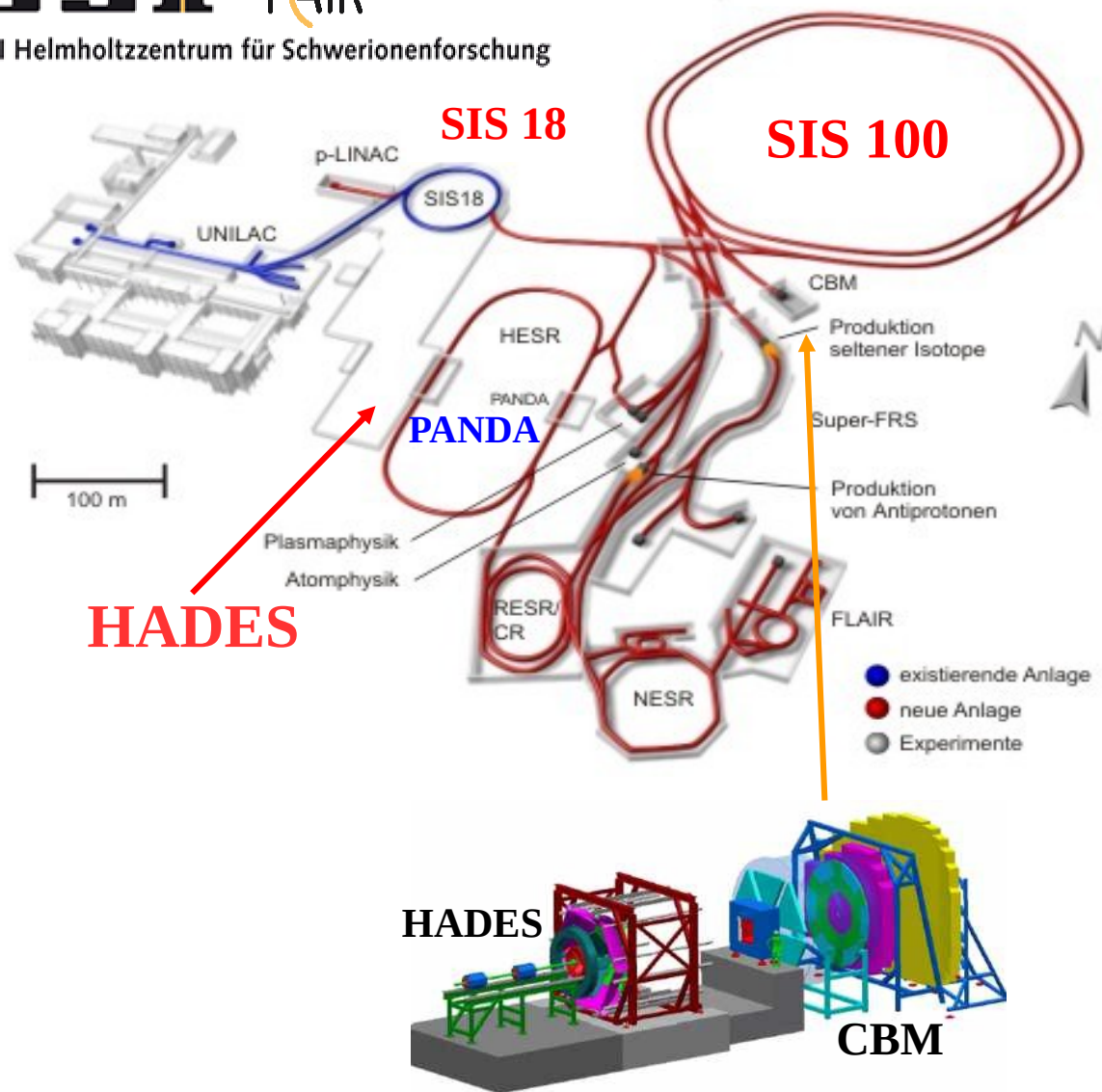
*Phys. Rev. C* 104, 015201 (2021)

VDM1 Lagrangian



Shape and yield  
sensitive to  
the interference  
between  
the  $\gamma$  and  $\rho$   
contributions





**SIS 18**

**18Tm (1.8 T magnets)**

**$U^{73+}$ :** 1.0 GeV/u,  $10^9$  ions/s

**$Ni^{26+}$ :** 2.0 GeV/u,  $10^{10}$

**Protons:** 4.5 GeV,  $2.8 \times 10^{13}/s$

**Secondary beams**

**Pions:** 0.5-2 GeV/c

**SIS 100**

**2T (4T/s) magnets**

**Au:** up to 8-10 GeV/u  
 $10^{12}$  ions/s

**Protons:** up to 30 GeV  
 $2.8 \times 10^{13}$  ions/s

**Secondary beams**

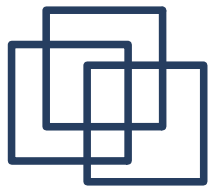
Radioactive beams 1.5 GeV/u

**Anty-protons** 30 GeV

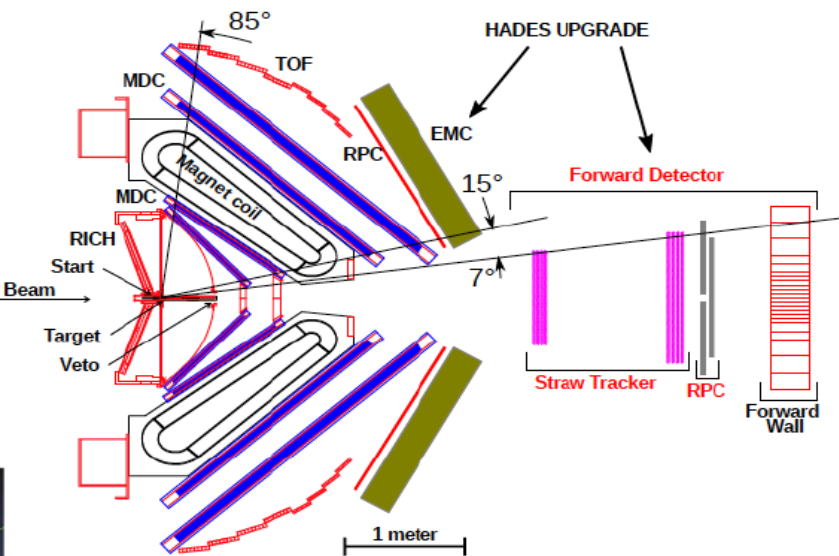
**HADES** - first detector of FAIR Phase0 (2018-2022)



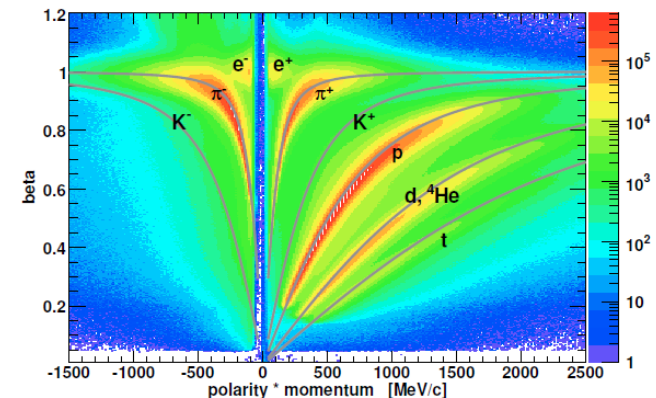
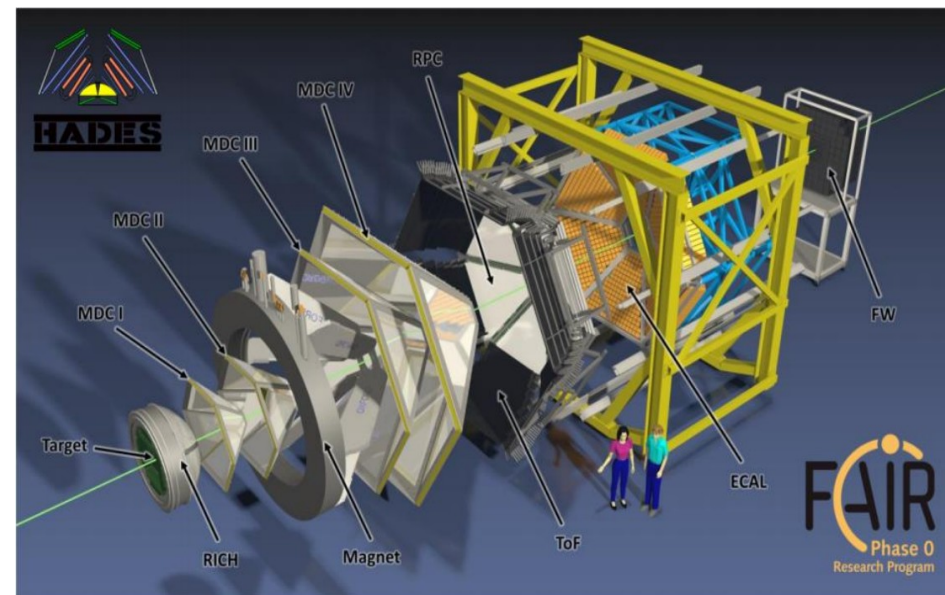




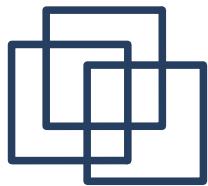
# High Acceptance DiElectron Spectrometer



- ✓ SIS18 beams: protons (1-4.5 GeV), nuclei (1-2 A GeV), pions (0.4-2 GeV) secondary beam
- ✓ Spectrometer with  $\Delta M/M \sim 2\%$  at  $\rho/\omega$
- ✓ PID ( $\pi/p/K$ ): ToF (TOF/RPC, T0 detector), tracking ( $dE/dx$ )
- ✓ momenta, angles: MDC+ magnetic field
- ✓  $e^+, e^-$ : RICH
- ✓ neutral particles: ECAL
- ✓ full azimuthal, polar angles  $18^\circ - 85^\circ$
- ✓  $e^+e^-$  pair acceptance  $\sim 0.35$





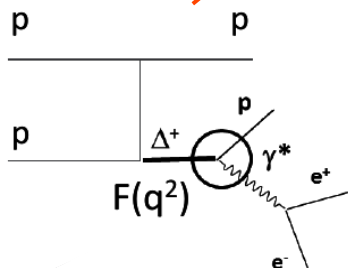
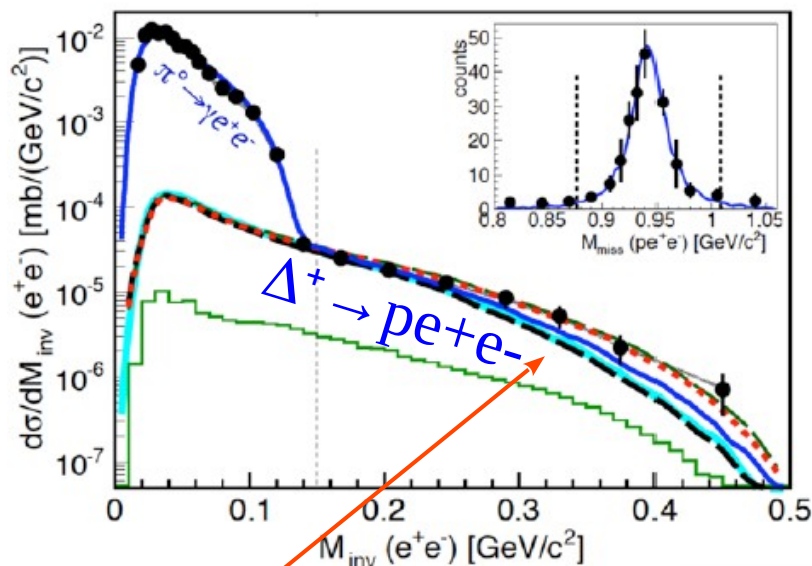


# $\Delta(1232)$ resonance - **exclusive** $pe^+e^-$ analysis

HADES: *Phys. Rev. C* 95, 065205 (2017)

**$pp \rightarrow ppe^+e^-$  @1.25 GeV**

→ cross sections for  $pn\pi^+$ ,  $pp\pi^0$  using PWA



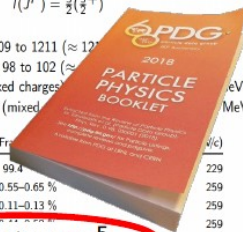
$\Delta(1232) \ 3/2^+$

$I(J^P) = \frac{3}{2}(\frac{3}{2}^+)$

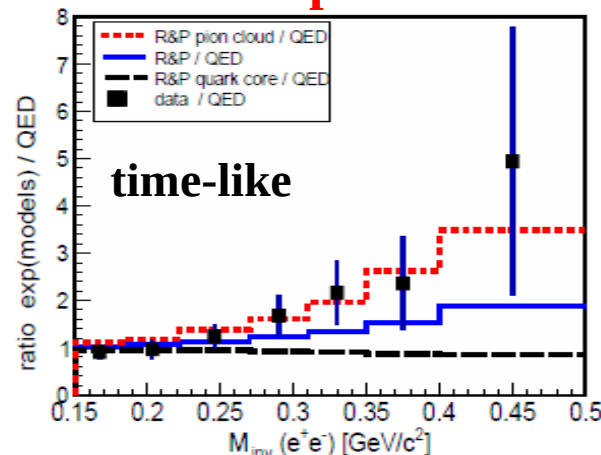
Re(pole position) = 1209 to 1211 ( $\approx 1210$ ) MeV  
 $-2\text{Im}(\text{pole position}) = 98$  to  $102$  ( $\approx 100$ ) MeV  
 Breit-Wigner mass (mixed charges)  
 Breit-Wigner full width (mixed)

$\Delta(1232)$  DECAY MODES

Decay Mode	Branching Ratio (%)	Partial Width (MeV)
$N\pi$	99.4	229
$N\gamma$	0.55-0.65 %	259
$N\gamma$ , helicity=1/2	0.11-0.13 %	259
$N\gamma$ , helicity=3/2		259
$pe^+e^-$	$(4.2 \pm 0.7) \times 10^{-5}$	259

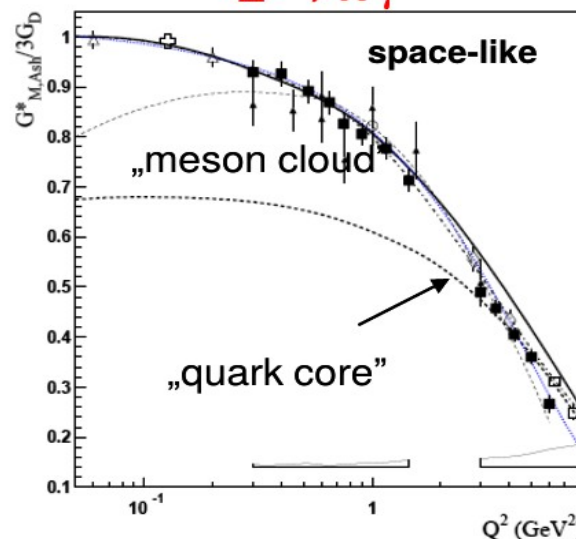


**$\Delta^+ \rightarrow pe^+e^-$**



time-like

**$\Delta \rightarrow N \gamma$**

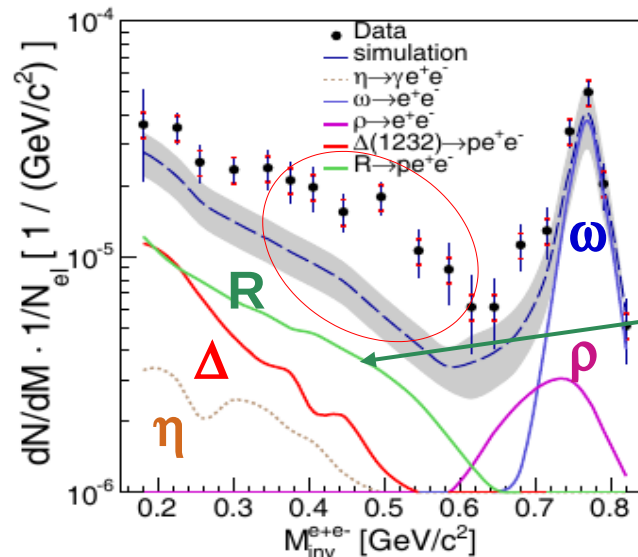


I. G. Aznauryan and V. D. Burkert,  
*Prog. Part. Nucl. Phys.* 67, 1 (2012)



# Dalitz decay studies of heavier baryons

HADES: EPJ A50, 82 (2014)

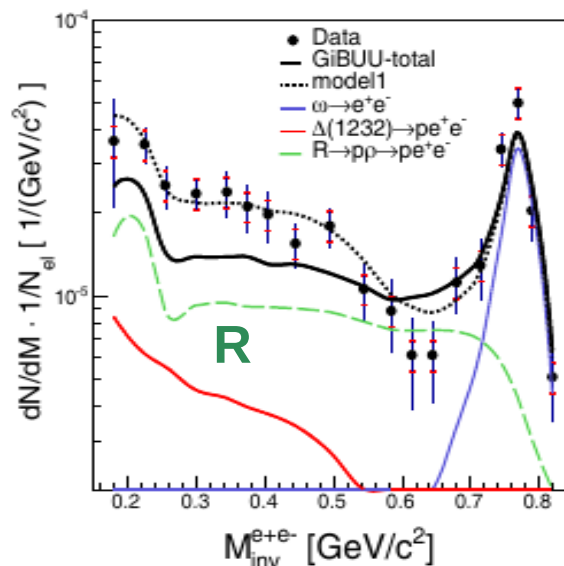
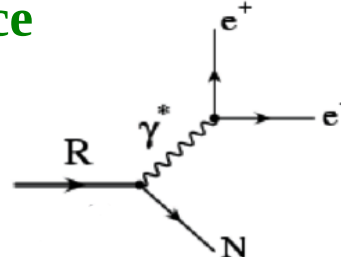


$pp \rightarrow ppe^+e^-$  @3.5 GeV

Dalitz decays of **point-like** baryonic resonances  
(constrained by  $pp\pi^0$  and  $pn\pi^+$  channels)

**QED reference**

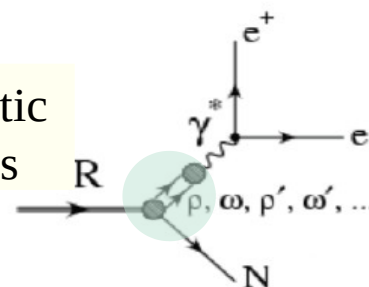
$R \rightarrow pe+e^-$



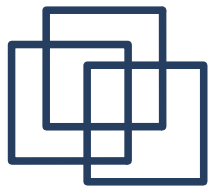
effect of electromagnetic  
transition Form Factors

$R \rightarrow pp \rightarrow pe+e^-$

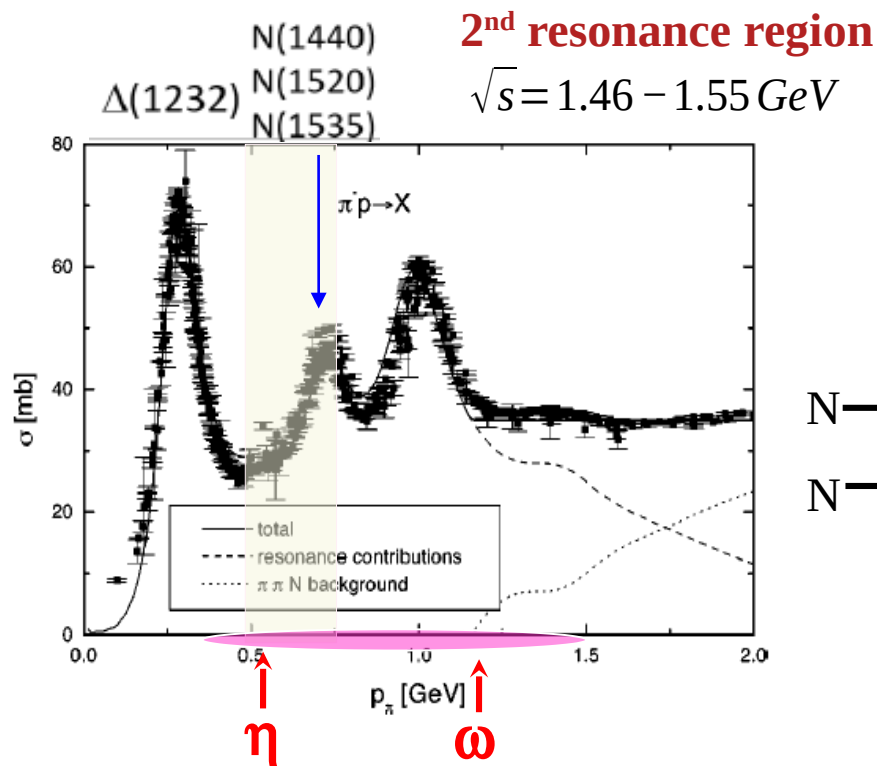
**model 1** = GiBUU, but with modified  
cross sections (HADES simul. )



$R = \Delta^+(1232)$   
 $N^*(1440)$   
 $N^*(1520)$   
 $N^*(1535)$   
 $N^*(1680)$   
 $\Delta^+(1700)$   
 $\Delta^+(1910)$

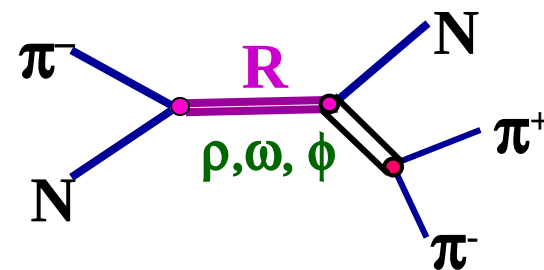
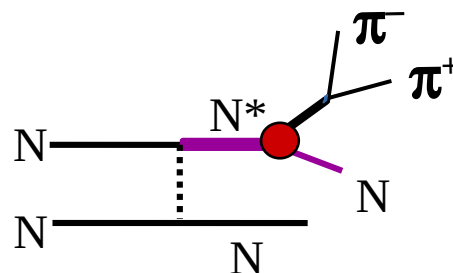


# Motivations for pion beam experiments with HADES



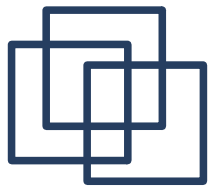
**selectivity:**

production of resonance with given mass in s-channel



**HADES + GSI pion beam is an ideal (unique in world) tool to:**

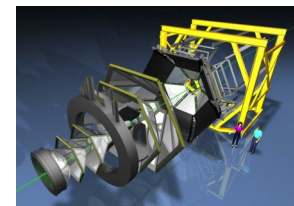
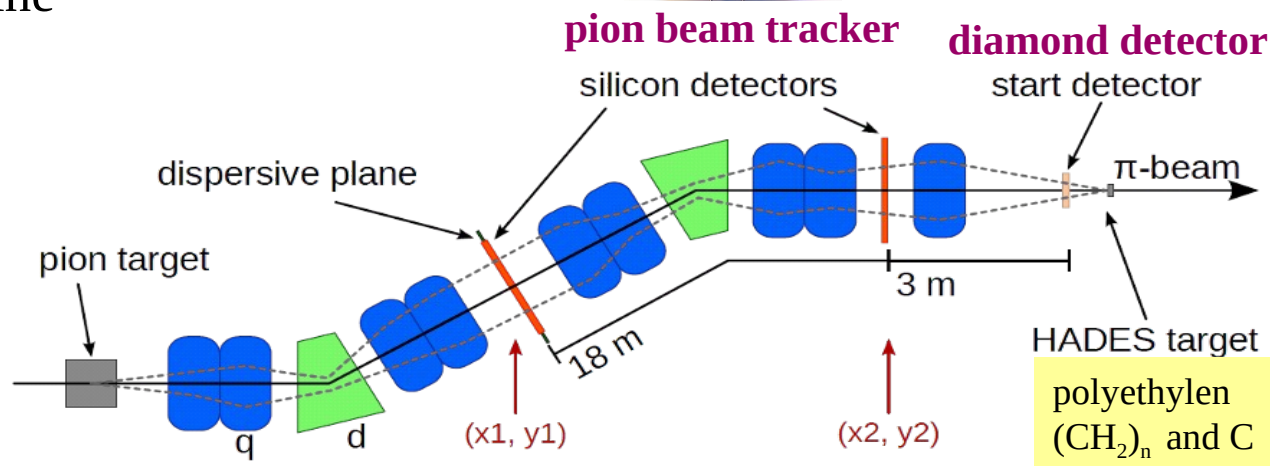
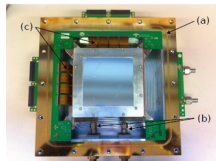
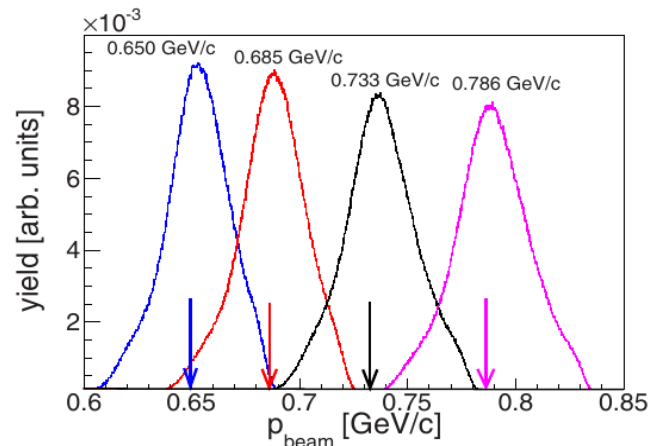
- Study the time-like electromagnetic structure of baryons
- Complete the very scarce pion beam data base for hadronic couplings
- **Dilepton channel**  $R \rightarrow N e^+ e^-$ , **never** measured in pion induced reactions



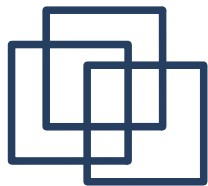
# Pion beam facility @ GSI

*Eur. Phys. J. A 53, 188 (2017)*

- reaction **N+Be**,  $8-10 \cdot 10^{10}$   $N_2$  ions/spill (4s)
- secondary  $\pi^-$  with **I**  $\sim 2-3 \cdot 10^5/s$
- $p = 650, \textbf{685}, 733, 786$  (+/- 1) MeV/c
- **PE**  $(CH_2)_n$  and **C** targets

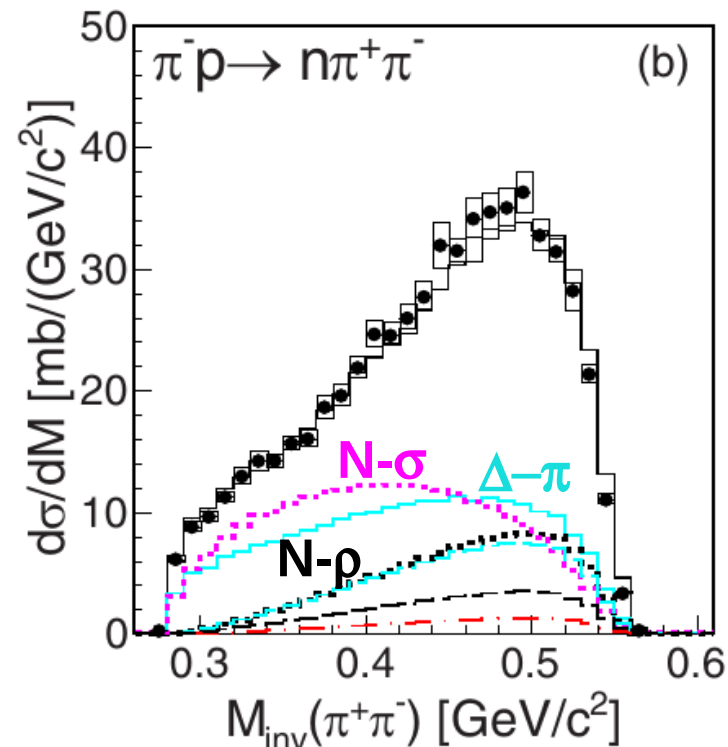






# 2-pion production in $\pi\bar{p}$

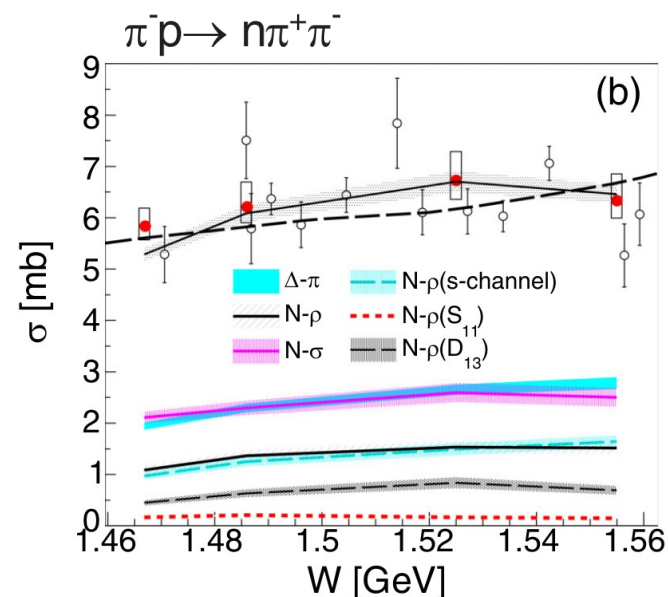
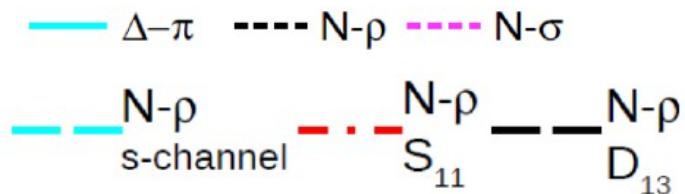
HADES: *Phys. Rev. C* 102, 024001, (2020)



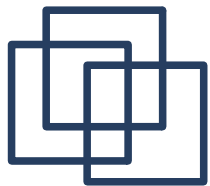
HADES data ( $\pi^-p \rightarrow n\pi^+\pi^-$  and  $\pi^-p \rightarrow p\pi^0\pi^-$  at 4 energies )  
+ photon (CB-ELSA, MAMI) and pion (Crystal Ball) data base  
included in **Bonn-Gatchina Partial Wave Analysis**

**s-channel**  
**N(1520) 3/2-**  
**dominant contribution**  
**BR=11.8 +/- 1.9 %**  
**in  $\rho$  production**

**crucial**  
**for e+e- analysis**

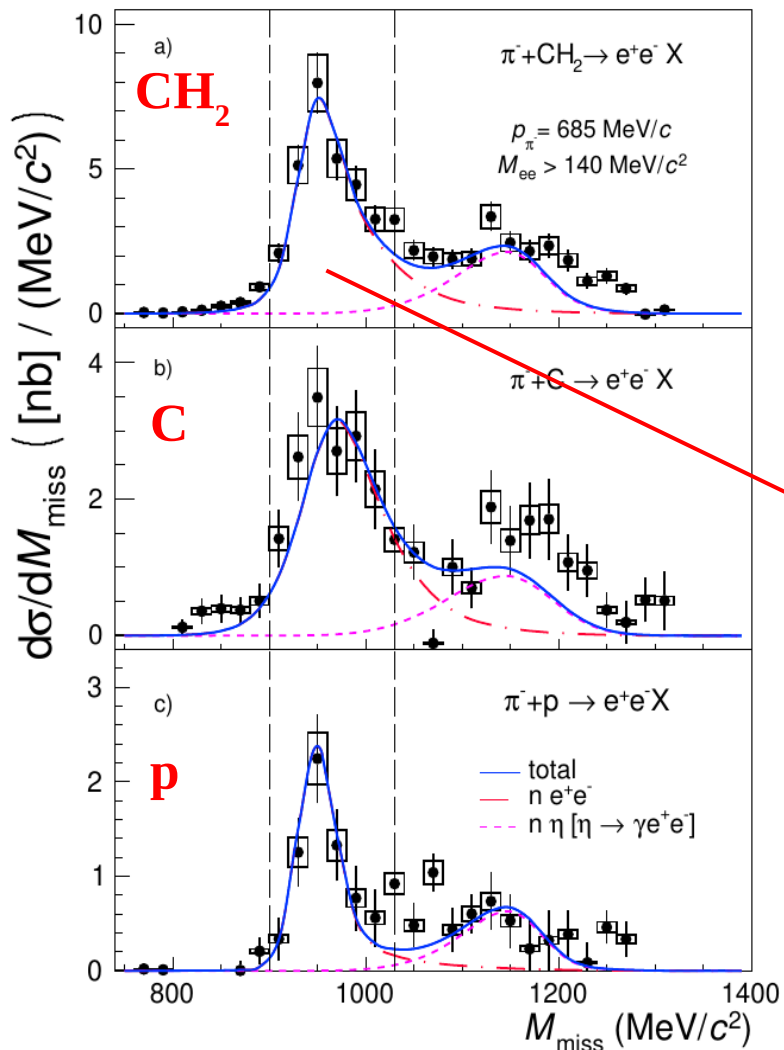


Branching ratios of N(1440), N(1535), N(1520) to  $2\pi$  channels ( $\Delta\pi$ ,  $\sigma N$ ,  $\rho N$ )  
→ **8 new entries** (4 first + 4 additional entries)

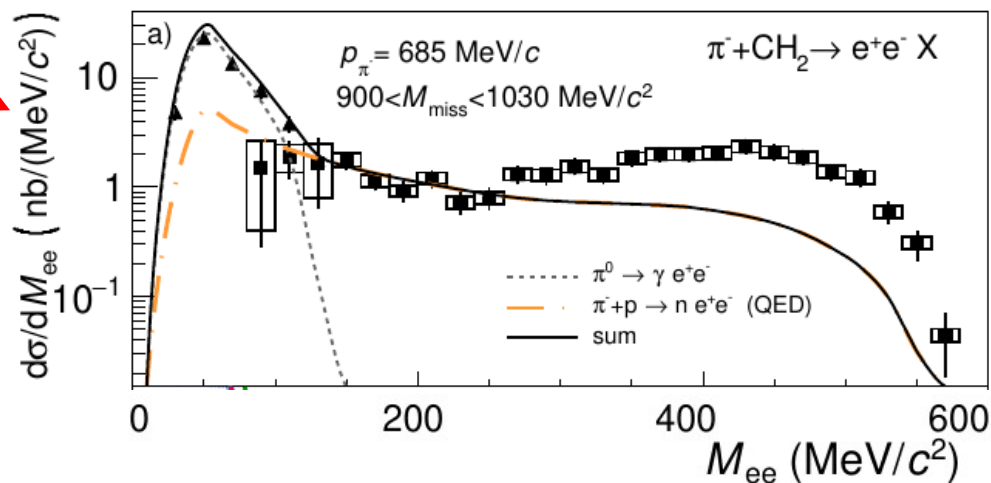


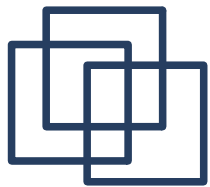
# Selection of quasi-free $\pi^- p \rightarrow n e^+ e^-$

HADES Coll. *arXiv:2205.15914 [nucl-ex]*



- cut on  $\text{inv} M_{e^+ e^-} > 140 \text{ MeV}$  ( $\pi^0$  removed)
- selection of  $\pi p \rightarrow n e^+ e^-$  exclusive channel using missing mass cut ( $\eta$  removed)
- quasi-free treatment of  $\pi C$  interaction



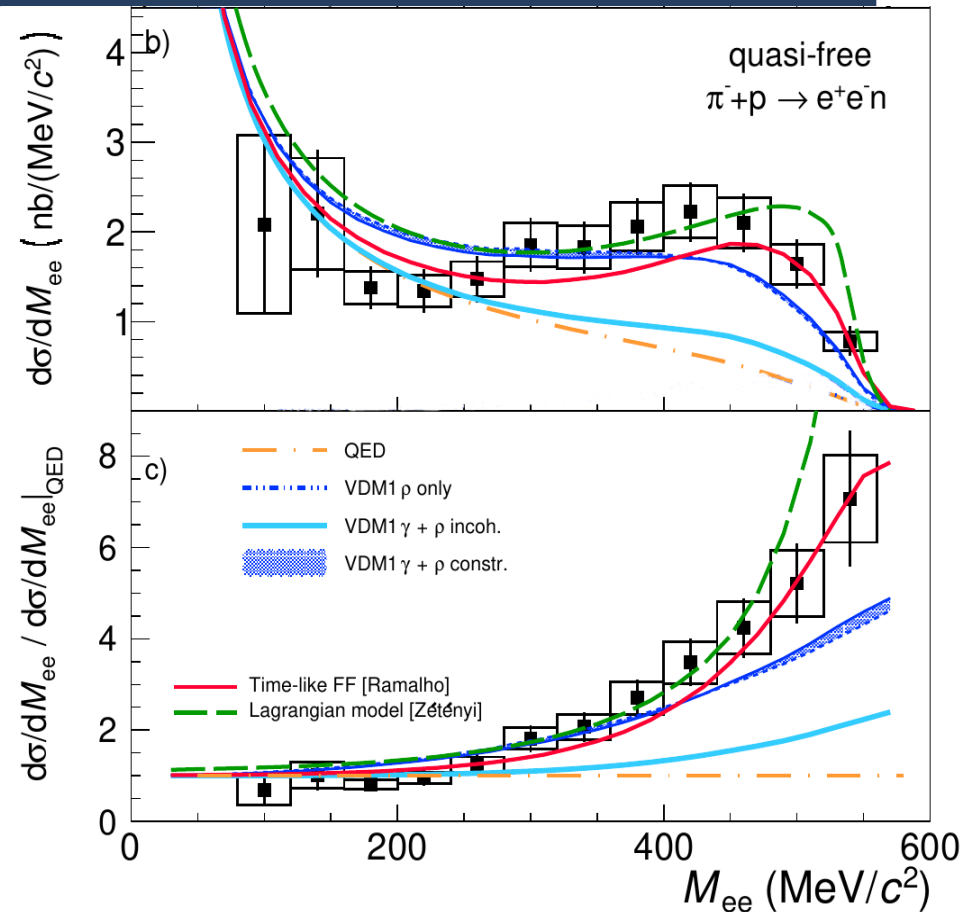
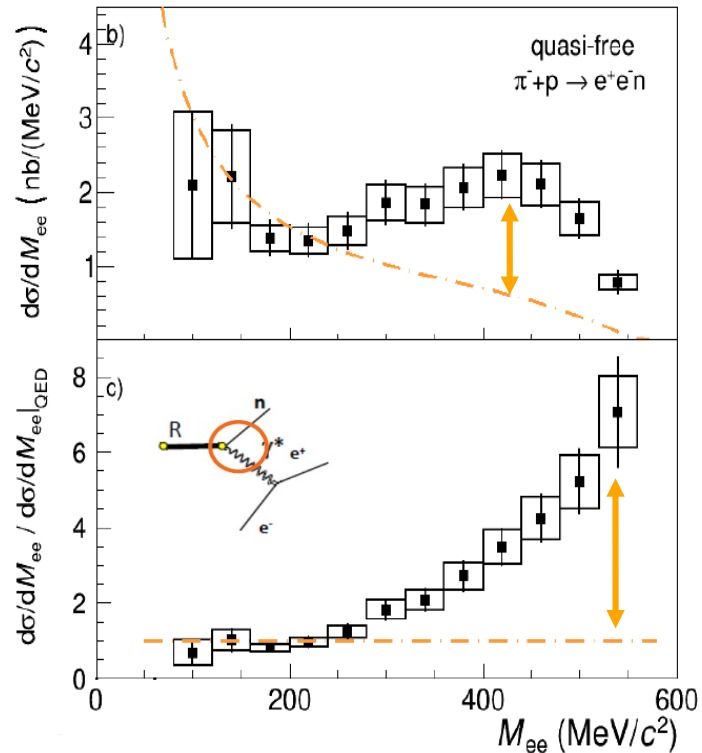


# Effective time-like transition form factor

$$R_{\text{QED}} = (d\sigma/dM) / (d\sigma/dM)_{\text{QED}}$$

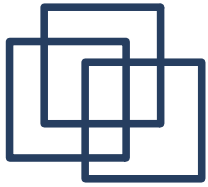
HADES Coll. arXiv:2205.15914 [nucl-ex]

## huge excess over point-like QED



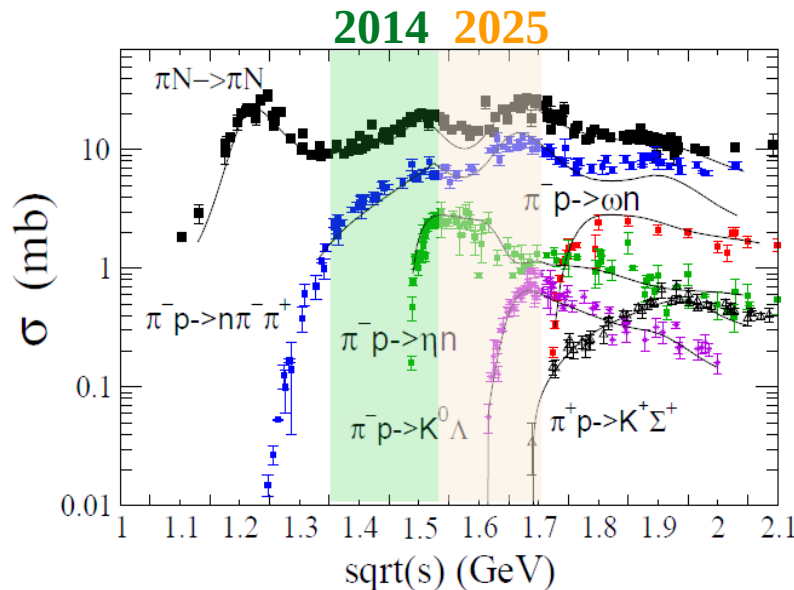
- $M_{ee} < 200 \text{ MeV/c}^2$  consistency with QED reference
- Strong excess at larger  $M_{ee}$  (up to a factor 5)

VDM1 - gives reasonable description  
 Lagrangian model – very promising  
 Time-like FF - dominant pion cloud contribution (pion emFF)



# Summary

- **HADES & pion beam** is an unique tool to understand in details **baryon- $\rho$  couplings**:
  - significant off-shell contribution originating from  $N(1520)D_{13}$  shown by combined PWA,
  - $D_{13}(1520)$  coupling to  $\rho$ -N:  $12\pm 2\%$ ,
  - very new information on electromagnetic baryon transitions in the time-like region,
- Proposal for pion beam experiment in 2025 in the third resonance region.

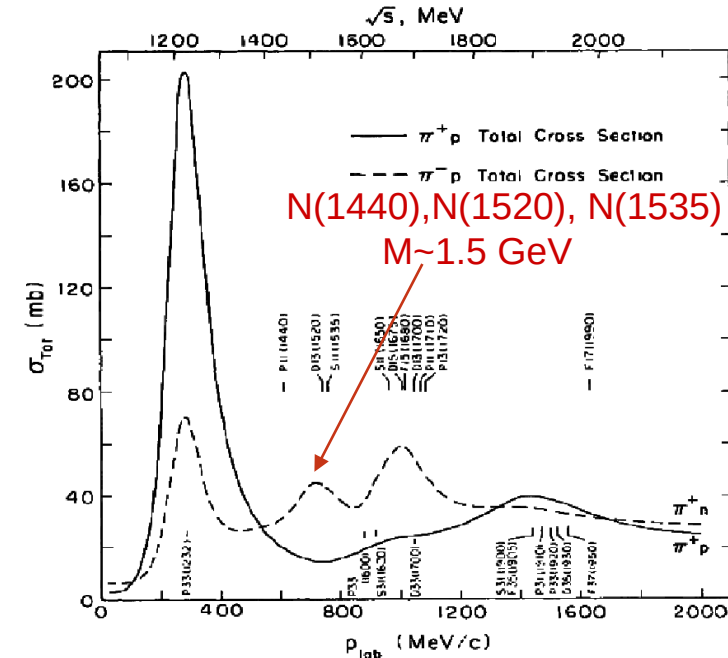


Investigate heavier resonances  
 $N(1620)$ ,  $N(1720)$ , ...  
in  $e^+e^-$  channels and many hadronic  
channels, e.g.  $\pi\pi N$ ,  $\omega n$ ,  $\eta n$ ,  $K^0\Lambda$ ,  $K^0\Sigma$ , ....

# Studies of pion and proton emission channels with C target

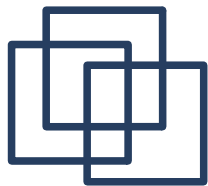
**Main goal:** microscopic structure of baryon dominated matter and role of baryonic resonances in the 2<sup>nd</sup> resonance region.

- **test of transport models** used as a tool to identify medium effects (study of various reaction mechanisms) in heavy-ion collisions at a few AGeV,
- **pion dynamics** crucial to describe the evolution of the collision:  
→ real pions copiously produced



## Previous investigations with pion beam:

- $P_{\pi} < 250 \text{ MeV/c}$ :  $\Delta(1232)$  resonance region well-known.
- $300 < P_{\pi} < 500 \text{ MeV/c}$ : few measurements ( $\pi, \pi X$ ) or ( $\pi, \pi \pi X$ ) (LAMPF, TRIUMF, KEK).
- $P_{\pi} > 500 \text{ MeV/c}$ : only total cross sections (Saturne-1, NIMROD, BNL) and differential elastic cross sections (KEK).

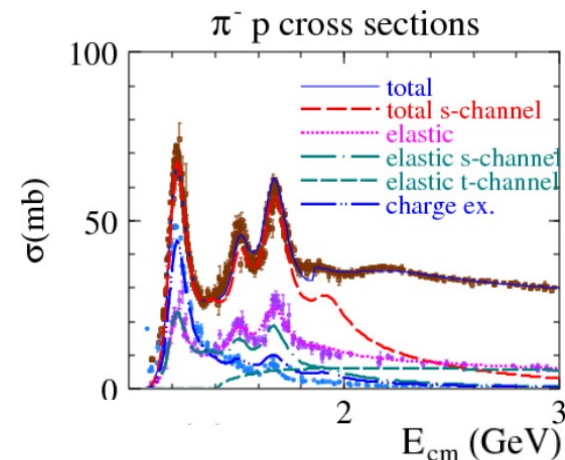


# Transport models

- Nucleon Fermi gas,
- Binary interactions: inelastic collisions through resonance/string excitation and decay,
- All **baryonic resonances** included ( $\Delta(1232)$ ,  $N(1440)$ ,  $N(1520)$ , ... up to  $M=2 \text{ GeV}/c^2$ ),
- Elementary cross-sections adjusted to data.

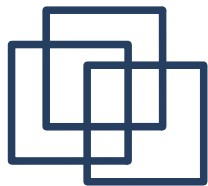
$\pi N \rightarrow R(\text{string}), R \rightarrow \pi N, \pi\pi N$

$pp \rightarrow pR, R \rightarrow \pi N$



BUU (Boltzmann-Uehling-Uhlenbeck transport equation)		QMD (Quantum Molecular Dynamics)	
GiBUU	SMASH	RQMD.rmfm	UrQMD
<a href="https://gibuu.hepforge.org">https://gibuu.hepforge.org</a>	<a href="https://smash-transport.github.io">https://smash-transport.github.io</a>		<a href="http://urqmd.org">http://urqmd.org</a>
momentum-dependent mean field potential	mean field potential	potential: sum of potentials from surrounding particles (wave packets)	
		mom.-dep.	non mom.-dep.
only field-type (continuous) interaction via the mean field, no N-N int. (except for collisions)		particle moves in the potential + collides with neighbours	
		N-N interaction	

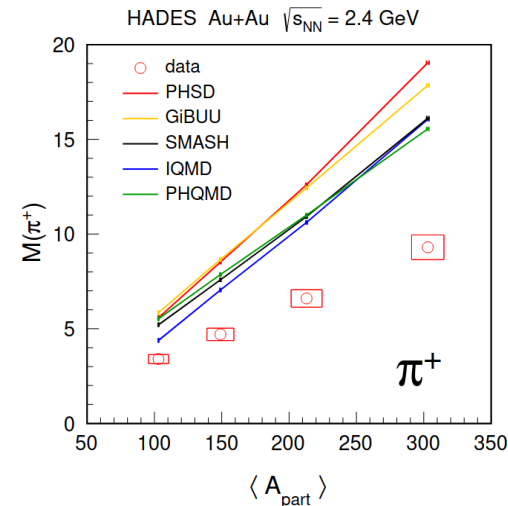
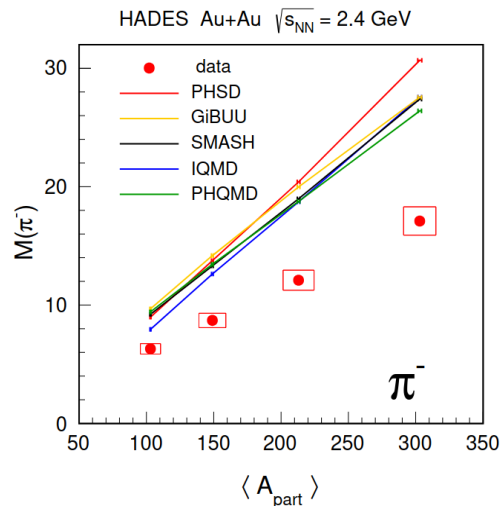




# Open issues .....

- **HI collisions with HADES**  
overestimation of pion production

HADES: *Eur. Phys. J. A* 56, 259 (2020)

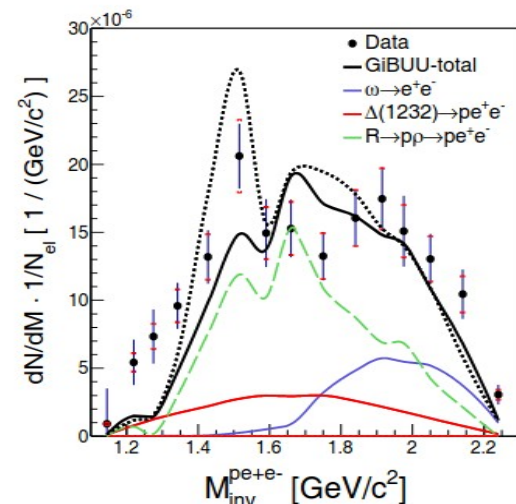
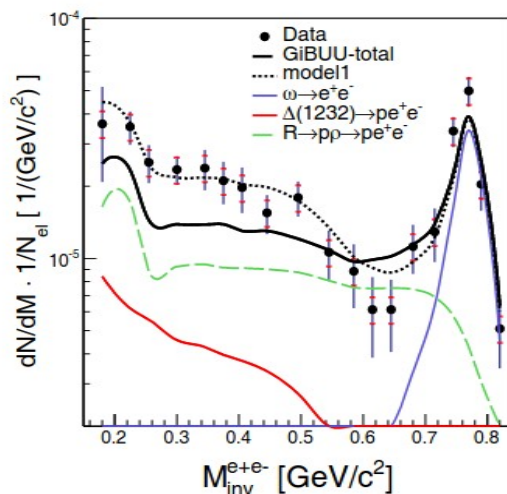


- **pp → ppe<sup>+</sup>e<sup>-</sup> @3.5 GeV**

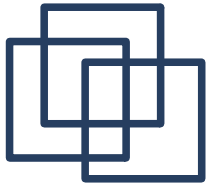
HADES: *EPJ A* 48, 64 (2012)

**model 1** = GiBUU, but with modified cross sections (HADES simul. )

R = N\*(1520) - 38%  
N\*(1720) - 22%  
Δ<sup>+</sup>(1620) - 15%  
Δ<sup>+</sup>(1905) - 7%



→ pp validates only the primary NN collisions....



# INCL++ cascade model

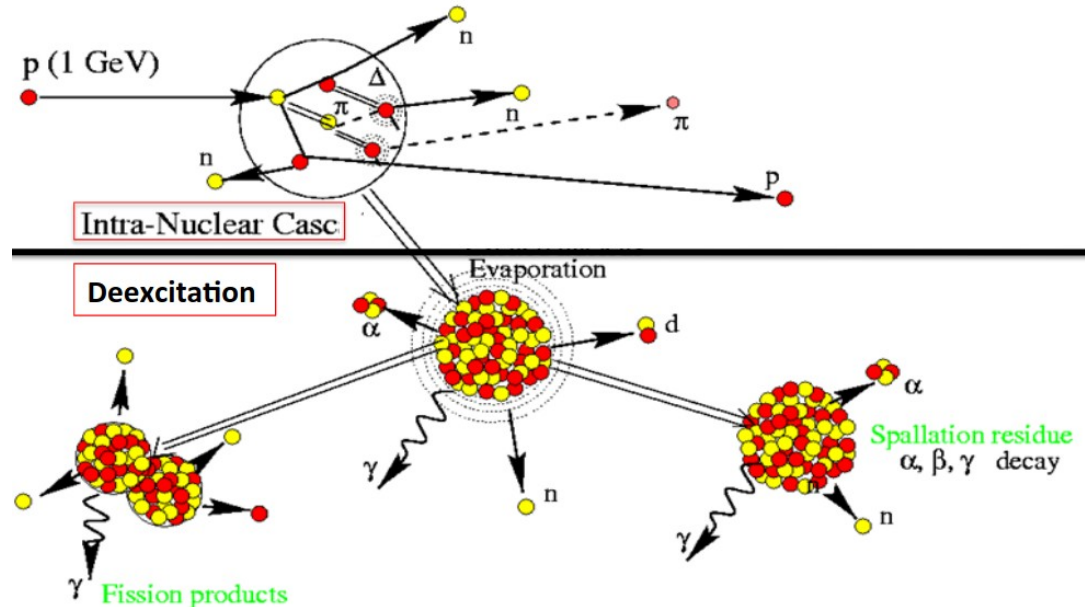
<https://irfu.cea.fr/dphn/Spallation/incl.html>

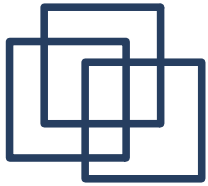
- Based on transport equations, but **constant potentials** are applied.
- Baryon spectrum: only  **$\Delta(1232)$  resonance** is included.
- Dynamic creation of composity nuclear products (surface coalescence).

## Applications:

- GEANT4
- Interaction of pions in detectors (e/ $\pi$  discrimination)
- Neutrino physics.

p/ $\pi$ /light ions + A





# $\pi^- + {}^{12}\text{C}$ @ 685 MeV/c

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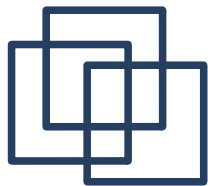
## Our strategy:

- Test transport models and INCL++: investigate various exit channels of  $\pi^- + {}^{12}\text{C}$  to constrain the description of various processes: quasi-elastic, rescattering, pion absorption,...
- Events are generated based on different models,
- Events processed through detector material (GEANT),
- Reconstruction of simulated events same as data events.

- “inclusive”: p,  $\pi^+$ ,  $\pi^-$ , d, t (TOF/RPC Mult2 trigger)
- quasi-elastic:  $\pi^- + {}^{12}\text{C} \rightarrow \text{p} + \pi^- + \text{X}$  (SRC, rescattering)
- 2-particle:  $\pi^-\pi^+$ ,  $\pi^-\pi^-$ , pp,  $\text{p}\pi^+$ ,  $\text{p}\pi^-$
- 3-particle:  $\text{p}\pi^-\pi^+$ ,  $\text{p}\pi^+\pi^-$ ,  $\text{pp}\pi^-$ ,  $\text{ppp}$

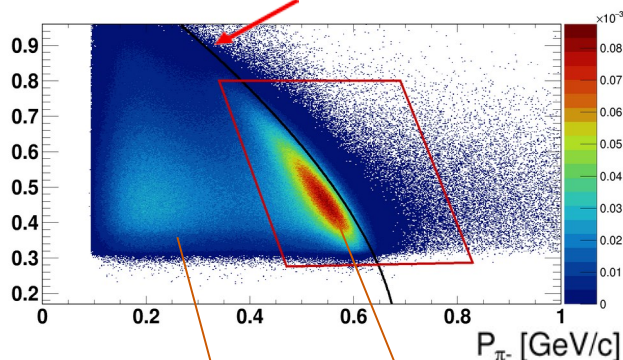
## Models:

- **INCL**
- RQMD.rmfm
- SMASH
- GiBUU

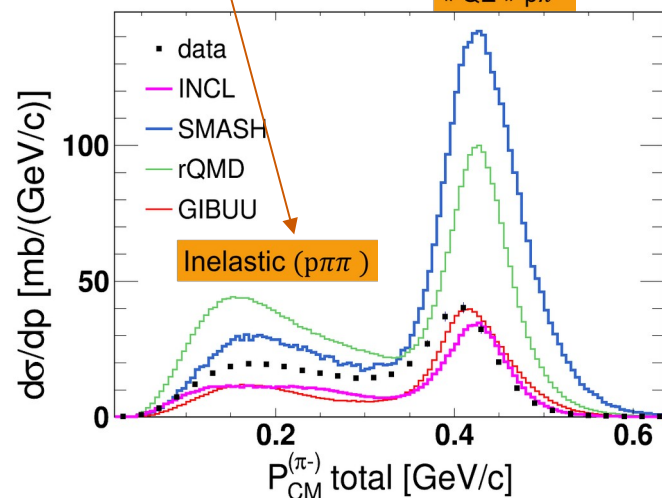


# $\pi^- + {}^{12}\text{C} \rightarrow \pi^- + p + X$ quasi elastic

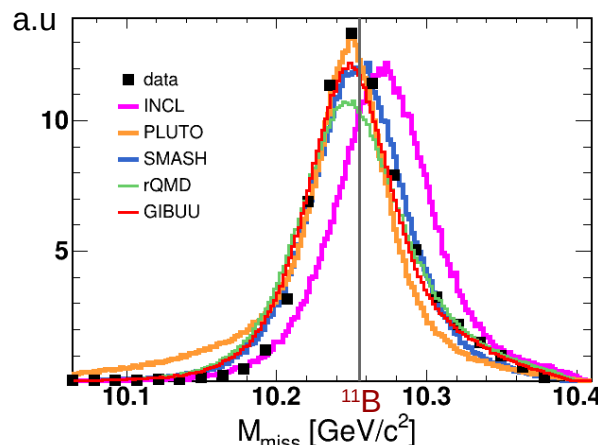
$p_p$  vs  $p_\pi$  typical of binary reaction  $\pi^- + p \rightarrow \pi^- + p$



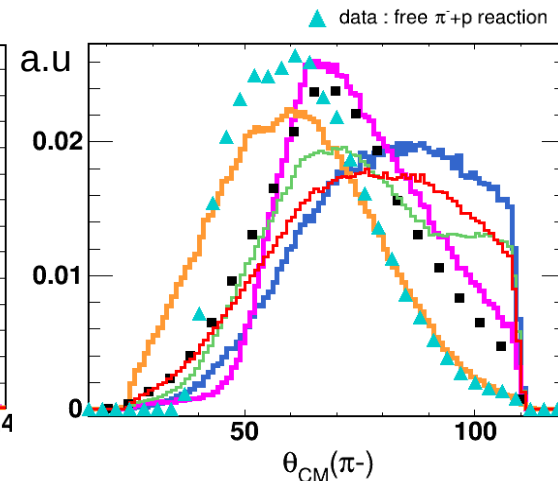
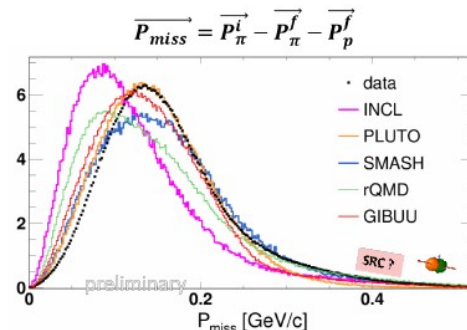
« QE »  $p\pi^-$



$$M_{miss} = M_{(\pi^- + {}^{12}\text{C} \rightarrow \pi^- + p + X)}$$

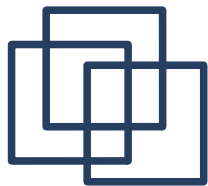


missing mass shifted in INCL



INCL reproduces well pion angular distribution

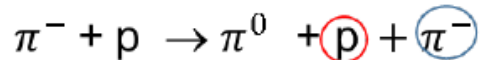
- SMASH & rQMD overestimate data
- INCL underestimates data



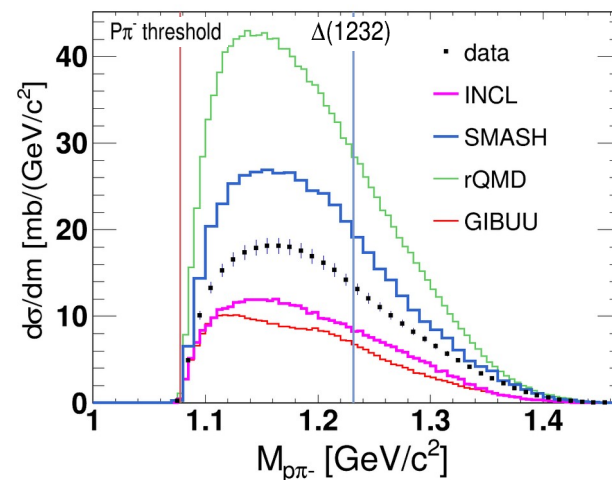
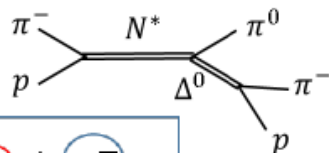
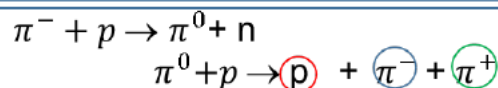
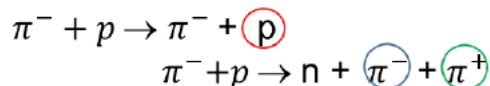
# $\pi^- + {}^{12}\text{C} @ 685 \text{ MeV/c}$

## $p\pi^-$ : Inelastic

Single step



Multi step

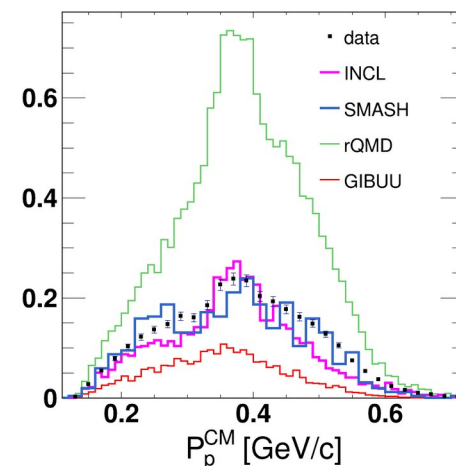
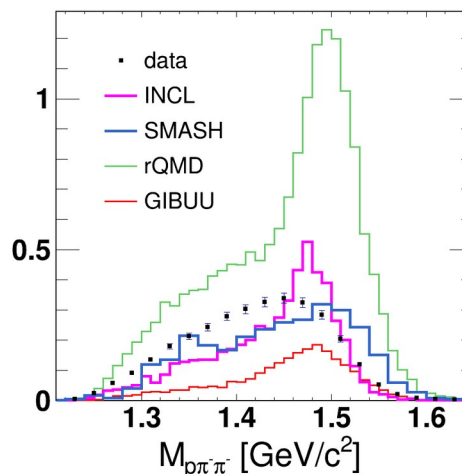
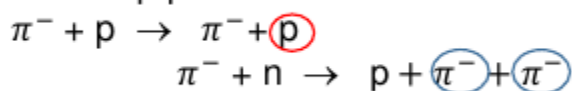


## $p\pi^- \pi^-$

Single step production:



Two step production:



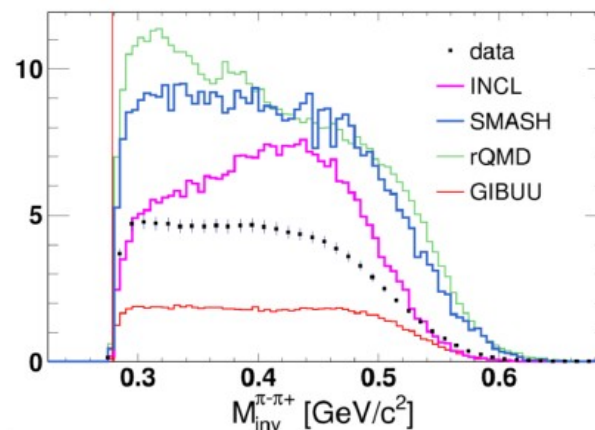
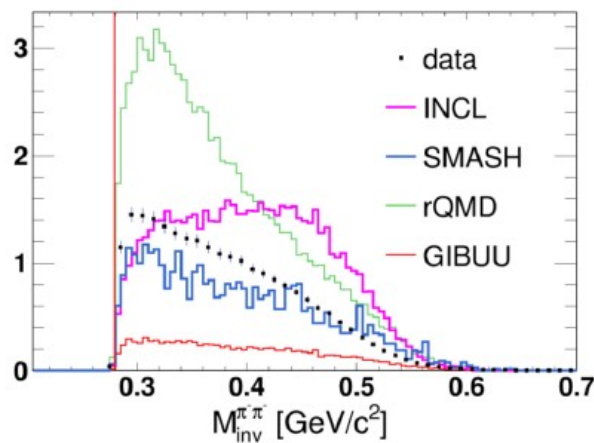
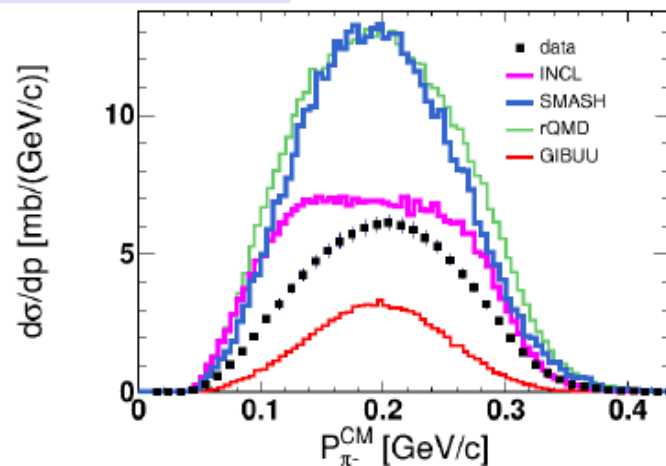
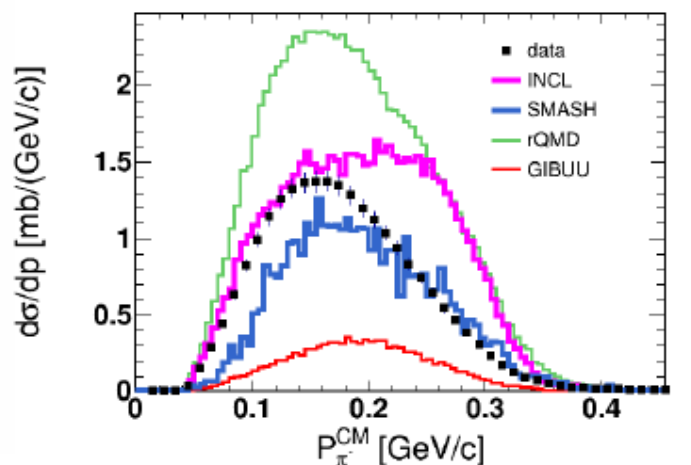


# $\pi^- + {}^{12}\text{C} @ 685 \text{ MeV/c}$

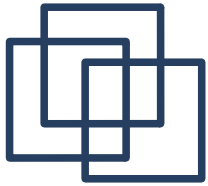
$\pi^- \pi^-$

- $\pi^- \pi^-$  same 2-step processes as  $p \pi^- \pi^-$
- $\pi^- \pi^+$  can be produced in  $\pi^- + p \rightarrow n + \pi^- + \pi^+$   
 $\sigma = 6.2 \text{ mb} \rightarrow$  higher yields

$\pi^- \pi^+$



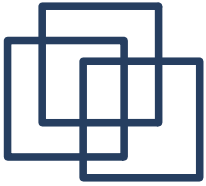




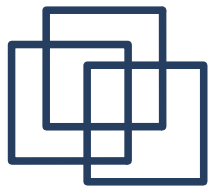
## Summary and outlook

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- **Pion on carbon reactions** are under investigation:
  - comprehensive analysis of inclusive, quasi-free and 2-3-particle correlations,
  - comparison to various transport models (SMASH, GIBUU, RQMD) and cascade INCL model – large dispersion of the predictions (
  - INCL++ does a **rather** good job for channels with detected pion  $p\pi^+$ ,  $p\pi^-$ .
- HADES and GSI pion beam facility is very unique tool to study electromagnetic structure of baryons via Dalitz decays.
- Cold nuclear matter studies with C target: important for the interpretation of in-medium hadron properties studied in HI collisions.

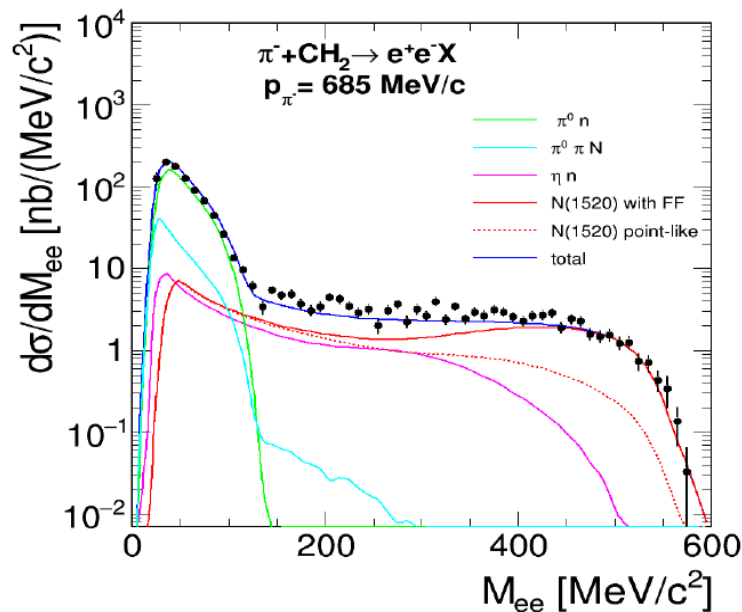


**Thank You  
for  
Your Attention**



# Inclusive e<sup>+</sup>e<sup>-</sup> cocktail

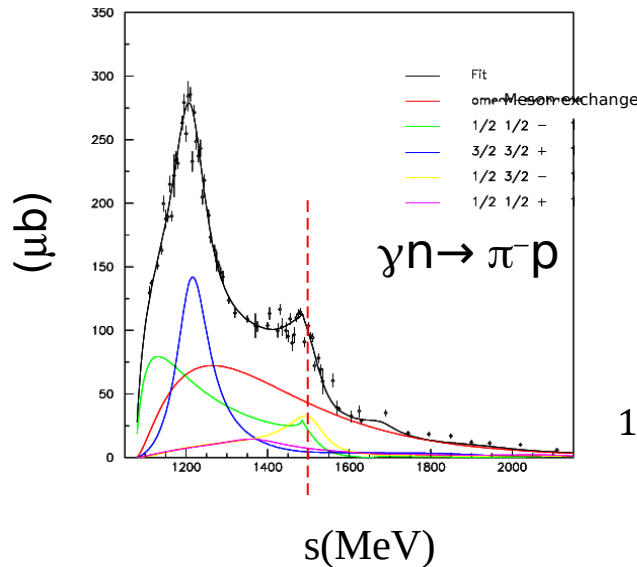
## Fixing cocktail ingredients



$\pi^- p \rightarrow n \pi^0$  [9 mb] (SAID)  
 $\pi^- p \rightarrow n \pi^0 \pi^0$  [1.9 mb] (L.-B.)  
 $\pi^- p \rightarrow p \pi^0 \pi^-$  [4.0 mb] (L.-B.)  
 $\pi^- p \rightarrow n \eta$  [0.83 mb]

**Dalitz Decay BR**  
 $\pi^0$ : 0.012  
 $\eta$ : 0.006

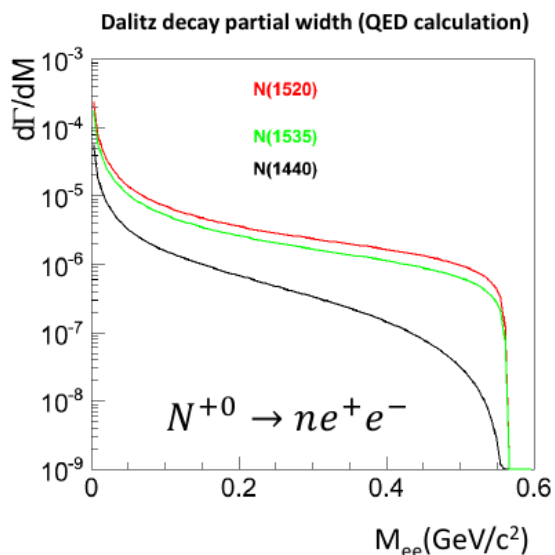
Arndt et al., PRC72 (2005) 045202



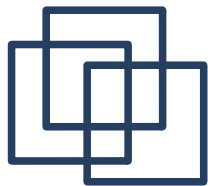
Bonn-Gatchina PWA

$N(1520) \text{ to } \pi^- p \rightarrow \gamma n$ : 21%  
 $N(1535) \text{ to } \pi^- p \rightarrow \gamma n$ : 15%

$$\sigma(\pi^- p \rightarrow n e^+ e^-) \sim 1.35 \alpha \sigma(\pi^- p \rightarrow n \gamma) = 2 \mu\text{b}$$

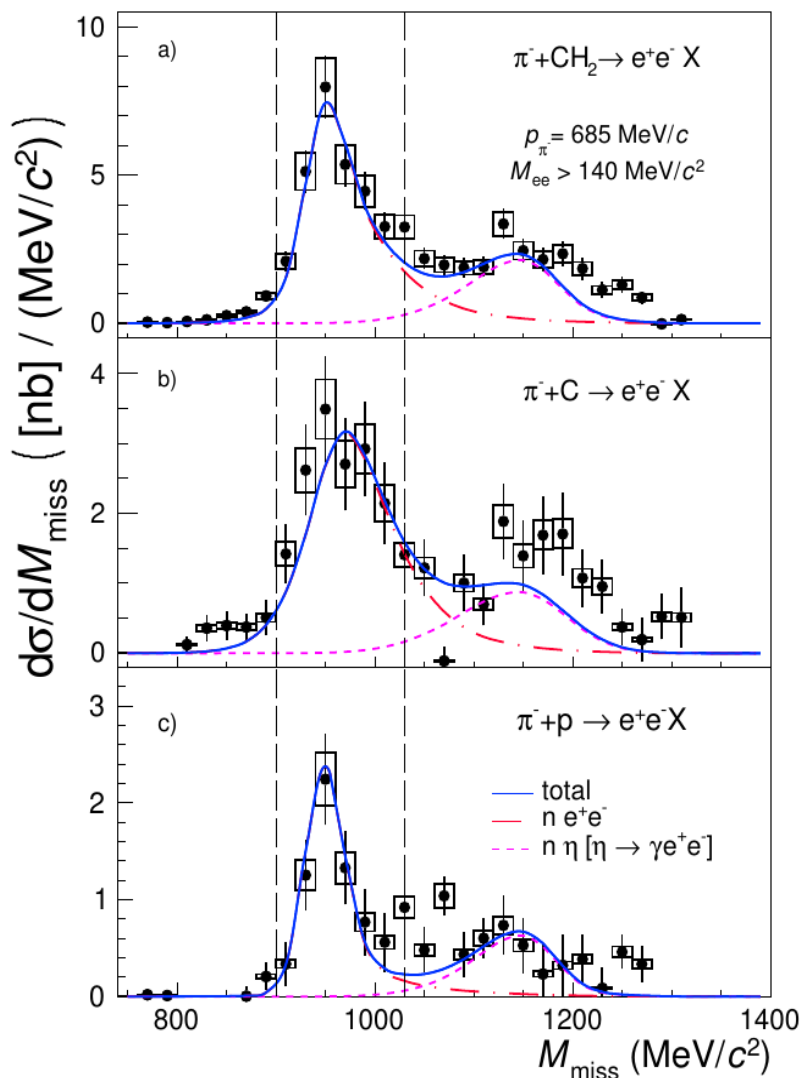


input for  $\pi^- p \rightarrow \gamma^*(e^+e^-)n$   
 QED Dalitz decay contribution



# Selection of quasi-free $\pi^- p \rightarrow n e^+ e^-$

HADES coll. arXiv:2205.15914 [nucl-ex]

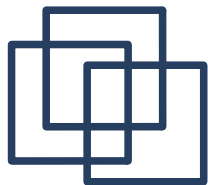


- cut on  $\text{inv} M_{e^+ e^-} > 140 \text{ MeV}$  (above  $\pi^0$  mass)
- missing mass cut on  $M_{\text{miss}}$  ( $\eta$  removed)

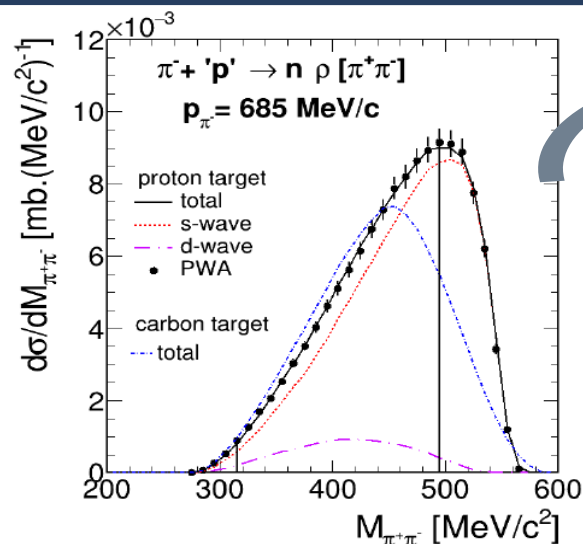
- $\pi^- \text{C}$  simulations using Pluto (qfs participant-spectator model)
- production cross sec. on C for:  $\pi^0$ ,  $\eta$ ,  $\rho$ ,  $\gamma$  deduced from the scaling:  $R_{C/H} = \sigma_C / \sigma_H$

- $\text{CH}_2$  target:

$$\left( \frac{d\sigma}{dM_{ee}} \right)_{\text{CH}_2} = \left( \frac{d\sigma}{dM_{ee}} \right)_C + 2 \left( \frac{d\sigma}{dM_{ee}} \right)_H$$

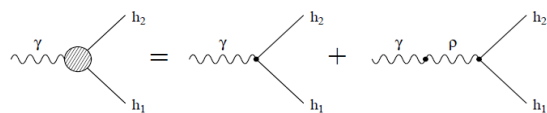


# Exclusive e<sup>+</sup>e<sup>-</sup> cocktail comparison to VMD1 and VMD2



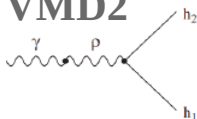
$$\left( \frac{d\sigma_{ee}}{dM_{ee}} \right)_{M_{ee}=M} = \left( \frac{d\sigma_{\pi\pi}}{dM_{\pi\pi}} \right)_{M_{\pi\pi}=M} \frac{\Gamma_{\rho \rightarrow e^+e^-}(M)}{\Gamma_{\rho \rightarrow \pi^+\pi^-}(M)}$$

**VMD1**



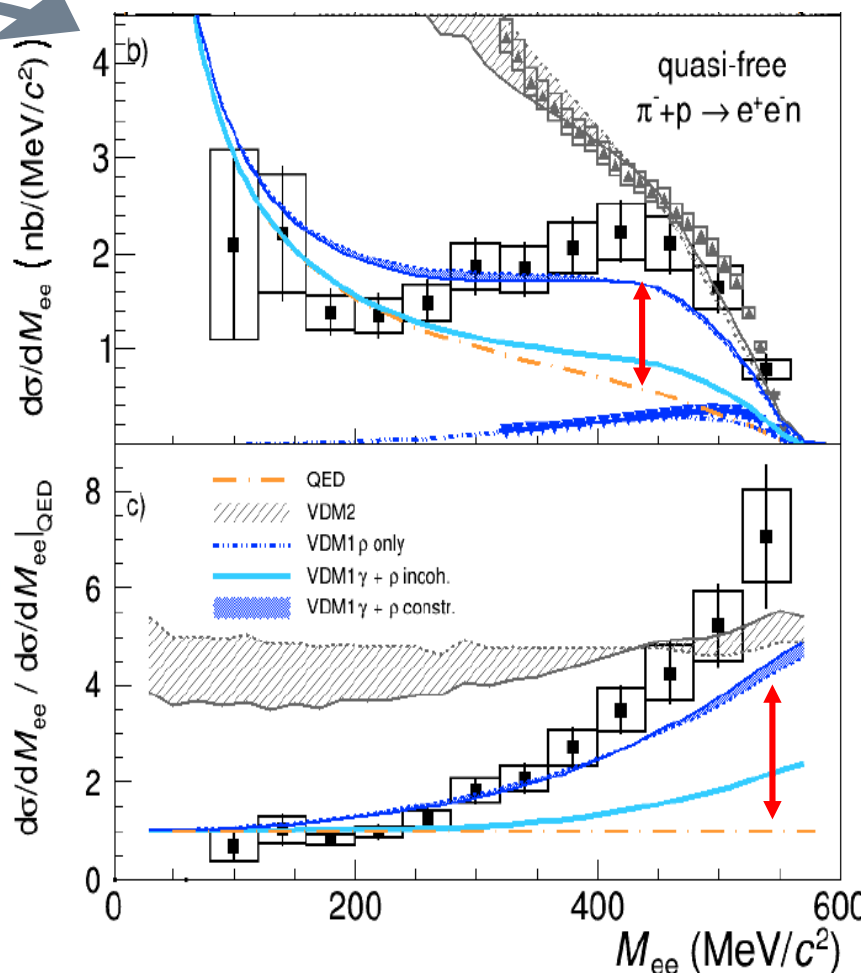
**reasonable  
description**

**VMD2**



**large  
overestimation**

HADES coll. arXiv:2205.15914 [nucl-ex]





- Characteristics of main properties of selected ("currently on market") transport models

Property	GiBUU	IQMD	UrQMD	RQMD.RMF	SMASH	PHSD
Relativistic Kinematics	optionally	n,p : no K : yes	yes	yes	yes	yes
Potential = Mean field	yes	n,p : no K : yes	no	optionally	yes	yes
Potential = sum of nucleon pots.	no	yes	yes	optionally	no	no
Electromagnetic potential	yes	yes	yes for baryons no for $\pi$	optionally	no	no
Momentum-dependent potential	yes	yes	no	yes	no	yes
Creation of LCP (clusters)	at end of simulation	at end of simulation	no	at end of simulation	at end of simulation	no
modifications of hadron mass in the medium	yes	yes	no	baryons: yes K, $\pi$ : no	no	yes
quark-gluon phase described by "strings"	yes	no	yes	yes	yes	yes



[Data Base](#)
[Meson Spectroscopy](#)
[Baryon Spectroscopy](#)
[NN-interaction](#)
[Formalism](#)

Data: 2016-2018

130 datasets

solutions: A. Sarantsev

**event-by-event**

cross sec. calculated for  
every fitted data event

$$f = - \sum_j^{N(data)} \ln \frac{\sigma_j(PWA)^{data}}{\sum_m \sigma_m(PWA)}$$

**HADES**  
unique data sets

$$A = \sum_{IJ\xi, \alpha} \bar{u}(q_1) A_{\gamma_1 \dots \gamma_n}^{IJ\xi, \alpha} F_{\mu_1 \dots \mu_n}^{\gamma_1 \dots \gamma_n}(p) N_{\mu_1 \dots \mu_n}^{\xi}(k^\perp) u(k_1)$$

**2 $\pi$  data included in the fit**

Reaction	Observable	W (GeV)	
$\gamma p \rightarrow \pi^0 \pi^0 p$	DCS, Tot	1.2-1.9	MAMI
$\gamma p \rightarrow \pi^0 \pi^0 p$	E	1.2-1.9	MAMI
$\gamma p \rightarrow \pi^0 \pi^0 p$	DCS, Tot	1.4-2.38	CB-ELSA
$\gamma p \rightarrow \pi^0 \pi^0 p$	$P, H$	1.45-1.65	CB-ELSA
$\gamma p \rightarrow \pi^0 \pi^0 p$	$T, P_x, P_y$	1.45-2.28	CB-ELSA
$\gamma p \rightarrow \pi^0 \pi^0 p$	$P_x, P_x^c, P_x^s$ (4D)	1.45-1.8	CB-ELSA
$\gamma p \rightarrow \pi^0 \pi^0 p$	$P_y, P_y^c, P_y^s$ (4D)	1.45-1.8	CB-ELSA
$\gamma p \rightarrow \pi^+ \pi^- p$	DCS	1.7-2.3	CLAS
$\gamma p \rightarrow \pi^+ \pi^- p$	$I^c, I^s$	1.74-2.08	CLAS
$\pi^- p \rightarrow \pi^0 \pi^0 n$	DCS	1.29-1.55	Crystal Ball
$\pi^- p \rightarrow \pi^+ \pi^- n$	DCS	1.45-1.55	HADES
$\pi^- p \rightarrow \pi^0 \pi^- p$	DCS	1.45-1.55	HADES