

EXPLORING THE PROPERTIES OF HOT QCD MATTER IN THE QUASIPARTICLE APPROACH

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Outlook

1 What do we study?

- Quark-gluon plasma & its transport properties

2 What do we use?

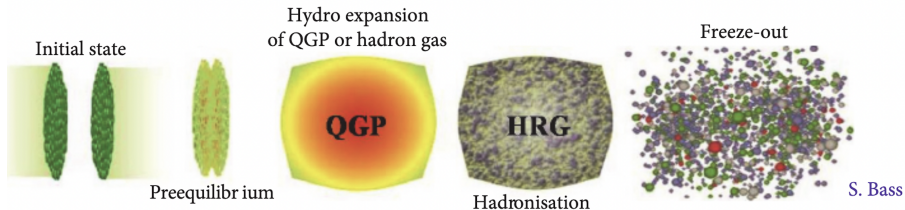
- Quasiparticle model & kinetic theory

3 What did we find?

- Transport parameters - shear & bulk viscosities, ...

Quark-Gluon Plasma

- Subject of Quantum ChromoDynamics (QCD) – theory of strong interactions
- Strongly coupled fluid produced in heavy ion collisions:



- Phase of matter in extreme conditions: $T \geq 155$ MeV, $\tau \simeq 10$ fm
- Mixture of *deconfined* quarks and gluons

Transport Phenomena in hot QCD

Longitudinal motion - friction between layers - shear viscosity η

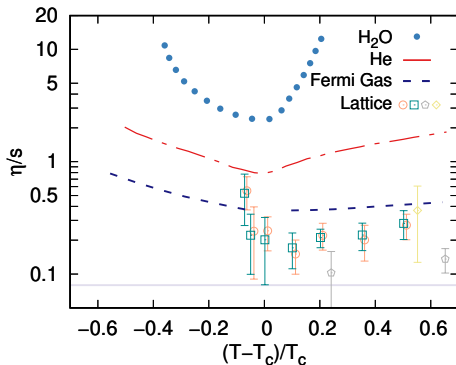


Resistance to volume expansion/compression- bulk viscosity ζ



+ electrical conductivity, heat conductivity ...

Transport Phenomena in Hot QCD



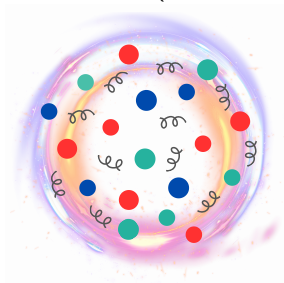
Lattice QCD data for gluon plasma (no quarks)

[V.M., "Transport Properties of Hot QCD Matter in the Quasiparticle Approach", PhD Thesis]

Quasiparticle Model

- similar to massive quasidelectron moving freely in solid states

Real QGP:

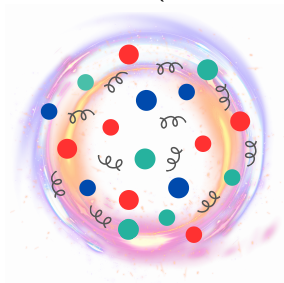


strongly-interacting particles,
constant (bare) masses m_i^0

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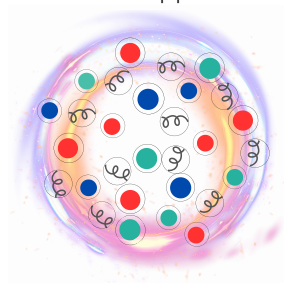
Real QGP:



strongly-interacting particles,
constant (bare) masses m_i^0



Effective approach:



weakly-interacting **quasiparticles**,
dynamical $m_i[T, G(T)]$

Quasiparticle Model

Quasiparticles are „dressed” with effective masses $m_i[G(T), T]$:

$$m_i[G(T), T] = \sqrt{(m_i^0)^2 + \Pi_i[G(T), T]} \quad (1)$$

self-energies Π_i from perturbative QCD:

$$\text{gluons: } \Pi_g[G(T), T] = \left(3 + \frac{N_f}{2}\right) \frac{G^2(T)}{6} T^2 \quad (2)$$

$$\text{quarks: } \Pi_{l,s}[G(T), T] = 2 \left[m_{l,s}^0 \sqrt{\frac{G^2(T) T^2}{6}} + \frac{G^2(T) T^2}{6} \right] \quad (3)$$

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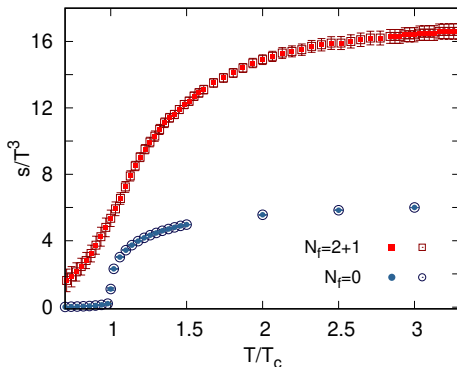
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➡ effective coupling $G(T)$ – reliable thermodynamics – lattice QCD

Quasiparticle Model

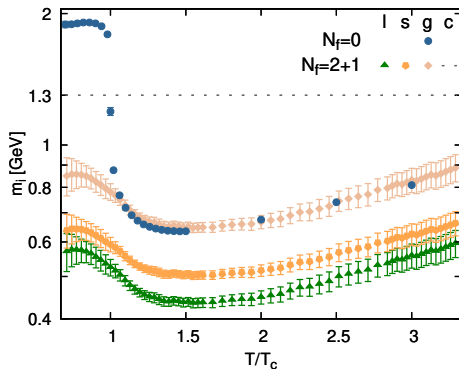
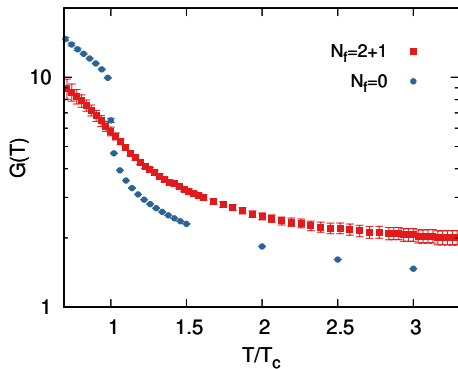
$$s(T) \simeq \sum_{i=g,l,s,\dots} \int d^3p ([1 \pm f_i^0] \ln[1 \pm f_i^0] \mp f_i^0 \ln f_i^0) = \text{lattice data} \rightarrow G(T)$$

$$f_i^0(E_i) : E_i[G(T), T] = \sqrt{p^2 + m_i^2[G(T), T]} \quad (4)$$



[V.M, M. Bluhm, C. Sasaki, K. Redlich, PRD 100 (2019); lattice: Wuppertal-Budapest]

Effective Coupling and Masses

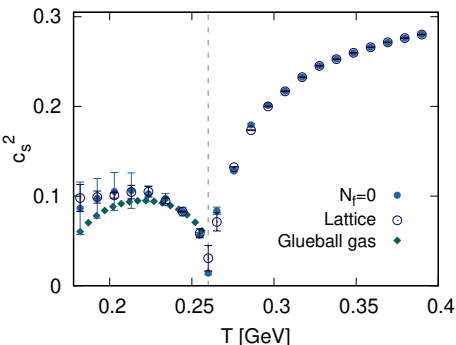


$$m_i[G(T), T] \gg m_l^0 = 5 \text{ MeV}, m_s^0 = 95 \text{ MeV}$$

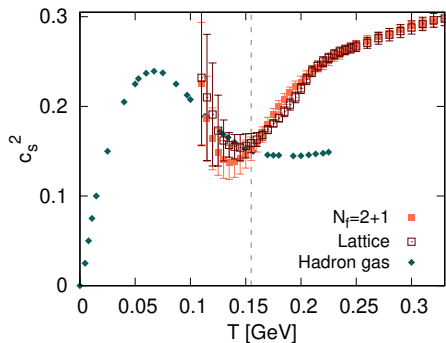
Thermodynamic Consistency

$$c_s^2 = \frac{\partial P}{\partial \epsilon} = \frac{s}{T} \left(\frac{\partial s}{\partial T} \right)^{-1}$$

Pure SU(3), $N_f = 0$



QCD, $N_f = 2 + 1$



☞ Ideal gas: $c_s^2 = 1/3$ vs Quasiparticle model: $c_s^2 \rightarrow 1/3$ as $T \rightarrow \infty$

Kinetic Theory: Relaxation Time Approximation

Boltzmann Equation:

$$p^\mu \partial_\mu f_i = \mathcal{C}[f_i] \sim \int \omega (f'_i f'_j - f_i f_j) \quad (5)$$

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$$p^\mu \partial_\mu f_i = C[f_i] \sim \int \omega(f_i' f_j' - f_i f_j) \simeq -\frac{f_i - f_i^0}{\tau_i} \quad (6)$$

Approximate solution: f_i relaxes to equilibrium value f_i^0 in time τ_i

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Pure gluon plasma ($N_f = 0$):

$$\tau_g = \frac{1}{n_g^0 \bar{\sigma}_{gg \rightarrow gg}} = [n_g^0 \bar{\sigma}_{gg \rightarrow gg}]^{-1}; \quad n_i^0 \sim \int f_i^0 \quad (7)$$

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Quark-gluon plasma ($N_f = 2 + 1$):

$$\tau_g = [n_g^0 (\bar{\sigma}_{gg \rightarrow gg} + \bar{\sigma}_{gg \rightarrow l\bar{l}} + \bar{\sigma}_{gg \rightarrow s\bar{s}}) + n_l^0 \bar{\sigma}_{gl \rightarrow gl} + n_s^0 \bar{\sigma}_{gs \rightarrow gs}]^{-1} \quad (8)$$

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→ Compute transport coefficients in the τ -approximation

Kinetic Theory: Relaxation Time Approximation

Shear viscosity (reaction to flow): $\rightarrow \eta_g, \zeta_g$ for gluon plasma ($N_f = 0$)

[Hosoya, Kajantie, NPB250 '85]

$$\eta = \frac{1}{15T} \sum_{i=g,l,s,\dots} d_i \int \frac{d^3p}{(2\pi)^3} \frac{p^4}{E_i^2} f_i^0 (1 \pm f_i^0) \tau_i \quad (9)$$

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Bulk viscosity (reaction to volume expansion/compression):

[Bлум, Kämpfer, Redlich, PRC 84 '11]

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Kinetic Theory: Relaxation Time Approximation

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Electrical conductivity:

$\rightarrow \sigma_g = 0$

[Srivastava, Thakur, Patra, PRC 91 '15]

$$\sigma = \frac{1}{3T} \sum_{i=u,d,s,\dots} q_i^2 d_i \int \frac{d^3p}{(2\pi)^3} \frac{p^2}{E_i^2} f_i^0 (1 - f_i^0) \tau_i \quad (10)$$

Kinetic Theory: Relaxation Time Approximation

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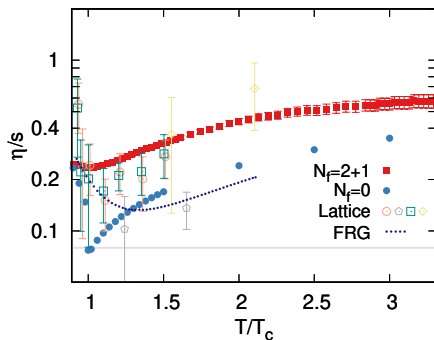
Electrical conductivity: $\rightarrow \sigma_g = 0$
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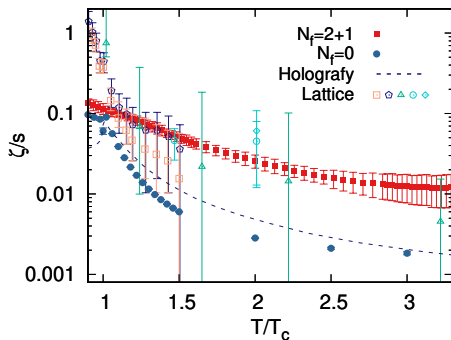
* common relaxation times τ_i

Shear and Bulk Viscosities: $N_f = 0$ vs $N_f = 2 + 1$

Shear viscosity (flow)



Bulk viscosity (volume)

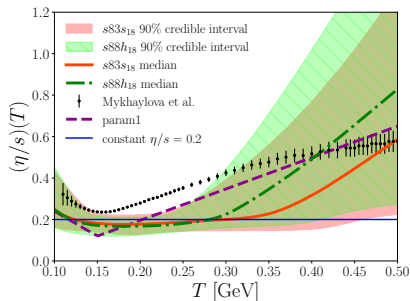
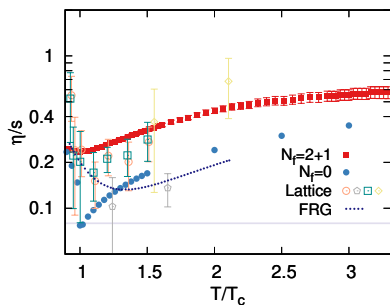


← time

- ★ Dynamical quarks increase viscosities of hot QCD matter
- ★ Faster restoration of conformal invariance for gluon plasma

[V. M., C. Sasaki, PRD103 '21; V. M., M. Bluhm, K. Redlich, C. Sasaki, PRD100 '19]

Specific Shear Viscosity

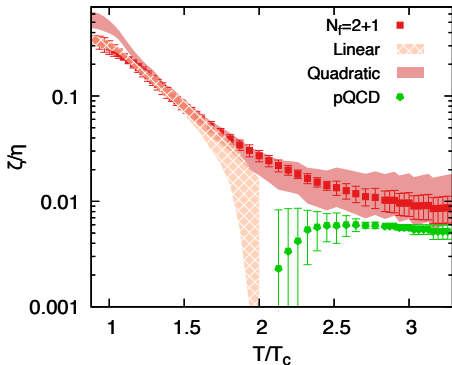
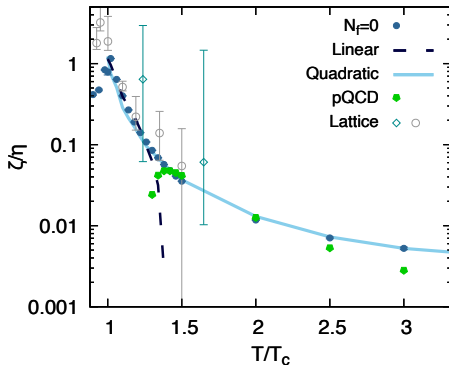


[V.M., M. Bluhm, K. Redlich, C. Sasaki, PRD100 '19; Auvinen, Eskola, Huovinen, Niemi, Paatelainen, Petreczky, PRC 102 '20]

Non-Perturbative vs Perturbative QCD Regimes

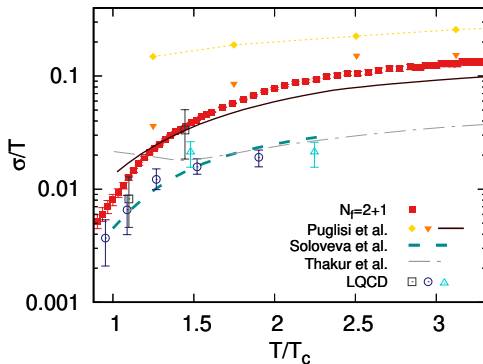
Linear: $\frac{\zeta}{\eta} \propto \left(\frac{1}{3} - c_s^2\right)$ – AdS/CFT (strong G) [Buchel, PRD 72 '05]

Quadratic: $\frac{\zeta}{\eta} \propto \left(\frac{1}{3} - c_s^2\right)^2$ – pQCD (weak G) [Weinberg, Astrophys. J. 168 '71]



[V.M., C. Sasaki, PRD 103 '21; pQCD: Arnold, Moore, Yaffe, JHEP 05 '03; Arnold, Dogan, Moore, PRD 74 '06]

Electrical Conductivity of QGP



★ Overall agreement with other models and with lattice at low T

Lattice: $m_\pi \approx 384$ MeV \implies larger bare quark masses

[V. M. and C. Sasaki, PRD 103 '21; V.M. EPJ ST 229 '20, Lattice: G. Aarts et al., JHEP 02 (2015)]

Summary

- ☞ **Quark-gluon plasma** – peculiar state of matter with unique properties and a lot of open questions.
- ☞ **Quasiparticle model** – well-established tool connecting non-perturbative and perturbative QCD regimes (strong vs weak coupling).
- ☞ **Possibilities** – finite μ , quasihadrons out of chemical equilibrium, $N_f = 2 + 1 + 1$, momentum anisotropy...

THANK YOU FOR ATTENTION!