

New searching approaches of CP violation effects in the $\Xi^+{}_c\to pK^-\pi^+$ decays in the LHCb experiment

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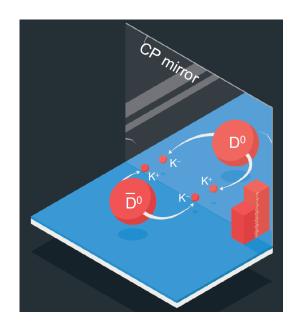
- Introduction
 - ♦ Why do we study flavour physics?
- CP asymmetry in charm
 - ♦ The first evidence of nonzero CP asymmetry in a specific charm meson decay
 - ♦ CP violation measurements in three-body charm baryons
 - ► Selection criteria of $\Xi_c^+ \rightarrow pK^-\pi^+$ and $\Lambda_c^+ \rightarrow pK^-\pi^+$
 - Mass distributions and statistics
 - The binned and unbinned results in control decays
 - Energy Test method
 - Kernel Density Estimation technique
- Summary

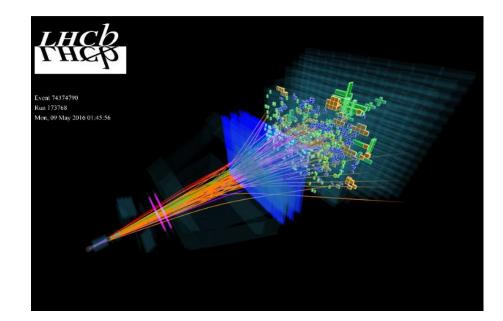


- The Standard Model is a theory which describes "well" existed data, but there are many phenomena which are not understood:
 - > Why are there three fermion generations? Only three?
 - Hierarchy in Yukawa couplings?
 - CP violation in quark sector is too small to explain the matter-antimatter asymmetry in the universe. Are there other sources of CP violation?
 - April '22: the measured W mass is different from the SM calculations! (CDF collaboration)

Why do we study flavour physics at hadronic machines?

- Flavour physics provides a unique window into new physics through indirect searches (potentially sensitive to higher energy scales than direct searches)
 - finding disagreement (in the LHCb) will be indirect indication of new phenomena existence



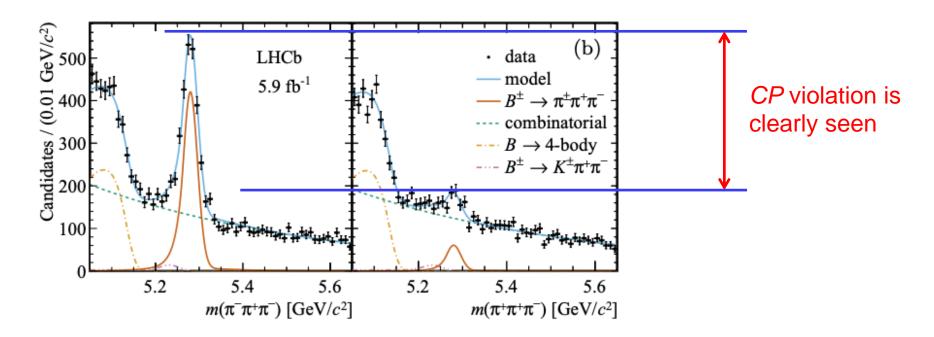


 Measurements of CP asymmetries in charm sector are very promising for searches for new physics signals

CP asymmetries: very different values!

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Local *CP* violation is ~75% in $B^{\pm} \rightarrow \pi^{\pm}\pi^{-}\pi^{+}$ (LHCb-PAPER-2021-049) The largest *CP* asymmetry ever observed!



- In charm sector:
 - in the SM, the expected *CP* violation is very small $≤ 10^{-4} 10^{-3}$
 - o the LHCb measurement (PRL 122 (2019) 211803)

 $\Delta A_{CP} \equiv A_{CP}(K^+K^-) - A_{CP}(\pi^+\pi^-) = (-1.54 \pm 0.29) \cdot 10^{-3}$

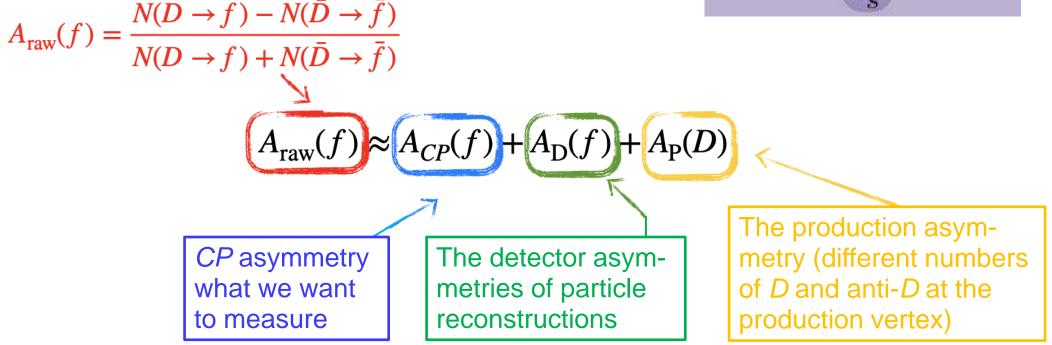
new physics contributions can enhance CP violation up to 10⁻²
 Int.J.Mod.Phys.A21(2006)5381 ;
 Ann.Rev.Nucl.Part.Sci.58(2008)249

Measuring asymmetry between matter and antimatter



- The $D^0 \rightarrow K^-K^+$ and $D^0 \rightarrow \pi^-\pi^+$ decays are used to measure the time integrated *CP* asymmetry
- The measured raw asymmetry A_{raw} may be written as a sum of components that are physics and detector effects:

prompt D^{o} π^{+}/K^{+} D^{*+} D^{*+} D^{0} π^{-}/K^{-}

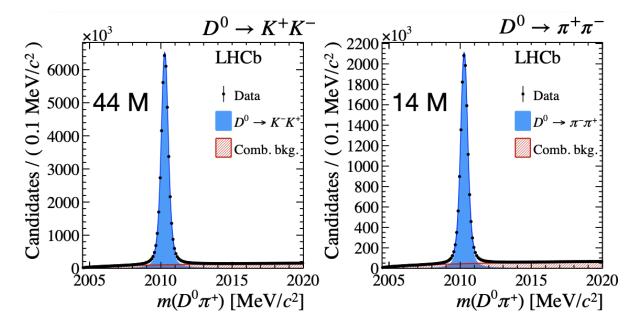


The A_{raw} , A_D and A_P are order ~2% or smaller but A_{CP} is smaller than 10⁻³

- The detector asymmetries for K^-K^+ and $\pi^-\pi^+$ cancel since the final states are charge symmetric
- The A_P is independent of the final state and this term cancels in the first order if we subtract raw asymmetries

$$A_{\rm raw}(K^+K^-) - A_{\rm raw}(\pi^+\pi^-) = A_{CP}(K^+K^-) - A_{CP}(\pi^+\pi^-) \equiv \Delta A_{CP} = (-1.54 \pm 0.29) \cdot 10^{-3}$$
(5.3 σ)

PRL 122 (2019) 211803
$$\Delta A_{CP} = \left[a_{CP}^{dir}(K^-K^+) - a_{CP}^{dir}(\pi^-\pi^+)\right] + \frac{\Delta \langle t \rangle}{\tau} a_{CP}^{ind}$$
[JHEP 1106 (2011) 089]



- 2015-2018, 5.7/fb
- Observable is mainly sensitive to direct *CP* asymmetry
- Indirect *CP* asymmetry is smaller than 10%



$$\Delta A_{CP} \equiv A_{CP}(K^+K^-) - A_{CP}(\pi^+\pi^-) = (-1.54 \pm 0.29) \cdot 10^{-3}$$
PRL 122 (2019) 211803

Two possibilities:

- A_{CP}(K⁺K⁻) and A_{CP}(π⁺π⁻) have the same magnitude but different sign (unlikely today)
- Asymmetries are significantly different: $A_{CP}(K^+K^-)$ is a few times smaller then $A_{CP}(\pi^+\pi^-)$

for example,

"CP violation in D decays to two pseudoscalars: A SM-based calculation"

- E. Solomonidi, BEACH 2022 Conference in Cracow
- Nonetheless, to properly determine and investigate the source of potential CP violation, one has to examine the single asymmetry



LHCb-PAPER-2022-024, arXiv:2209.03179

• Measuring time integrated asymmetry of single mode is much harder

$$A(K^{-}K^{+}) \approx A_{CP}(K^{-}K^{+}) + A_{P}(D^{*+}) + A_{D}(\pi_{tag}^{+})$$

• A_P and A_D are determined using control samples with negligible *CP* asymmetry

$$\begin{aligned} A(K^{-}\pi^{+}) &\approx A_{\rm P}(D^{*+}) - A_{\rm D}(K^{+}) + A_{\rm D}(\pi^{+}) + A_{\rm D}(\pi^{+}_{\rm tag}), \\ A(K^{-}\pi^{+}\pi^{+}) &\approx A_{\rm P}(D^{+}) - A_{\rm D}(K^{+}) + A_{\rm D}(\pi^{+}_{1}) + A_{\rm D}(\pi^{+}_{2}), \\ A(\overline{K}^{0}\pi^{+}) &\approx A_{\rm P}(D^{+}) + A(\overline{K}^{0}) + A_{\rm D}(\pi^{+}), \\ A(\phi\pi^{+}) &\approx A_{\rm P}(D^{+}_{s}) + A_{\rm D}(\pi^{+}), \\ A(\overline{K}^{0}K^{+}) &\approx A_{\rm P}(D^{+}_{s}) + A(\overline{K}^{0}) + A_{\rm D}(K^{+}). \end{aligned}$$



LHCb-PAPER-2022-024, arXiv:2209.03179

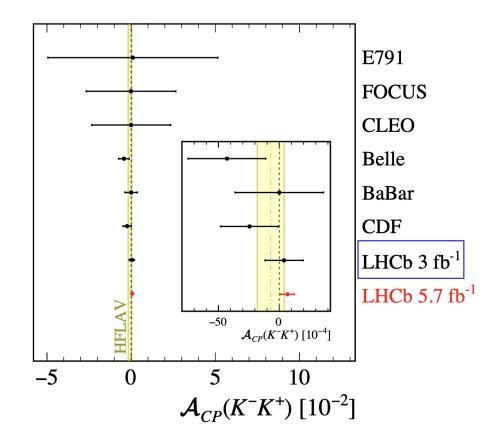
The measured CP asymmetry (Run 2 only):

 $\mathcal{A}_{CP}(K^-K^+) = [6.8 \pm 5.4 \,(\text{stat}) \pm 1.6 \,(\text{syst})] \times 10^{-4}$

The value is consistent with zero but can be subtracted from ΔA_{CP}

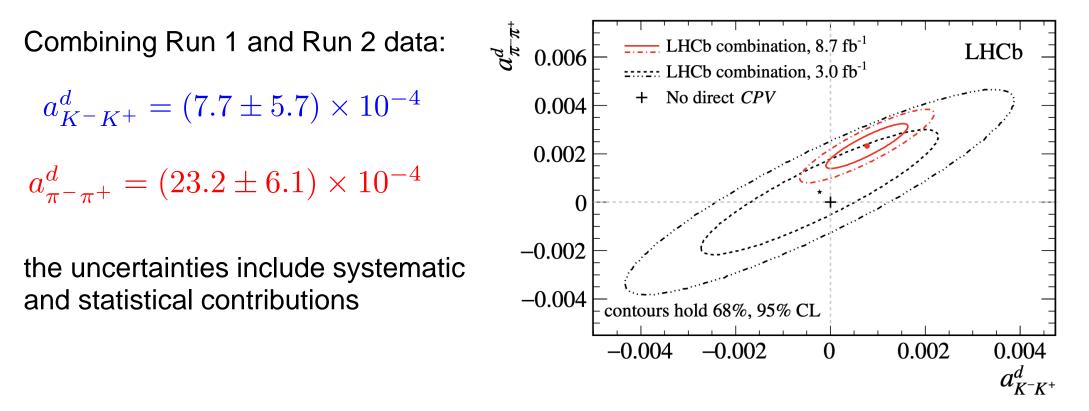
Assuming that CP is conserved in mixing and in the interference between decay and mixing ΔY

$$\mathcal{A}_{CP}(f) \approx a_f^d + \frac{\langle t \rangle_f}{\tau_D} \cdot \Delta Y_f$$
$$\Delta Y_{K^-K^+} = \Delta Y_{\pi^-\pi^+} = \Delta Y$$





LHCb-PAPER-2022-024, arXiv:2209.03179



The direct *CP* asymmetries deviate from zero by 1.4 and 3.8 standard deviations for $D^0 \rightarrow K^- K^+$ and $D^0 \rightarrow \pi^- \pi^+$

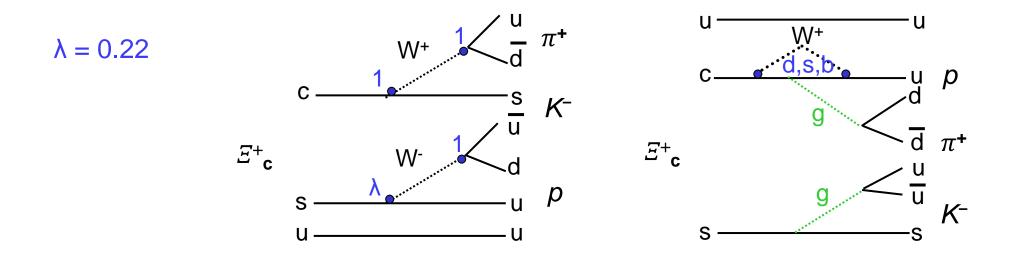
This is the first evidence for direct CP violation in a specific charm decay

Results departure from U-spin symmetry ($a^d_{K^-K^+} + a^d_{\pi^-\pi^+} = 0$) of 2.7 σ



The $\Xi^+_c \rightarrow pK^-\pi^+$ decays are singly Cabibbo-suppressed decays = place of *CP* violation in the Standard Model

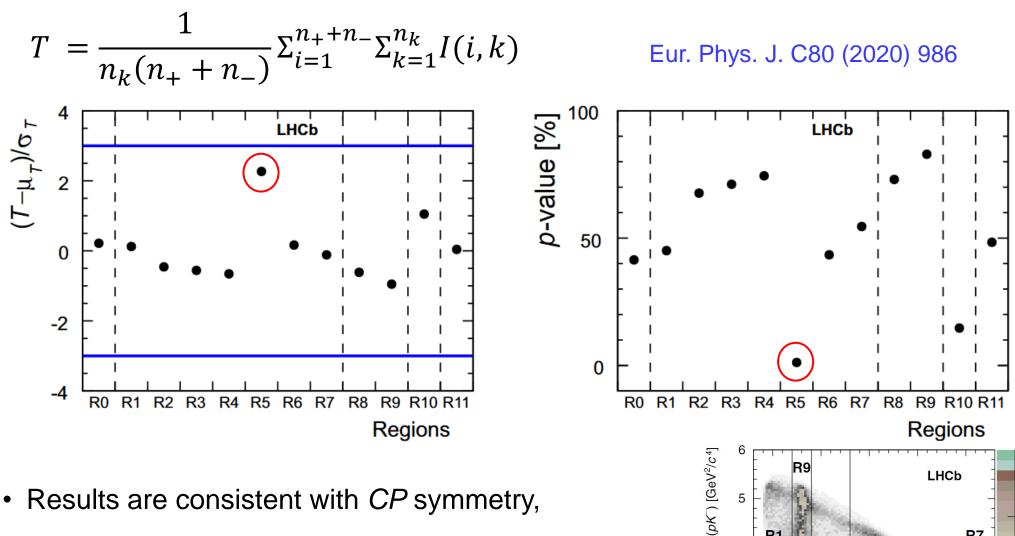
• Data collected in Run 1, $\sqrt{s} = 7$ TeV and 8 TeV, L = 3 fb⁻¹ [Eur. Phys. J. C80 (2020) 986],



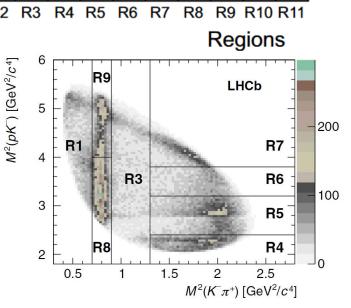
- If tree and penguin processes interfere with different phases for Ξ_c^+ and Ξ_c^- then *CP* symmetry is broken
- Penguin diagram opens possibilities for new particles exchange

The k-nearest neighbour method





- Local effect in one region corresponds to 2.7σ,
- It is worth to continue analysis with Run 2 data.



Selection - overview

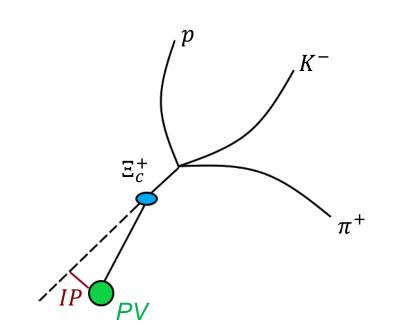


Proton/Kaon/Pion

- PID
- ProbNN
- $IP\chi^2$
- TRACK_GhostProb
- momentum

Charm baryon

- Vertex $\chi^2/ndof$
- $IP\chi^2$
- p_T
- DIRA
- $FD\chi^2$
- Pseudorapidity η
- Lifetime τ



Goal is to maxmize signal reducing background.

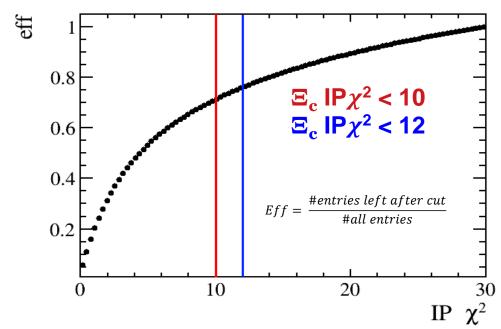
Figure of Merit:
$$FoM = \frac{S}{\sqrt{S+B}}$$

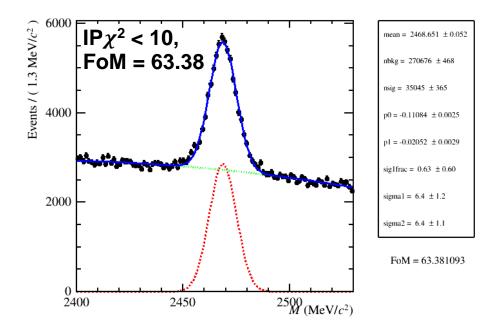
S - no. signal candidates, B - no. Background candidates



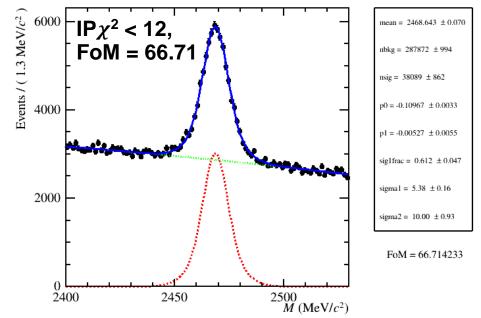
Selection process - $\Xi_c IP\chi^2$

An example





cut	8	10	12	15
S	37k	35k	38k	38k
В	244k	270k	288k	313k
FoM	69	63	67	64
	Eff ~ 78%			



New approach for searching for CP asymmetry in charm baryons



Finally, the following cuts were chosen:

Proton/Kaon/Pion

- PID >10/>-10/<12
- ProbNN >0.5/>0.1/>0.1
- $IP\chi^2$
- TRACK_GhostProb < 0.4
- momentum
 - proton: 15<P<100 GeV

>9

- kaon: 3<P<150 GeV
- pion: 3<P<150 GeV

Charm baryon

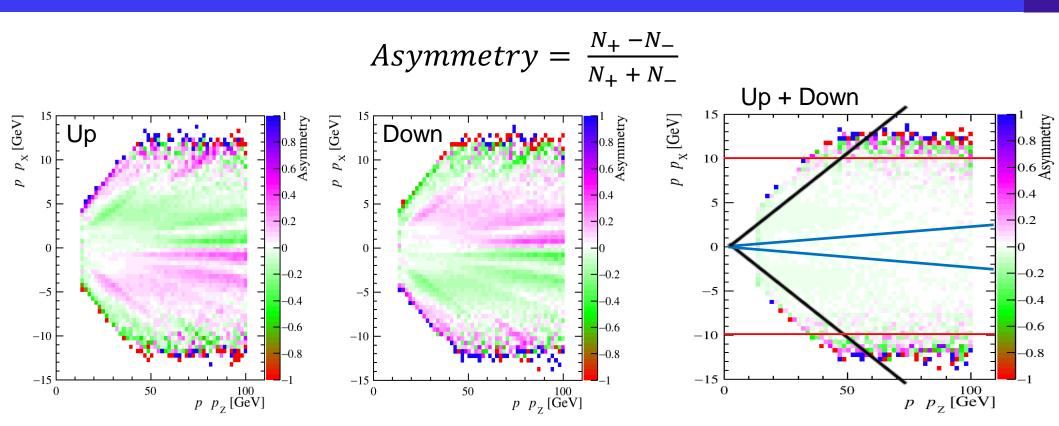
- Vertex $\chi^2/ndof$
- $IP\chi^2$
- p_T
- DIRA
- FDχ²
 Pseudorapidity η
- Lifetime τ (0.0005, 0.0015) *ns*

- <12 4< p_T <16 GeV
- >0.99995
- <2000

<8

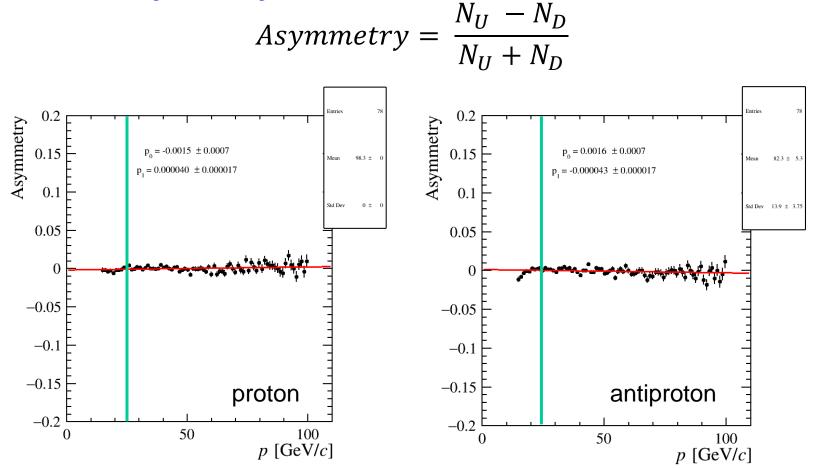
 η (2;4,5)

Fiducial cuts



- Geometry of the detector can be not uniform
- After adding MagUp and MagDown data samples the detector effects will remain
- Large detector asymmetries are expected in the external regions and close to the beam axis

 Due to different cross section for interacting with the material of the detector particles and antiparticles can be reconstructed disparately which leads to reconstruction asymmetry

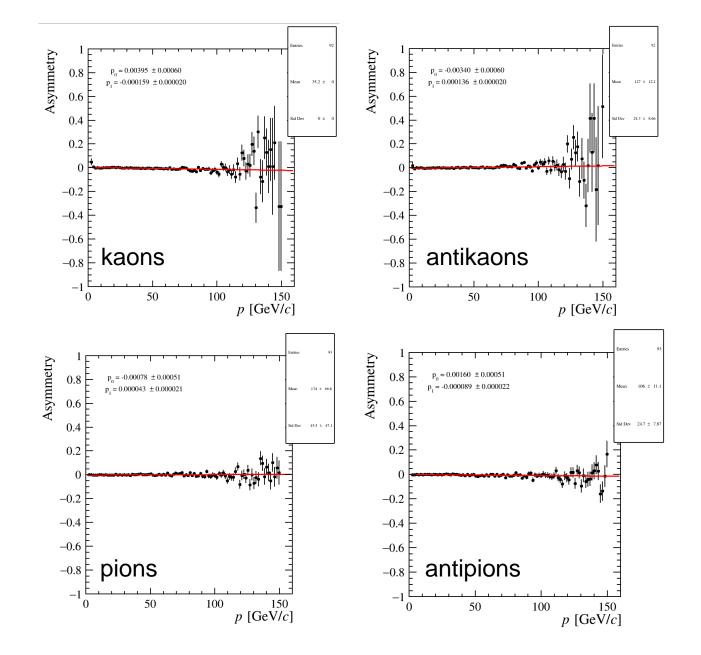


Protons and antiprotons with p < 25 GeV are rejected



Reconstruction effects for kaons and pions





Kaons are rejected if: p < 15 GeV Pions are rejected if: p < 15 GeV

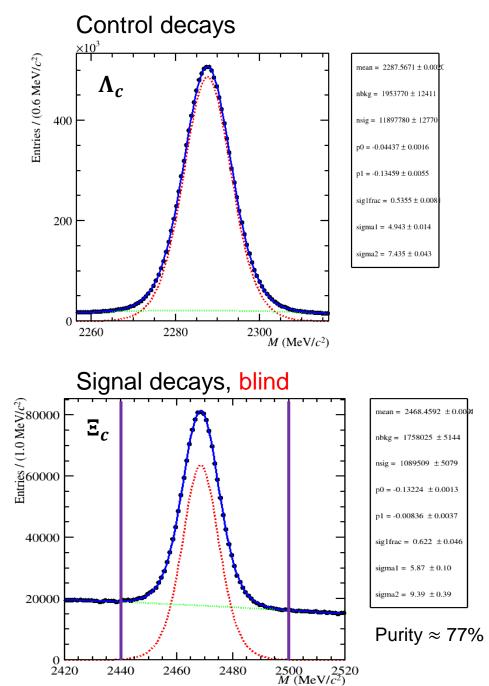
The largest reconstruction effects are for protons

The Run 2 final statistics



	Ξ _c (Mass Peak +/-20 MeV)	۸ _c
2016	554090	4133105
2017	584235	4644854
2018	648538	5073606
Run 2	1786863	13851565

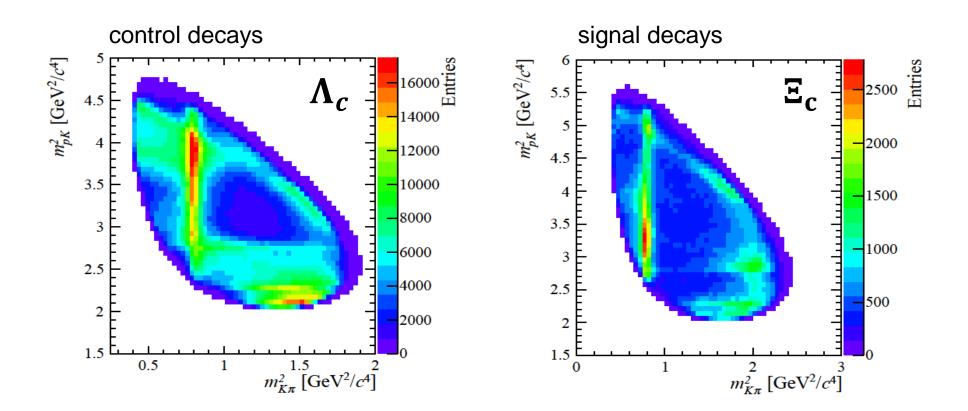
- ~ 1.09 mln \(\mathbf{E}_{C}\) candidates (only signal, from fit)
 - (> 5 times more than in Run 1 !)
- ~ 14 mln Λ_c candidates



The Dalitz plots



2018 data



The intermediate resonances are different for control decays and signal decays.

The S_{CP} method

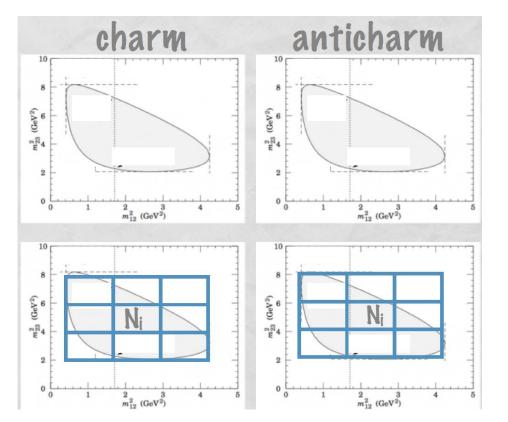


The method is based on dividing the phase space into n bins. For each bin, significance of the difference between number of particles (N+) and antiparticles (N-) is computed, using the following expression:

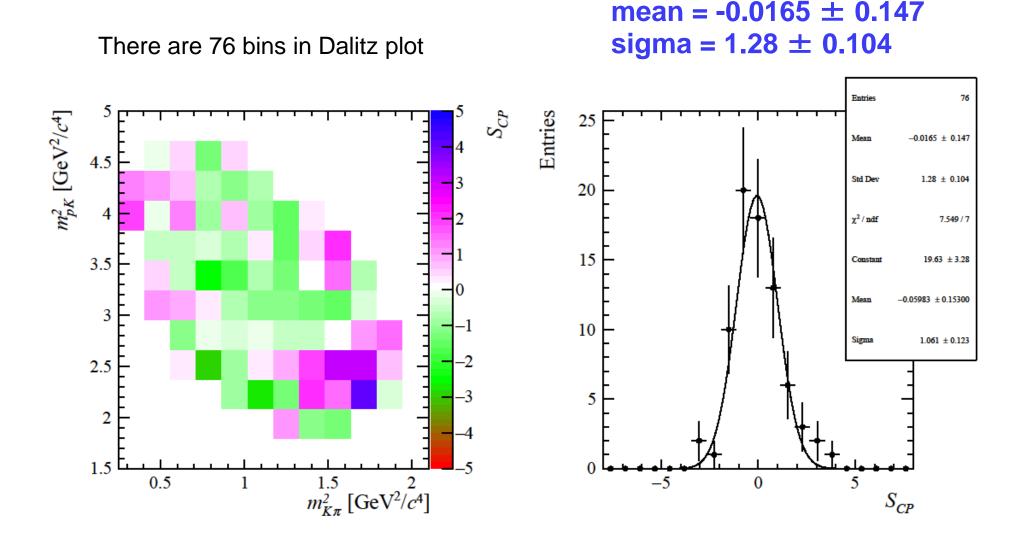
$$S_{CP}^{i} = \frac{N_i^+ - \alpha N_i^-}{\sqrt{\alpha (N_i^+ + N_i^-)}}$$

where $\alpha = N+/N-$ accounts for global asymmetries

 $\chi^2/ndf = \sum_i S_{CP}^i / (nbins-1)$ No CPV: $S_{CP} \sim N(0,1)$ CPV: p-value $\ll 1 (5\sigma \sim 6 \times 10^{-7})$



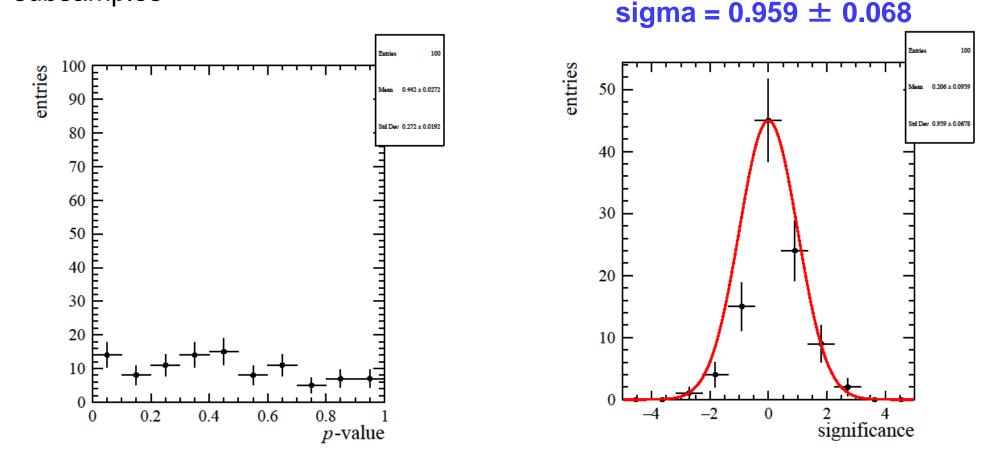




No fake signal of CPV in control decays

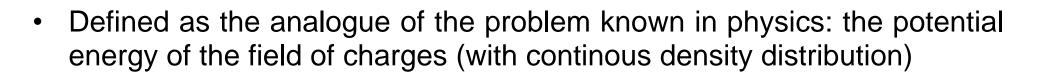


The whole sample is divided into 100 subsamples



The p-value distribution is flat as expected - no fake signal of CPV

mean = 0.206 ± 0.096



- Energy is minimum when two distribution are identical (total charge = 0)
- Can be used to compare two PDFs, denoted as f_a and f_p :

$$\phi = \frac{1}{2} \int \int (f_p(\vec{x}) f_p(\vec{x}') + f_a(\vec{x}) f_a(\vec{x}') - 2f_p(\vec{x}) f_a(\vec{x}')) K(\vec{x}, \vec{x}') d\vec{x} d\vec{x}'$$

where K is integral kernel. It is a metric that defines distance in the multivariate space.

Usually we use Gaussian distance function:

$$K(\vec{x}, \vec{x}') = \exp(-\frac{(\vec{x} - \vec{x}')^2}{2\delta})$$

where δ governs the width of the Gaussian



• ET can be estimated without the need for any knowledge about the forms of f_a or f_p :

$$\mathsf{T} = \phi = \frac{1}{n(n-1)} \sum_{i,j>i}^{n} K(|\vec{x_i} - \vec{x_j}|) + \frac{1}{m(m-1)} \sum_{i,j>i}^{m} K(|\vec{x_i}' - \vec{x_j}'|) - \frac{1}{nm} \sum_{i=1}^{n} \sum_{j=1}^{m} K(|\vec{x_i} - \vec{x_j}'|)$$

Null hypothesis H_0 : $f_p = f_a$:

- ϕ value for overall samples = nominal ϕ value
- We need control set of φ values (permuted φ values) for which the null hypothesis holds:
 - We calculate ϕ values for symmetric samples:
 - Mix the data together and randomly assign events to two new samples
- Next step is to calculate p-value:

 $p = \frac{\text{number of permuted } T \text{ values greater than nominal } T}{\text{total number of permuted } T \text{ values}}$

- If $f_p = f_a$ then p-value is uniformly distributed on [0,1]
- If $f_p \neq f_a$ then p-value $\rightarrow 0$





Λ_c control samples:

		10k permutations			
	2016	2017	2018	Run 2	
T-value	6.62839 · 10 ⁻⁷	8.1397 · 10 ⁻⁸	1.67794 · 10 ⁻⁷	2.99603 · 10 ⁻⁷	
p-value	0.0137	0.2385	0.129	0.0021	

No fake signal of CPV

The ET results in toy samples: no CPV



 max-perm = 50 n-perm = 1000, n-perm = 5000, n-perm = 10000, 	p-value = 0.808 p-value = 0.766 p-value = 0.766	 max-perm = 500 n-perm = 1000, p-value = 0.778 n-perm = 5000, p-value = 0.76
max-perm = 100		• n-perm = 10000, p-value = 0.765
• n-perm = 1000,	p-value = 0.767	max-perm = 2000
 n-perm = 5000, n-perm = 10000, 	p-value = 0.784 p-value = 0.775	 n-perm = 1000, p-value = 0.769 n-perm = 5000, p-value = 0.7714
max-perm = 200		• n-perm = 10000, p-value = 0.7724
 n-perm = 1000, n-perm = 5000, n-perm = 10000, 	p-value = 0.762 p-value = 0.762 p-value = 0.762	1.0 0.9 - 50 100 200 500 2000
Sample with 200k entries		
No fake signal of CPV		0.6 -

test number

The ET results in 5% toy sample



Sample with 200k entries

CPV: 5% difference in amplitudes of K^{*} resonance

5 mln permutations

p-value = 9.2987 \cdot **10**⁻⁷

CPV is confirmed

Power of the method:

 ET is sensitive to CPV if it is 5% in K* and 200k events (1/5 of Run 2 statistics)



Kernel Density Estimation (KDE)

Data

0

Data value

2

4

Kernel Density Estimation is a non-parametric method:

$$f(\hat{x}) = \frac{1}{n} \sum_{i=1}^{n} \omega(x - x_i, h)$$

where: $\omega(t,h) = \frac{1}{h}K(\frac{t}{h})$ is weighting function.

K is the kernel function, h – bandwidth parameter In this analysis I use triangle kernel:

$$\omega(t,h) = \begin{cases} \frac{1}{h} \left(1 - \frac{|t|}{h}\right) for |t| < h \\ 0 & otherwise \end{cases}$$

8

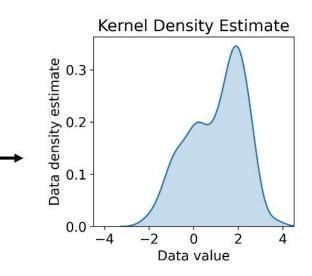
Number observed

0

-4

-2

Common kernel functions



KDE example:

26/05/2023



- Significant impact in KDE performance
- Globally determined bandwidth:

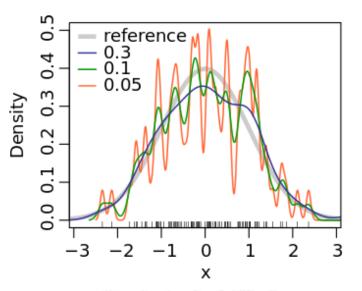
 $h = k \, \hat{S} N^{-0.2}$

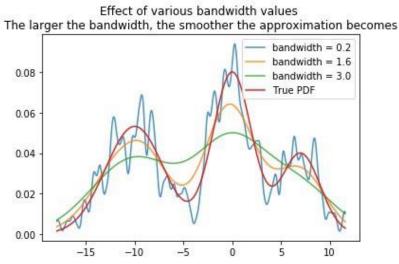
where k – correction parameter (1.06), \hat{S} - standard deviation of the sample, N – sample size

• Adaptive bandwidth parameter hopt:

$$h_{opt}^i = \frac{h}{\sqrt{f(x_i)}}$$

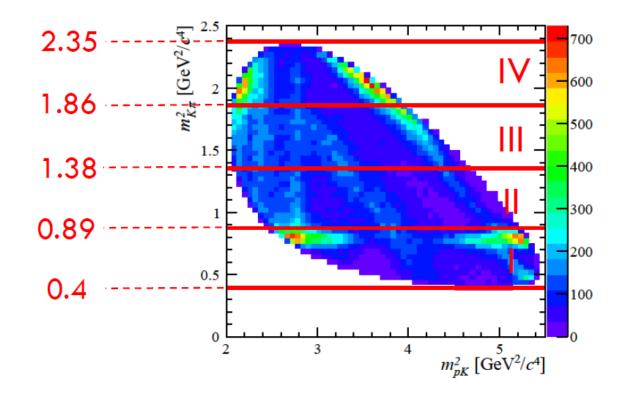
 Whole proces can be repeated multiple times





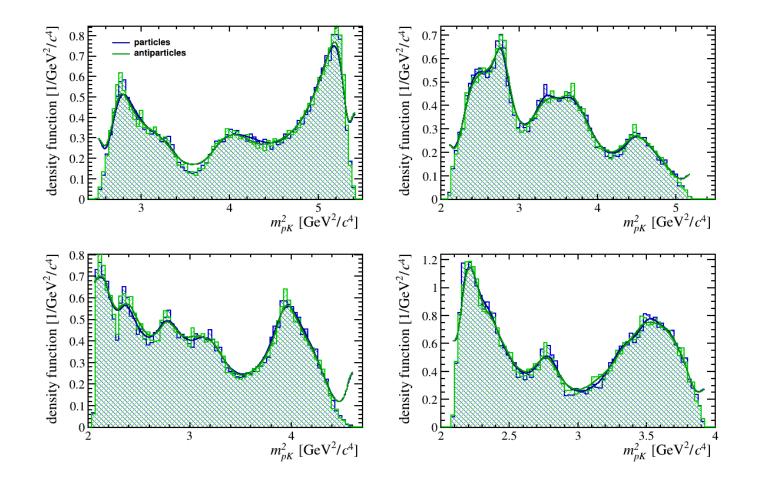


- Toy sample with no *CPV*
- 200k entries in each sample (100k particles and 100k antiparticles),
- The Dalitz plots are split into four kinematic regions, each of which is subsequently projected onto the horizontal axis.



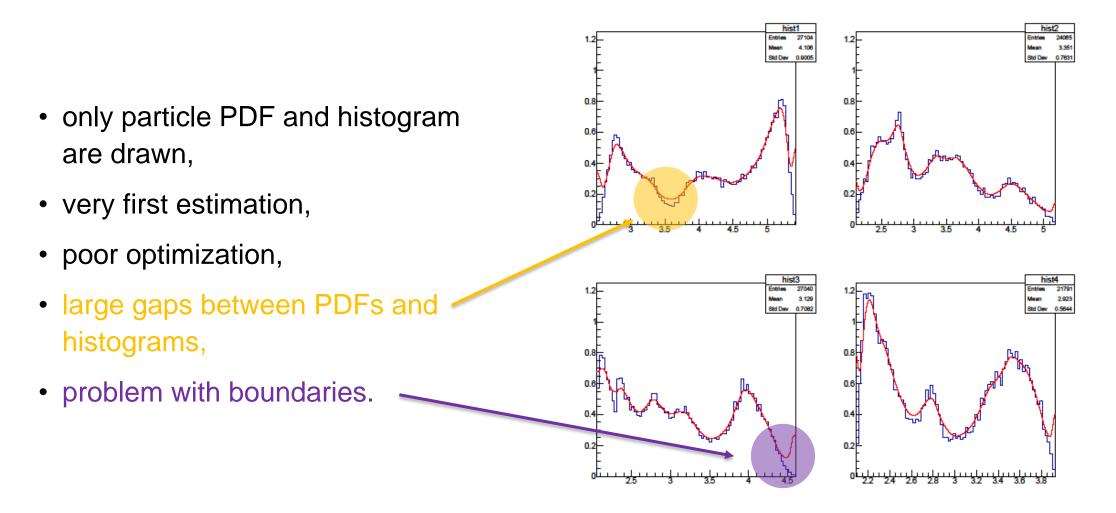


• There are no visible differences between particle and antiparticle density functions – as expected

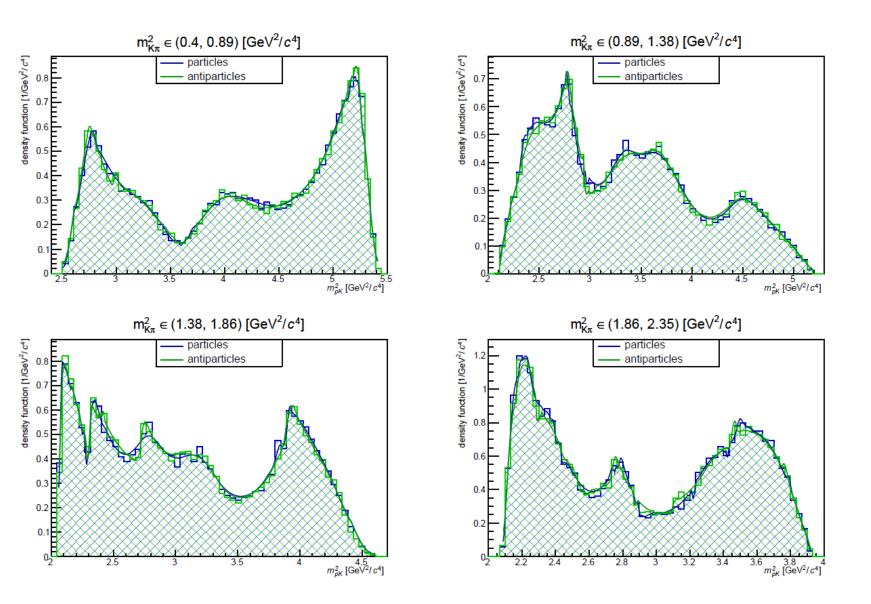


Smoothing parameter optimization



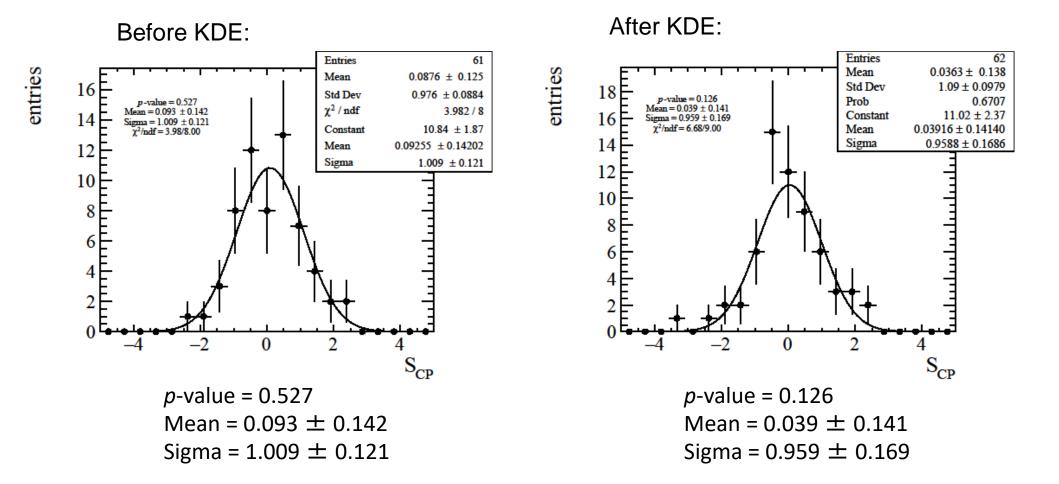






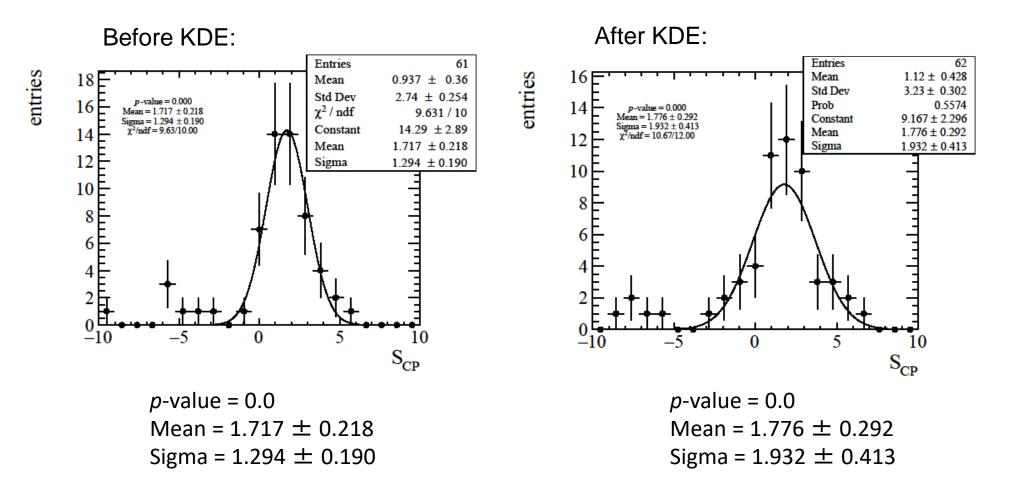


KDE can used to improve the sensitivity of the S_{CP} method



The S_{CP} results after KDE implementation look reasonable





The CPV is confirmed as it should be



• The first evidence for direct *CP* violation in a specific charm hadron decay

$$a_{K^-K^+}^d = (7.7 \pm 5.7) \times 10^{-4}$$

 $a_{\pi^-\pi^+}^d = (23.2 \pm 6.1) \times 10^{-4}$

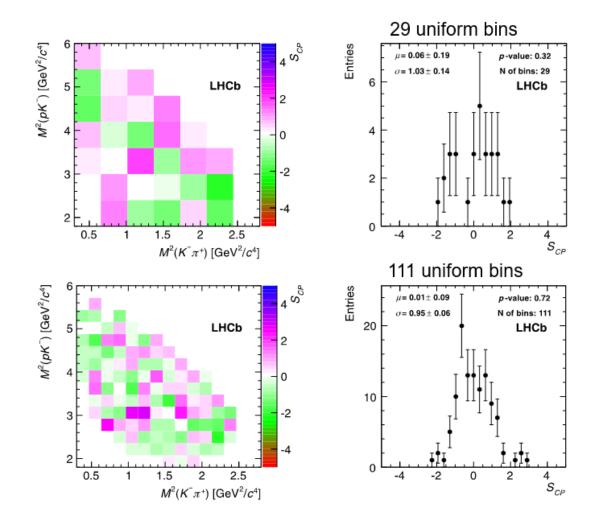
- So far, in any baryon decays the measured CP-violating asymmetries are compatible with the hypothesis of CP symmetry
- New measurements of CP asymmetries in Ξ⁺_c → pK⁻π⁺ decays are expected using binned S_{CP} and unbinned Energy Test methods improved with Kernel Density Estimation technique
 - ✓ The methods are tested in control $\Lambda_c^+ \to pK^-\pi^+$ decays as well as in toy samples
 - ✓ The methods do not generate fake signal of CP violation and confirms its existence if exists





The S_{CP} method





- p-values > 32%
- S_{CP} agree with N(0,1)
- Results are consistent with CP symmetry

The kNN method



The kNN tests whether baryons and antibaryons share the same parent distribution function.

$$T = \frac{1}{n_k(n_+ + n_-)} \sum_{i=1}^{n_+ + n_-} \sum_{k=1}^{n_k} I(i, k)$$

Under the null hypothesis $T \sim N(\mu_T, \sigma_T)$:

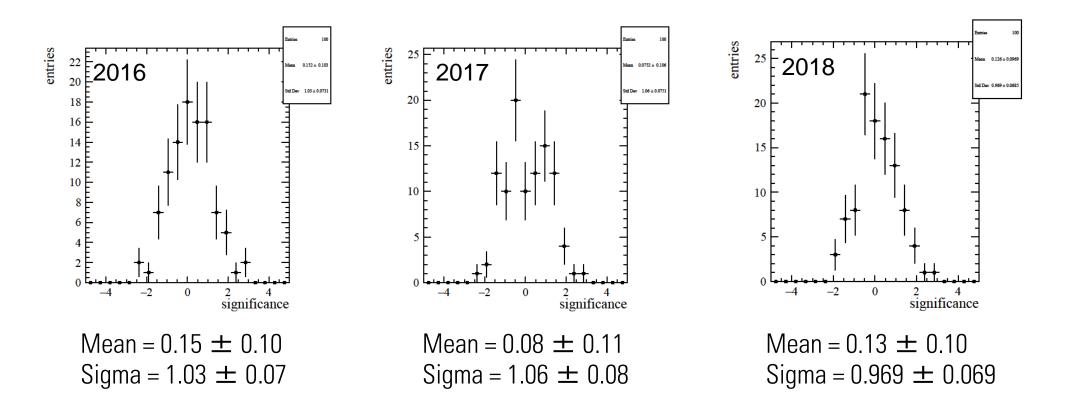
$$\mu_T = \frac{n_+ (n_+ - 1) + n_- (n_- - 1)}{n(n-1)}$$

$$\lim_{n,n_k,D\to\infty} \sigma_T^2 = \frac{1}{nn_k} \left(\frac{n_+n_-}{n^2} + \frac{4n_+^2n_-^2}{n^4} \right)$$

[J. Am. Stat. Assoc. 81, 799 (1986)]



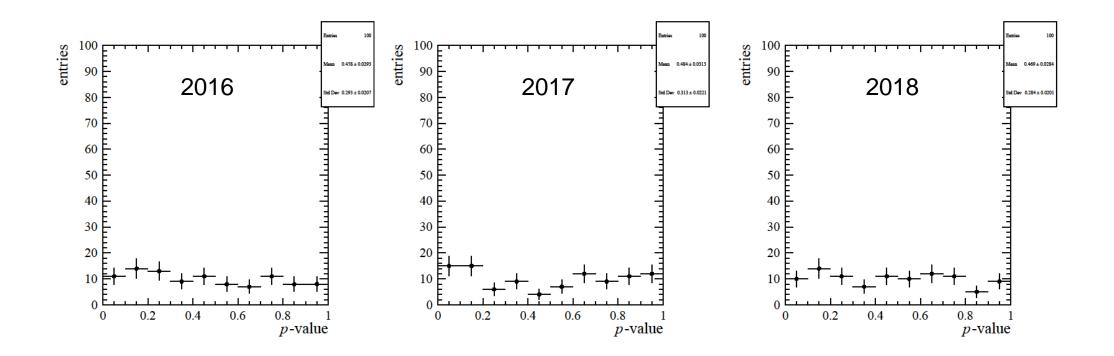
The S_{CP} method is performed individually for each year of data taking



Means agree with 0, sigmas agree with 1 Conclusion: No fake signal of CPV.



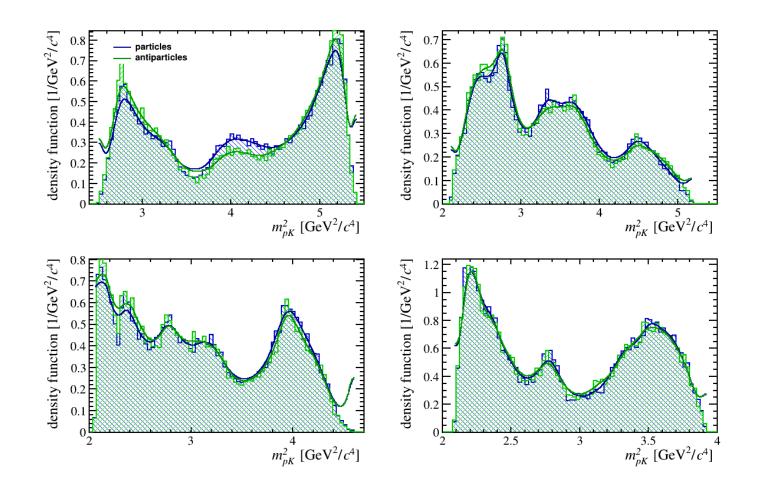
100 random subsamples for each year of data taking.



Flat distributions => Conclusion: No fake signal of CPV.

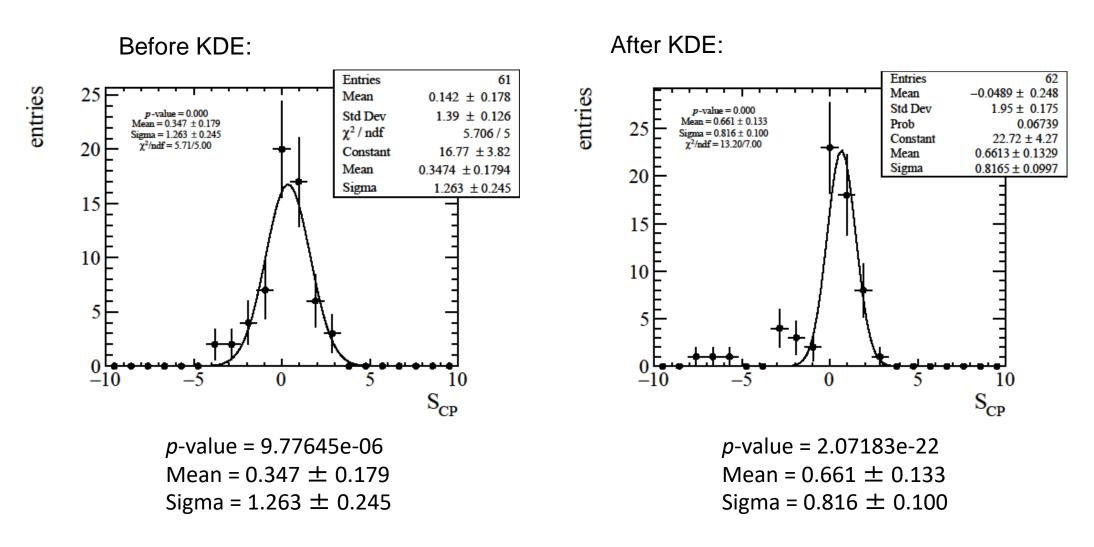
KDE results: 20% CP sample

- Difference between particles and antiparticles is clearly visible,
- KDE works properly,
- Next steps: Compute p-value and optimize bandwidth,



KDE 2D scenario in toy sample with 5% CPV



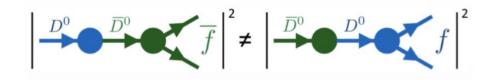


New approach for searching for CP asymmetry in charm baryons

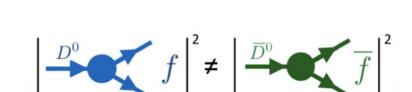
Three ways of CP violation in the Standard Model



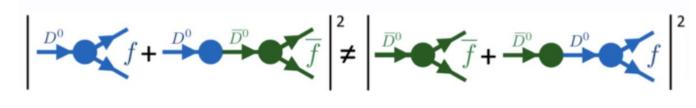
- **1.** In the mixing (only neutral particles) $P^0 \rightarrow anti P^0 \neq anti P^0 \rightarrow P^0$



2. In the amplitudes of direct decays (neutral and charge particles) $P^{\pm} \rightarrow f \neq anti-P^{\pm} \rightarrow anti-f$



3. In the interference between direct decays and decays via mixing (only neutral particles)

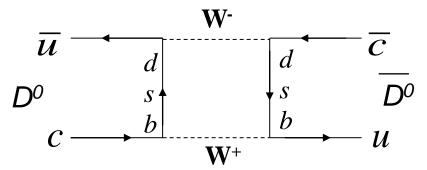


Mixing and decay processes can be mediated via loop diagrams. New physics is likely to enter in loops where new particles can be exchanged.

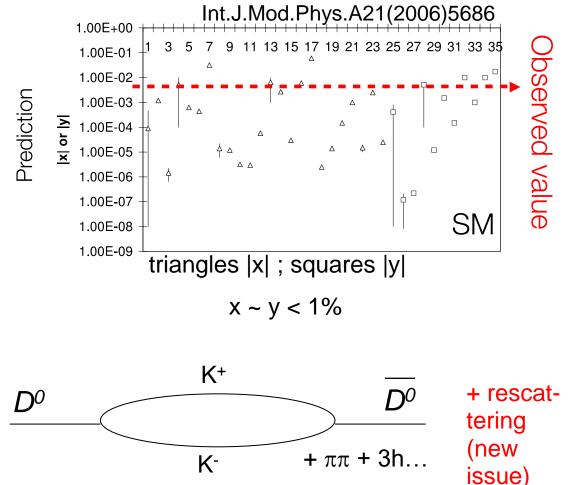


The Standard Model predictions for charm

- Predicted CPV in charm sector is very small $\leq 10^{-4} - 10^{-3}$ (much smaller than in the beauty sector)
- The SM predictions vary widely
- New physics contributions can enhance CPV up to 10⁻²
 Int.J.Mod.Phys.A21(2006)5381 ; Ann.Rev.Nucl.Part.Sci.58(2008)249



Mixing via box diagram, short range



Mixing via hadronic intermediate states, long range (difficult to calculate)

Perfect place for new physics searching (small background from the SM) Since *CP* violation, *x* and *y* are very small, we need very precise detector to measure observables with extremely high accuracy \rightarrow LHCb at LHC

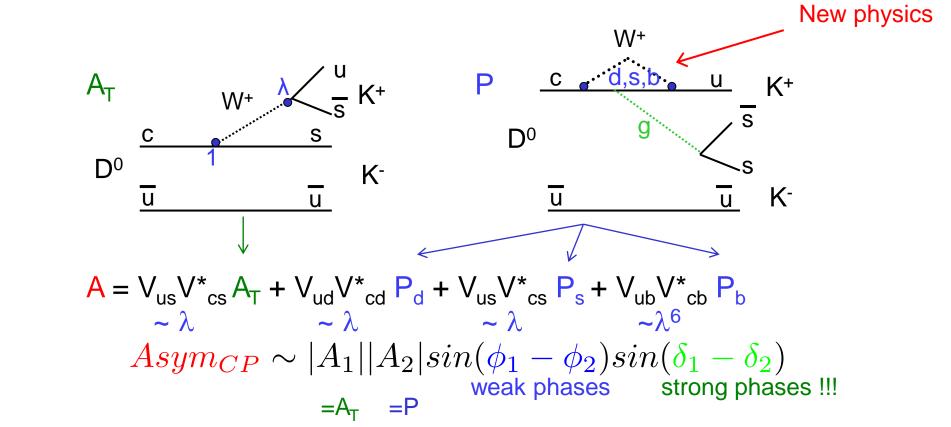
CP violation in direct decays



Singly Cabibbo-suppressed decay (SCS):

- a place for CP violation in the Standard Model (only)
- both: tree and penguin diagrams

 $\lambda = 0.22$



To observe *CP* violation, at least two amplitudes must interfering with different weak phases AND DIFFERENT STRONG PHASES

Measurement of *CP* asymmetry in $D^0 \rightarrow K^-K^+$



LHCb-PAPER-2022-024, arXiv:2209.03179

Data from Run 2:

37M of $D^0 \rightarrow K^-K^+$ decays

58M of $D^0 \rightarrow K^-\pi^+$ decays 188M of $D^+ \rightarrow K^-\pi^+\pi^+$ decays 6M of $D^+ \rightarrow K^0\pi^+$ decays 43M of $D^+_s \rightarrow \phi\pi^+$ decays 5M of $D^+ \rightarrow K^0K^+$ decays

